Last class

- Fitness level
 - Original fitness level
 - Refined fitness level
- Drift analysis
 - Additive drift
 - Multiplicative drift
 - Negative drift
- Switch analysis
- Results of running time analysis





Heuristic Search and Evolutionary Algorithms

Lecture 11: Evolutionary Algorithms for Multi-objective Optimization

Chao Qian (钱超)

Associate Professor, Nanjing University, China

Email: qianc@nju.edu.cn

Homepage: http://www.lamda.nju.edu.cn/qianc/

Multi-objective optimization: optimize multiple objectives (which are usually conflicting) simultaneously

$$max_{x \in \mathcal{X}} (f_1(x), f_2(x), ..., f_m(x))$$
 feasible solution space, consisting of all solutions satisfying the constraints

• x weakly dominates y, denoted as $x \ge y$, if

$$\forall i \in \{1,2,...,m\}: f_i(x) \ge f_i(y)$$

• x dominates y, denoted as x > y, if

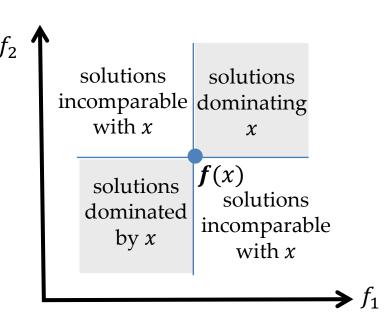
$$\forall i \in \{1,2,...,m\}: f_i(x) \ge f_i(y) \text{ and } \exists i \in \{1,2,...,m\}: f_i(x) > f_i(y)$$

• x is incomparable with y, if neither $x \ge y$ nor $y \ge x$

Multi-objective optimization: optimize multiple objectives (which are usually conflicting) simultaneously

$$max_{x \in \mathcal{X}} \left(f_1(x), f_2(x), \dots, f_m(x) \right)$$

Bi-objective maximization



Multi-objective optimization: optimize multiple objectives (which are usually conflicting) simultaneously

$$max_{x \in \mathcal{X}} \left(f_1(x), f_2(x), \dots, f_m(x) \right)$$

A solution is Pareto optimal if no other solution dominates it

The collection of objective vectors of all Pareto optimal solutions is called the Pareto front

The goal of multi-objective optimization is to find a set of solutions whose objective vectors cover the Pareto front

Multi-objective optimization: optimize multiple objectives (which are usually conflicting) simultaneously

$$max_{x \in \mathcal{X}} \left(f_1(x), f_2(x), \dots, f_m(x) \right)$$

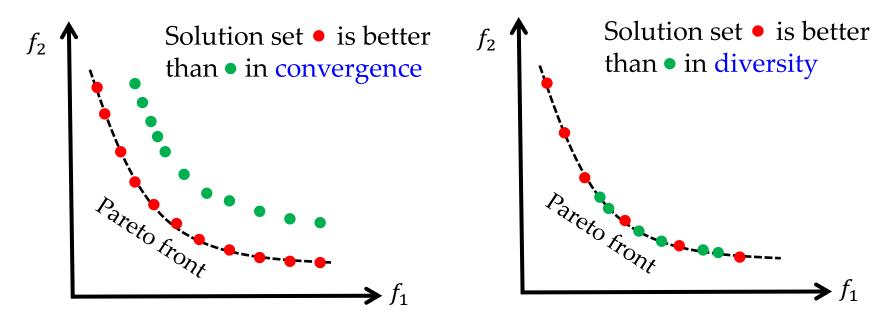
However, the size of Pareto front can be exponentially large

In practice, we want to find a set of solutions that is good in terms of:

- Convergence (to the Pareto front)
- Diversity (along the Pareto front)

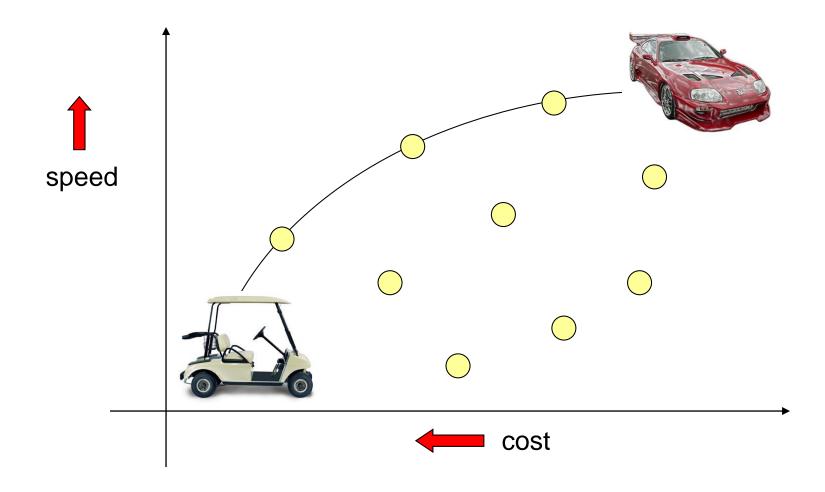
Multi-objective optimization: optimize multiple objectives (which are usually conflicting) simultaneously

$$max_{x \in \mathcal{X}} \left(f_1(x), f_2(x), \dots, f_m(x) \right)$$

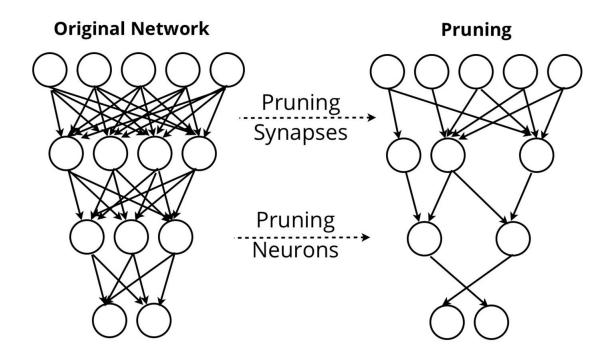


Bi-objective minimization

Example of multi-objective optimization

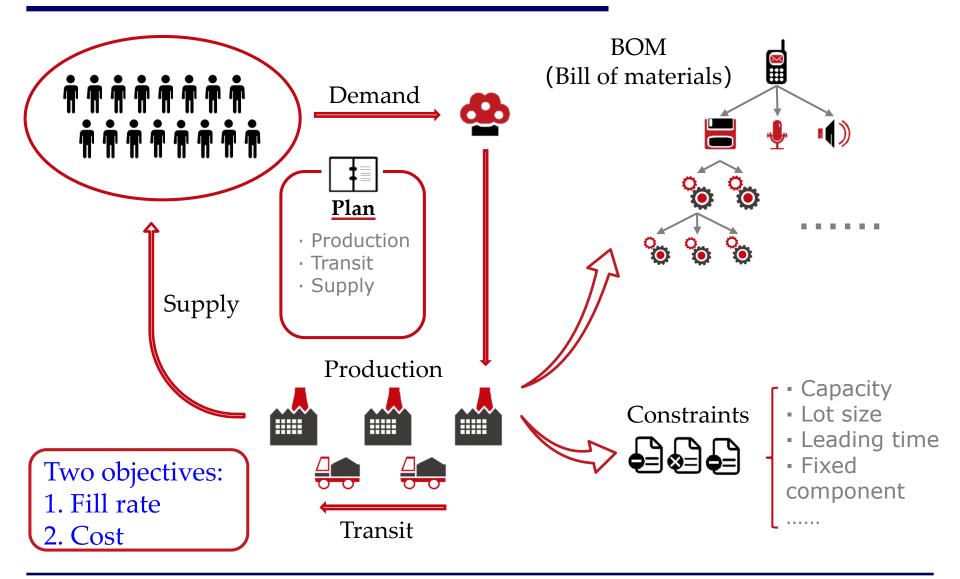


Example of multi-objective optimization



- Accuracy: the higher the better
- Complexity: the smaller the better

Example of multi-objective optimization



Multi-objective evolutionary algorithms

- EAs for multi-objective optimization are usually called Multi-Objective Evolutionary Algorithms (MOEAs)
- Almost all types of EAs have their multi-objective version
- Become a prosperous sub-area of EAs since 1985

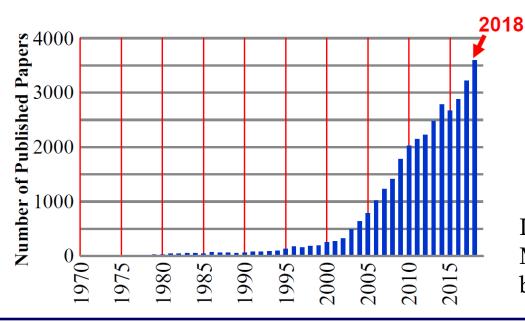


Image source: "Evolutionary Many-objective Optimization" by H. Ishibuchi

Variants of MOEA

• Pareto dominance based: NSGA-II, SPEA-II, ...



K. Deb, A. Pratap, S. Agarwal and T. Meyarivan. A fast and elitist multiobjective genetic algorithm: NSGA-II. *IEEE Transactions on Evolutionary Computation*, 2002. (Google scholar引用: 33727)

Performance indicator based: SMS-EMOA, HyPE,



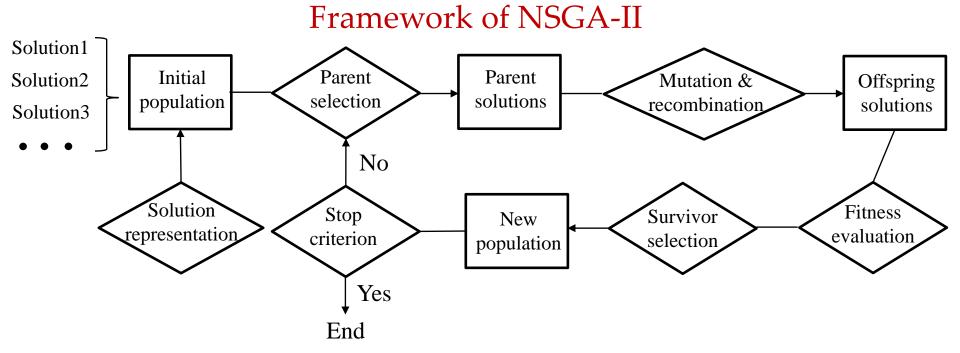
N. Beume, B. Naujoks and M. Emmerich. SMS-EMOA: Multiobjective selection based on dominated hypervolume. *European Journal of Operational Research*, 2007. (Google scholar引用: 1422)

Decomposition based: MOEA/D,

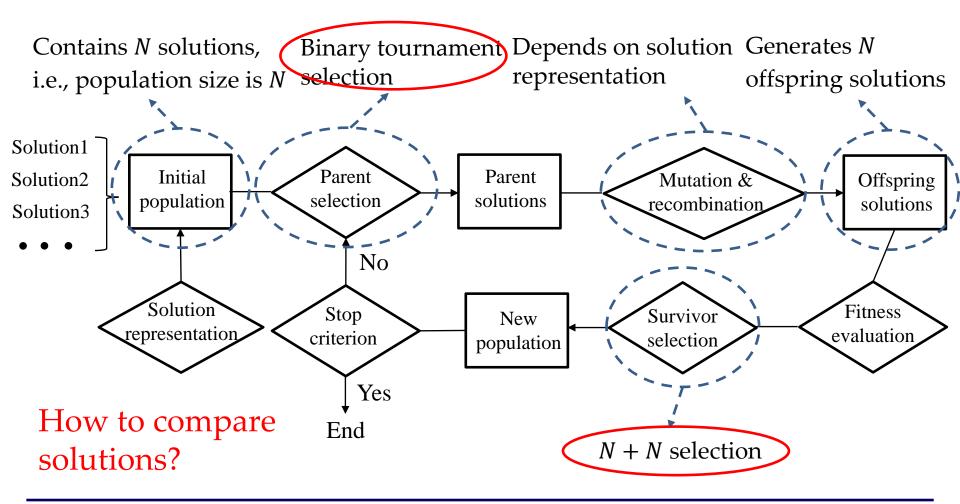


Q. Zhang and H. Li. MOEA/D: A multiobjective evolutionary algorithm based on decomposition. *IEEE Transactions on Evolutionary Computation*, 2007. (Google scholar引用: 4891)

- NSGA-II: probably the most influential work on MOEAs
- Majority of papers on MOEAs emerge after this seminal work, and adopt similar framework as NSGA-II

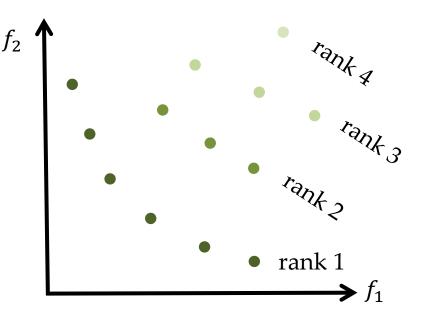


Framework of NSGA-II



Non-dominated sorting

```
Input: P = \{x_1, x_2, ..., x_u\};
Initialize k = 1, Q = \emptyset
                          many redundant
While P \neq \emptyset Do
                          comparisons
   for each x_i \in P
      if x_i is not dominated by any x_i in P
         \operatorname{ran}k(x_i) = k;
         Q = Q \cup \{x_i\}
      end if
   end for
   P = P/Q;
   k = k + 1
End While
```

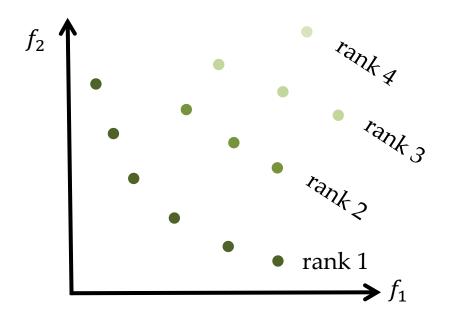


Bi-objective minimization

end for

i = 1;Fast non-dominated sorting while $F_i \neq \emptyset$ store the solutions for each $x \in P$ _____ the set of solutions $Q = \emptyset$; with the next rank $(S_x) = \emptyset; (n_x) = 0;$ dominated by x for each $x \in F_i$ for each $y \in P$ the number of solutions As x is for each $y \in S_x$ excluded now, dominating *x* if x > y then $n_y = n_y - 1$ decrease n_y $S_x = S_x \cup \{y\}$ if x dominates y, add y to S_x if $n_{\nu} = 0$ then else if x < y then rank(y) = i + 1; $n_x = n_x + 1$ if y dominates x, increase n_x y has the $Q = Q \cup \{y\}$ end if next rank end if end for end for if $n_x = 0$ then x is ranked by 1 end for $rank(x)=1; F_1 = F_1 \cup \{x\}$ $i = i + 1; F_i = 0$ end if

end while

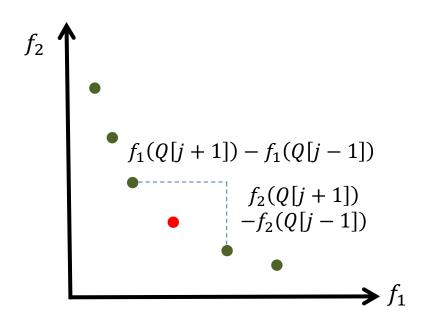


Bi-objective minimization

For the solutions with the same rank, which one is better?

Crowding distance assignment

```
Input: Q = \{x_1, x_2, ..., x_l\} with the same rank; for each i, set Q[i]_{distance} = 0 for each objective f_i the i-th solution in Q Q = sort(Q, f_i); in ascending order Q[1]_{distance} = \infty; boundary solutions Q[l]_{distance} = \infty; for j = 2 to l - 1
```



 $Q[j]_{distance} = Q[j]_{distance} + \underbrace{f_i(Q[j+1]) - f_i(Q[j-1])}_{f_i.max - f_i.min} \rightarrow \text{normalization}$ end for

end for

Crowding distance: the larger the better

Prefer diversity

Crowded comparison employed by NSGA-II

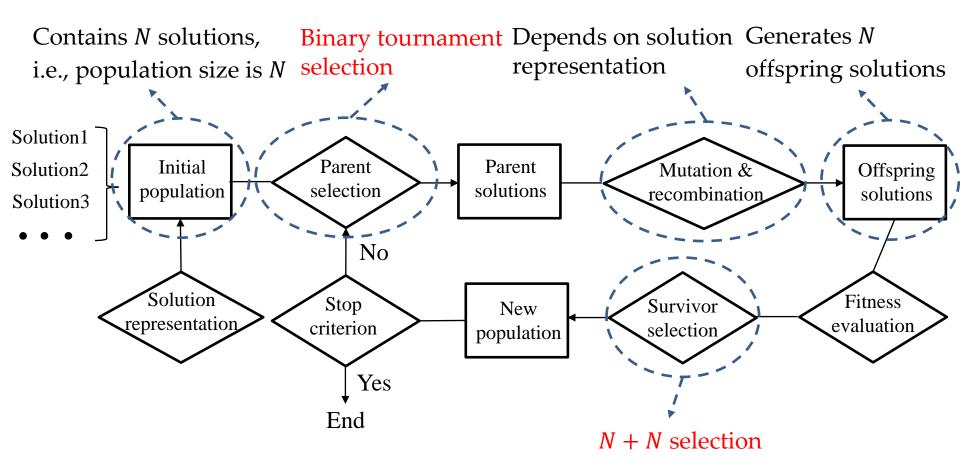
Given a set P of solutions, for any two solutions x, y in P, x is better than y, if

- $\operatorname{rank}(x) < \operatorname{rank}(y)$
- or rank(x) = rank(y) but distance(x) > distance(y)

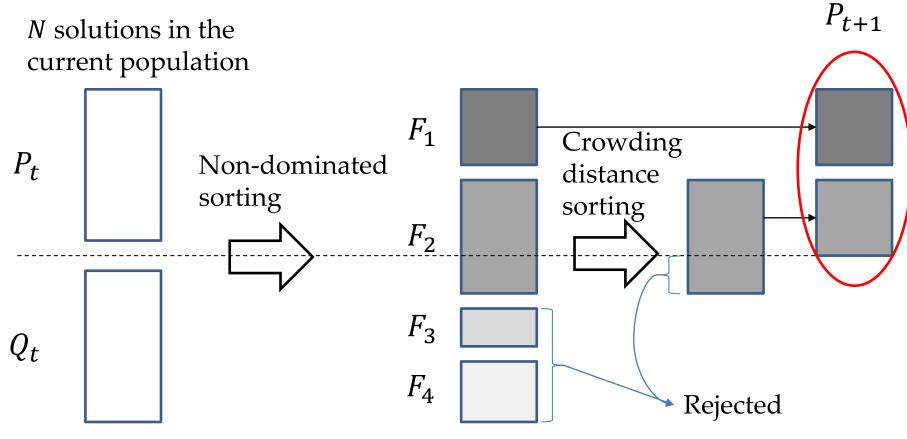
Convergence

Diversity

Framework of NSGA-II



N + N survivor selection



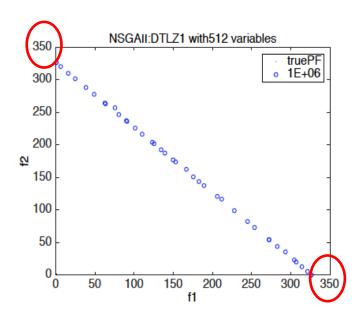
NSGA-II: population size 40, SBX crossover with $\eta = 20$, crossover probability 0.9, polynomial mutation with $\eta = 20$, mutation probability 1/n

DTLZ1:

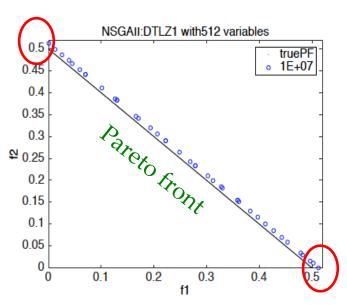
Minimize
$$f_1(\mathbf{x}) = \frac{1}{2}x_1x_2 \cdots x_{M-1}(1+g(\mathbf{x}_M)),$$

Minimize $f_2(\mathbf{x}) = \frac{1}{2}x_1x_2 \cdots (1-x_{M-1})(1+g(\mathbf{x}_M)),$
 \vdots :
Minimize $f_{M-1}(\mathbf{x}) = \frac{1}{2}x_1(1-x_2)(1+g(\mathbf{x}_M)),$
Minimize $f_M(\mathbf{x}) = \frac{1}{2}(1-x_1)(1+g(\mathbf{x}_M)),$
subject to $0 \le x_i \le 1$, for $i = 1, 2, \dots, n$. the vector containing the last $n - M + 1$ variables $g(\mathbf{x}_M) = 100\left[|\mathbf{x}_M| + \sum_{x_i \in \mathbf{X}_M} (x_i - 0.5)^2 - \cos(20\pi(x_i - 0.5))\right]$
 $n - M + 1$

For NSGA-II solving DTLZ1 with M = 2 and n = 512



The population after 10⁶ fitness evaluations



The population after 10⁷ fitness evaluations

NSGA-II: population size 40, SBX crossover with $\eta = 20$, crossover probability 0.9, polynomial mutation with $\eta = 20$, mutation probability 1/n

DTLZ3:

```
Min. f_1(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \cos(x_{M-1} \pi/2),

Min. f_2(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \sin(x_{M-1} \pi/2),

Min. f_3(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \sin(x_{M-2} \pi/2),

\vdots \vdots

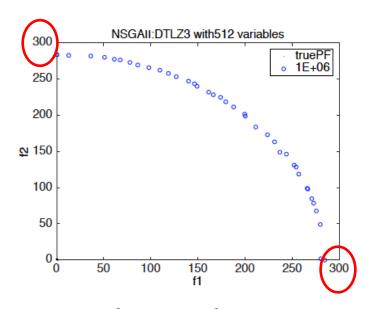
Min. f_M(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \sin(x_1 \pi/2),

with g(\mathbf{x}_M) = 100 \left[ |\mathbf{x}_M| + \sum_{x_i \in \mathbf{X}_M} (x_i - 0.5)^2 - \cos(20\pi(x_i - 0.5)) \right],

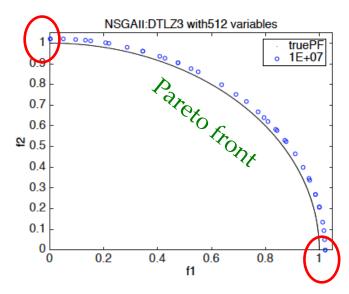
0 \le x_i \le 1, \quad \text{for } i = 1, 2, \dots, n.
```

the vector containing the last n - M + 1 variables

For NSGA-II solving DTLZ3 with M = 2 and n = 512



The population after 10⁶ fitness evaluations

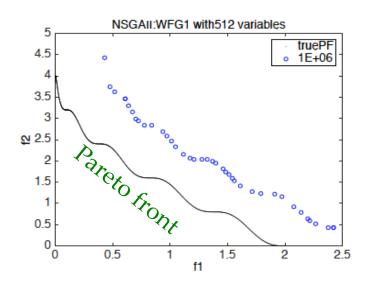


The population after 10⁷ fitness evaluations

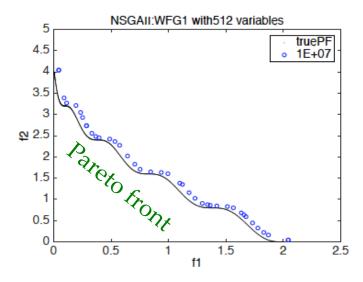
NSGA-II: population size 40, SBX crossover with $\eta = 20$, crossover probability 0.9, polynomial mutation with $\eta = 20$, mutation probability 1/n

```
WFG: to be optimized Given  \mathbf{z} = \{z_1, \dots, z_k, z_{k+1}, \dots, z_n\}  Minimise  f_{m=1:M}(\mathbf{x}) = x_M + S_m h_m(x_1, \dots, x_{M-1})  where  \mathbf{x} = \{x_1, \dots, x_M\} = \{\max(t_M^p, A_1)(t_1^p - 0.5) + 0.5, \dots, \\ \max(t_M^p, A_{M-1})(t_{M-1}^p - 0.5) + 0.5, t_M^p\}   \mathbf{t}^p = \{t_1^p, \dots, t_M^p\} \leftarrow [\mathbf{t}^{p-1} \leftarrow [\dots \leftarrow [\mathbf{t}^1 \leftarrow [\mathbf{z}_{[0,1]}] \\ \mathbf{z}_{[0,1]} = \{z_{1,[0,1]}, \dots, z_{n,[0,1]}\} = \{z_1/z_{1,\max}, \dots, z_n/z_{n,\max}\}
```

For NSGA-II solving WFG1 with M = 2 and n = 512



The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations



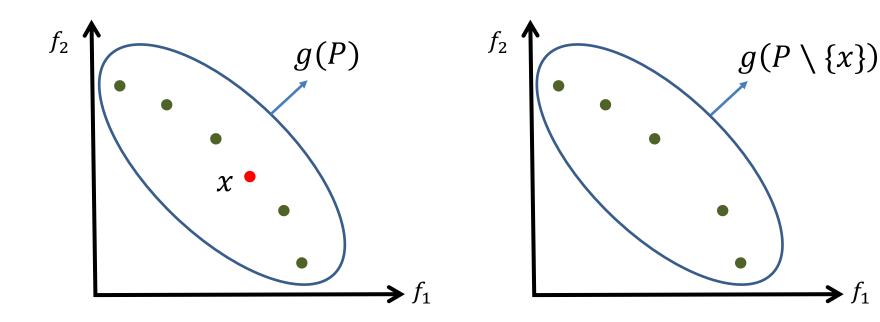
The population

 Similar to NSGA-II, except the goodness measure for the solutions with the same rank

Make use of quality indicators to measure the goodness

 Typically, the goodness of a solution is defined based on how much the quality indicator decreases if the solution is removed

Quality indicator: g(P), where P is a set of solutions

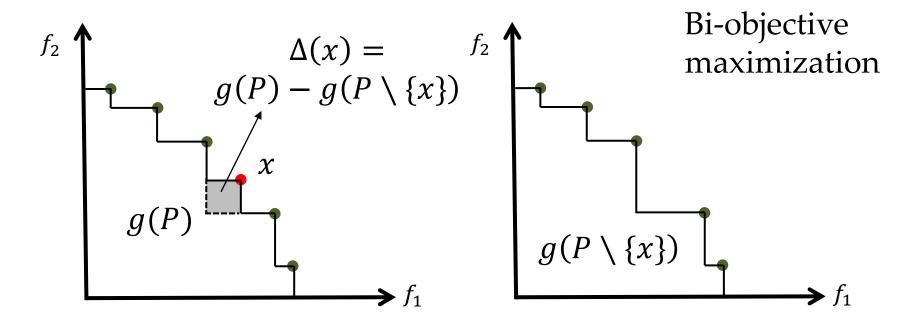


$$\Delta(x) = g(P) - g(P \setminus \{x\})$$

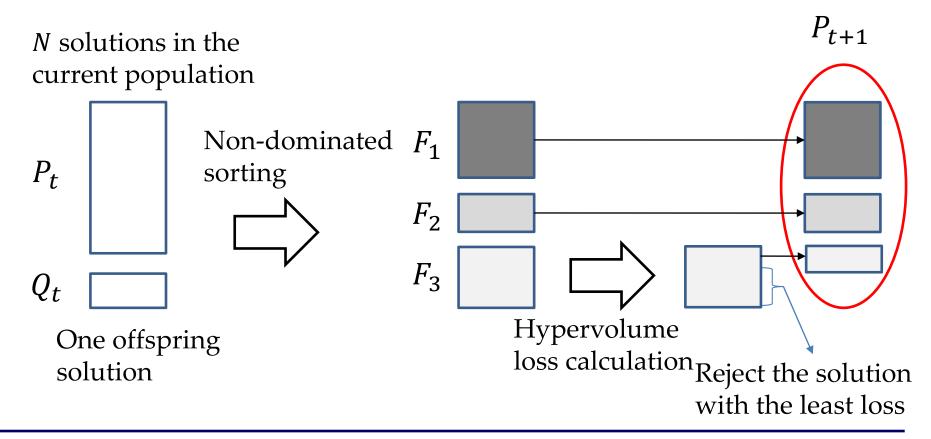
Quality indicator loss: the larger the better

The quality indicator g(P) should be coherent with "convergence" and "diversity"

E.g., the hypervolume indicator



The basic SMS-EMOA generates only one offspring solution



SMS-EMOA: application illustration

SMS-EMOA: population size 40, SBX crossover with $\eta = 20$, crossover probability 0.9, polynomial mutation with $\eta = 20$, mutation probability 1/n

DTLZ1:

Minimize $f_1(\mathbf{x}) = \frac{1}{2}x_1x_2\cdots x_{M-1}(1+g(\mathbf{x}_M)),$ Minimize $f_2(\mathbf{x}) = \frac{1}{2}x_1x_2\cdots (1-x_{M-1})(1+g(\mathbf{x}_M)),$ \vdots : Minimize $f_{M-1}(\mathbf{x}) = \frac{1}{2}x_1(1-x_2)(1+g(\mathbf{x}_M)),$ Minimize $f_M(\mathbf{x}) = \frac{1}{2}(1-x_1)(1+g(\mathbf{x}_M)),$ subject to $0 \le x_i \le 1$, for i = 1, 2, ..., n.

DTLZ3:

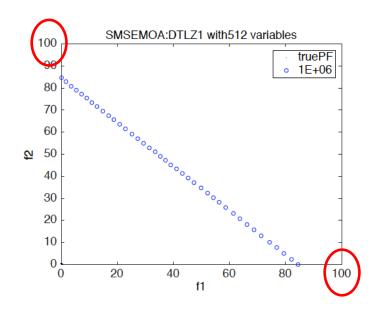
```
\begin{aligned} & \text{Min. } f_1(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \cos(x_{M-1} \pi/2), \\ & \text{Min. } f_2(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \sin(x_{M-1} \pi/2), \\ & \text{Min. } f_3(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \sin(x_{M-2} \pi/2), \\ & \vdots & \vdots \\ & \text{Min. } f_M(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \sin(x_1 \pi/2), \\ & \text{with } g(\mathbf{x}_M) = 100 \left[ |\mathbf{x}_M| + \sum_{x_i \in \mathbf{X}_M} (x_i - 0.5)^2 - \cos(20\pi(x_i - 0.5)) \right], \\ & 0 \leq x_i \leq 1, \quad \text{for } i = 1, 2, \dots, n. \end{aligned}
```

```
WFG:
```

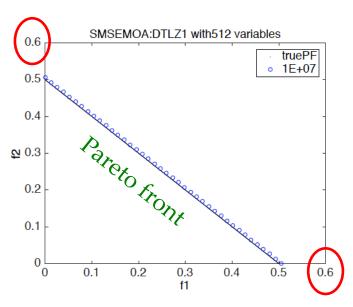
```
Given \mathbf{z} = \{z_1, \dots, z_k, z_{k+1}, \dots, z_n\}
Minimise f_{m=1:M}(\mathbf{x}) = x_M + S_m h_m(x_1, \dots, x_{M-1})
where \mathbf{x} = \{x_1, \dots, x_M\} = \{\max(t_M^p, A_1)(t_1^p - 0.5) + 0.5, \dots, \\ \max(t_M^p, A_{M-1})(t_{M-1}^p - 0.5) + 0.5, t_M^p\}
\mathbf{t}^p = \{t_1^p, \dots, t_M^p\} \leftarrow [\mathbf{t}^{p-1} \leftarrow [\dots \leftarrow [\mathbf{t}^1 \leftarrow [\mathbf{z}_{[0,1]}] \\ \mathbf{z}_{[0,1]} = \{z_{1,[0,1]}, \dots, z_{p,[0,1]}\} = \{z_{1}/z_{1,\max}, \dots, z_{n}/z_{p,\max}\}
```

SMS-EMOA: application illustration

For SMS-EMOA solving DTLZ1 with M = 2 and n = 512

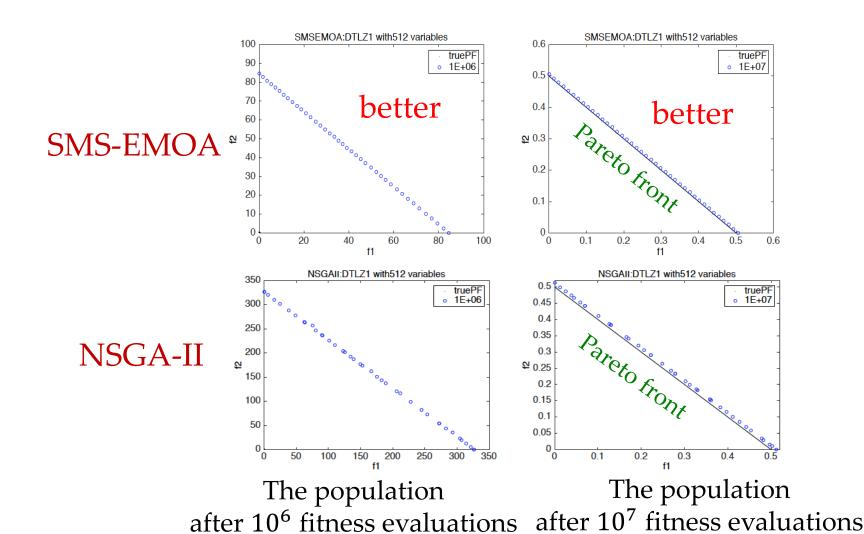


The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations



The population

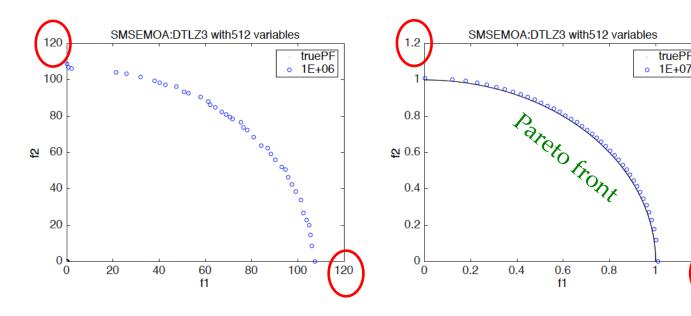
SMS-EMOA vs. NSGA-II



http://www.lamda.nju.edu.cn/qianc/

SMS-EMOA: application illustration

For SMS-EMOA solving DTLZ3 with M = 2 and n = 512



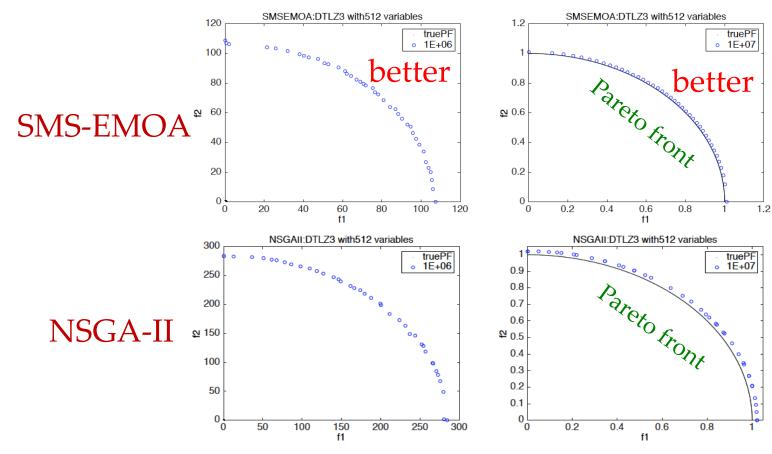
The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations

The population

truePF

1.2

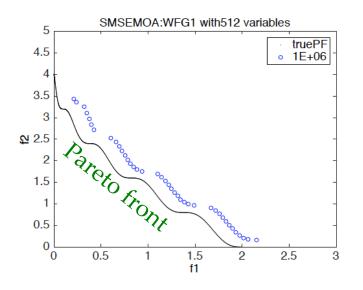
SMS-EMOA vs. NSGA-II



The population The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations

SMS-EMOA: application illustration

For SMS-EMOA solving WFG1 with M = 2 and n = 512



4.5 1E+07 3.5 № 2.5 0.5 1.5 0.5 2.5 3

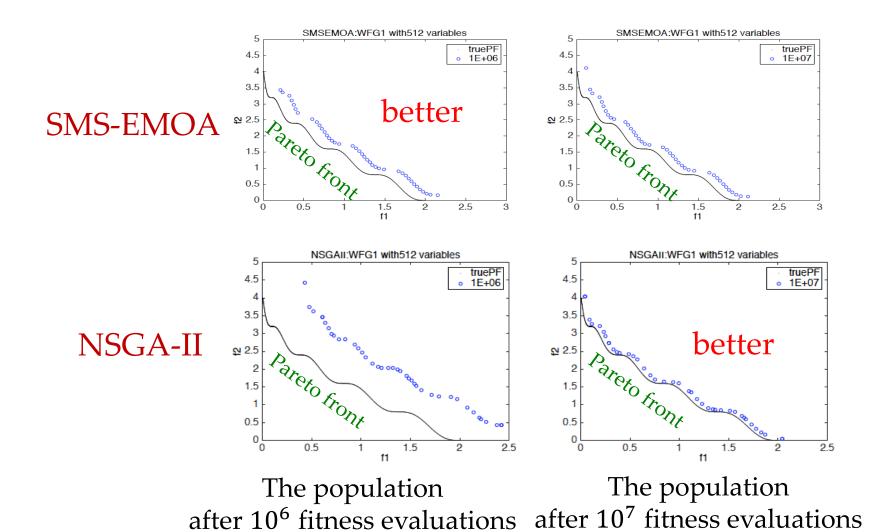
SMSEMOA:WFG1 with512 variables

The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations

The population

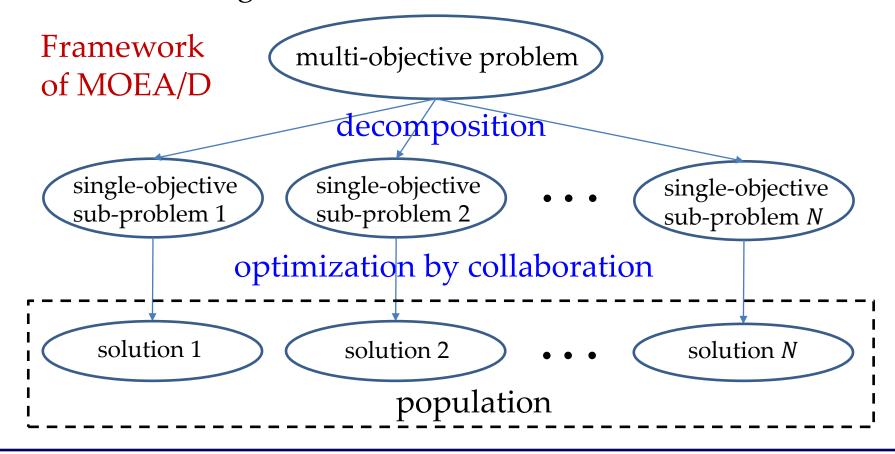
truePF

SMS-EMOA vs. NSGA-II



MOEA/D

 MOEA based on Decomposition (MOEA/D): old things become new again



MOEA/D - decomposition

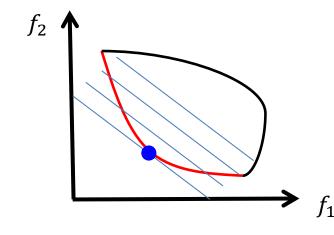
Weighted sum approach

$$\min_{x \in \mathcal{X}} \left(f_1(x), f_2(x) \right)$$

$$Q^{WS}(x \mid \lambda) = \lambda \cdot f_1(x) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left($$

$$min_{x \in \mathcal{X}} \ g^{ws}(x \mid \lambda) = \lambda_1 f_1(x) + \lambda_2 f_2(x)$$

where $\lambda_1 + \lambda_2 = 1$, λ_1 , $\lambda_2 \ge 0$



An optimal solution for $g^{ws}(x \mid \lambda)$ must be Pareto optimal

MOEA/D - decomposition

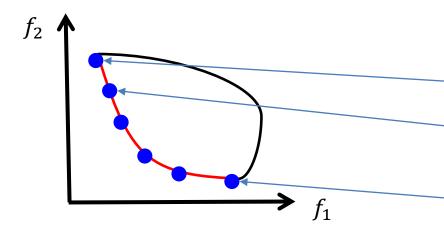
Weighted sum approach

$$min_{x \in \mathcal{X}} \left(f_1(x), f_2(x) \right)$$



$$min_{x \in \mathcal{X}} g^{ws}(x \mid \lambda) = \lambda_1 f_1(x) + \lambda_2 f_2(x)$$

where
$$\lambda_1 + \lambda_2 = 1$$
, λ_1 , $\lambda_2 \ge 0$



N single-objective sub-problems

$$g^{ws}(x \mid \lambda)$$
 with $\lambda_1 = 1$, $\lambda_2 = 0$

$$g^{ws}(x \mid \lambda)$$
 with $\lambda_1 = \frac{N-2}{N-1}$, $\lambda_2 = \frac{1}{N-1}$

$$g^{ws}(x \mid \lambda)$$
 with $\lambda_1 = 0$, $\lambda_2 = 1$

MOEA/D - decomposition

Tchbycheff approach

$$min_{x \in \mathcal{X}} (f_1(x), f_2(x))$$

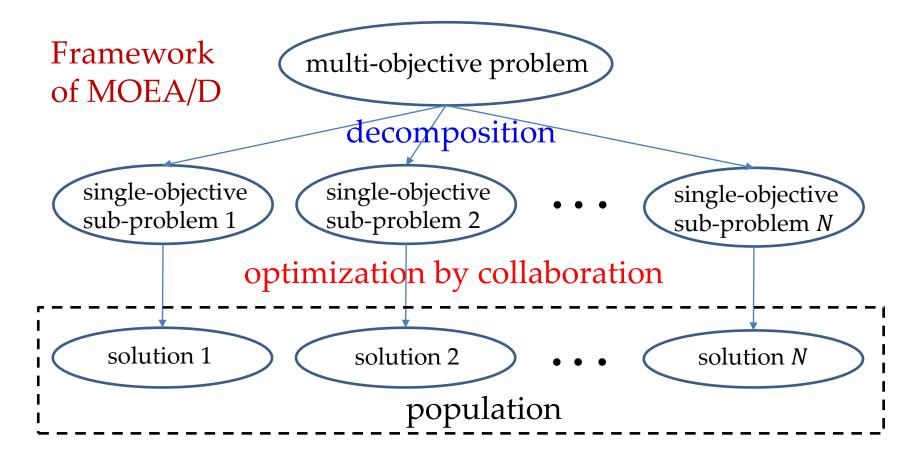
$$min_{x \in \mathcal{X}} \ g^t(x \mid \lambda, \mathbf{z}^*) = \max\{\lambda_1 | f_1(x) - z_1^* |, \ \lambda_2 | f_2(x) - z_2^* | \}$$

where $\lambda_1 + \lambda_2 = 1, \ \lambda_1, \lambda_2 \ge 0$

 \mathbf{z}^* is an Utopian point, where $z_1^* < \min\{f_1(x)\}$ and $z_2^* < \min\{f_2(x)\}$

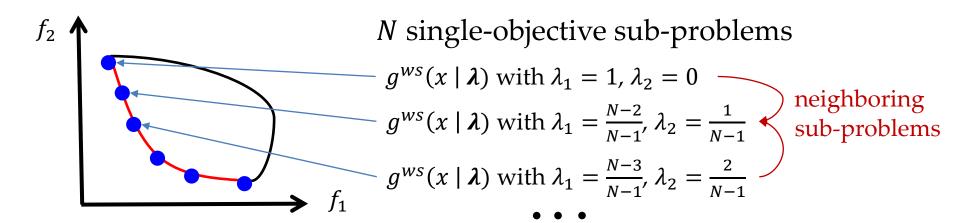
For any Pareto optimal solution x^* , there is a λ such that x^* is optimal to $g^t(x \mid \lambda, z^*)$

MOEA/D - optimization



For each sub-problem, one needs to find neighboring subproblems, e.g., sub-problems with close weight vectors

MOEA/D - optimization



For optimizing each sub-problem in each iteration

- 1. Mating selection: obtain the current solutions of some neighbours
- 2. Reproduction: generate a new solution by applying reproduction operators on its own solution and borrowed solutions
- 3. Replacement:
 - 3.1 replace its old solution by the new one if the new one is better
 - 3.2 pass the new solution on to some of its neighbours, and update its neighbor's solutions when better

MOEA/D: Tchbycheff decomposition approach, population size 40, SBX crossover with $\eta = 20$, crossover probability 0.9, polynomial mutation with $\eta = 20$, mutation probability 1/n

DTLZ1:

Minimize $f_1(\mathbf{x}) = \frac{1}{2}x_1x_2 \cdots x_{M-1}(1 + g(\mathbf{x}_M)),$ Minimize $f_2(\mathbf{x}) = \frac{1}{2}x_1x_2 \cdots (1 - x_{M-1})(1 + g(\mathbf{x}_M)),$ \vdots : Minimize $f_{M-1}(\mathbf{x}) = \frac{1}{2}x_1(1 - x_2)(1 + g(\mathbf{x}_M)),$ Minimize $f_M(\mathbf{x}) = \frac{1}{2}(1 - x_1)(1 + g(\mathbf{x}_M)),$ subject to $0 < x_i < 1$, for i = 1, 2, ..., n.

Given

where

Minimise

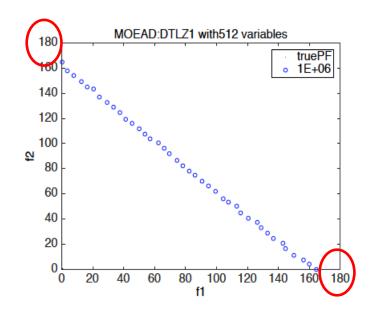
DTLZ3:

```
\begin{aligned} & \text{Min. } f_1(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \cos(x_{M-1} \pi/2), \\ & \text{Min. } f_2(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \cos(x_{M-2} \pi/2) \sin(x_{M-1} \pi/2), \\ & \text{Min. } f_3(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \cos(x_1 \pi/2) \cdots \sin(x_{M-2} \pi/2), \\ & \vdots \\ & \text{Min. } f_M(\mathbf{x}) = (1 + g(\mathbf{x}_M)) \sin(x_1 \pi/2), \\ & \text{with } g(\mathbf{x}_M) = 100 \left[ |\mathbf{x}_M| + \sum_{x_i \in \mathbf{X}_M} (x_i - 0.5)^2 - \cos(20\pi(x_i - 0.5)) \right], \\ & 0 \le x_i \le 1, \quad \text{for } i = 1, 2, \dots, n. \end{aligned}
```

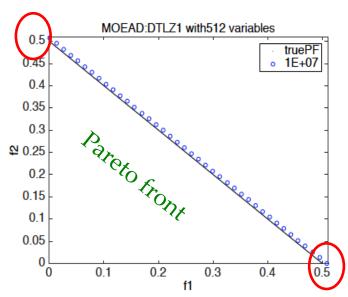
```
WFG:
```

```
\mathbf{z} = \{z_{1}, \dots, z_{k}, z_{k+1}, \dots, z_{n}\}
f_{m=1:M}(\mathbf{x}) = x_{M} + S_{m}h_{m}(x_{1}, \dots, x_{M-1})
\mathbf{x} = \{x_{1}, \dots, x_{M}\} = \{\max(t_{M}^{p}, A_{1})(t_{1}^{p} - 0.5) + 0.5, \dots, \max(t_{M}^{p}, A_{M-1})(t_{M-1}^{p} - 0.5) + 0.5, t_{M}^{p}\}
\mathbf{t}^{p} = \{t_{1}^{p}, \dots, t_{M}^{p}\} \leftarrow [\mathbf{t}^{p-1} \leftarrow [\dots \leftarrow [\mathbf{t}^{1} \leftarrow [\mathbf{z}_{[0,1]}] \\ \mathbf{z}_{[0,1]} = \{z_{1,[0,1]}, \dots, z_{n,[0,1]}\} = \{z_{1}/z_{1,\max}, \dots, z_{n}/z_{n,\max}\}
```

For MOEA/D solving DTLZ1 with M = 2 and n = 512

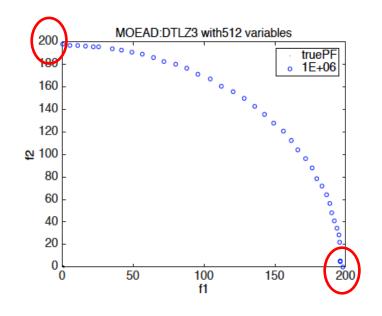


The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations

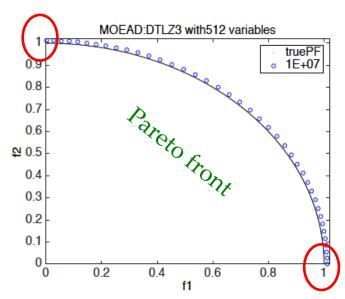


The population

For MOEA/D solving DTLZ3 with M = 2 and n = 512

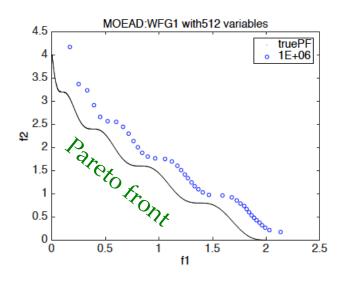


The population after 10⁶ fitness evaluations

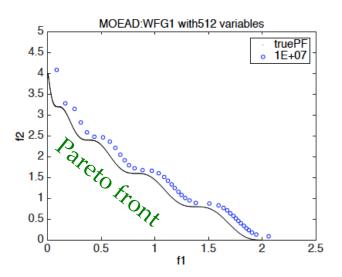


The population after 10⁷ fitness evaluations

For MOEA/D solving WFG1 with M = 2 and n = 512

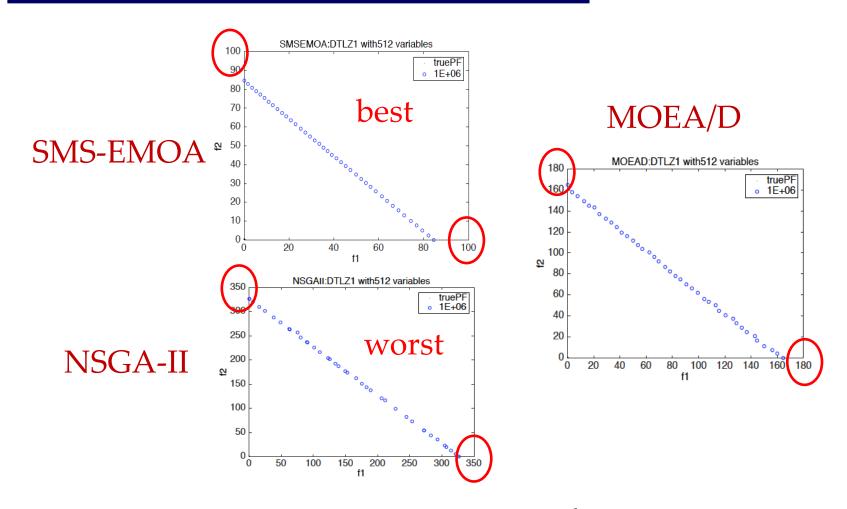


The population after 10⁶ fitness evaluations after 10⁷ fitness evaluations



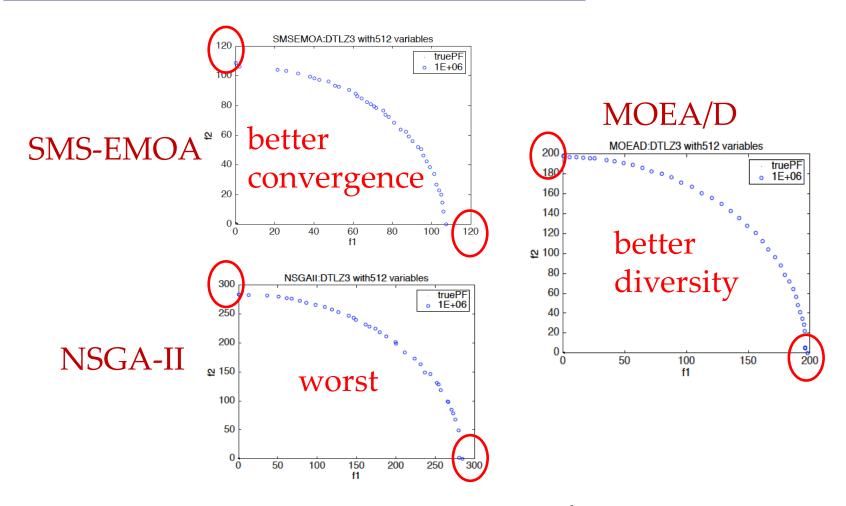
The population

Comparison on DTLZ1



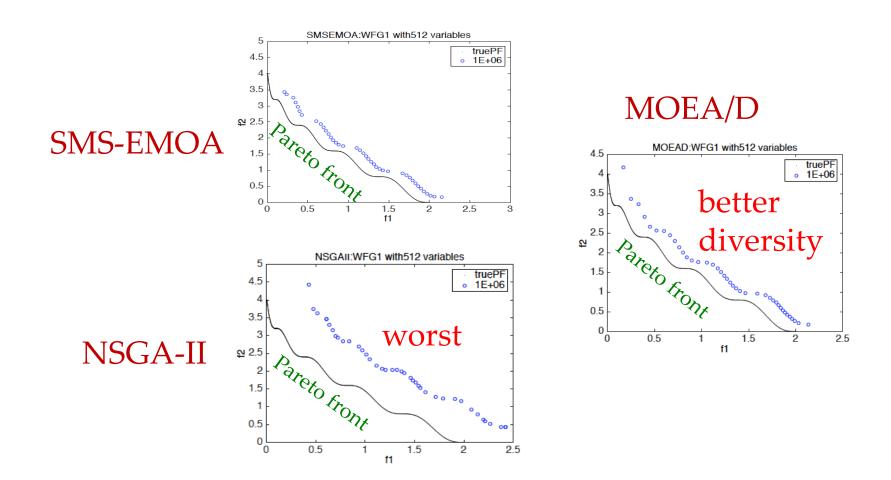
The population after 10⁶ fitness evaluations

Comparison on DTLZ3



The population after 10⁶ fitness evaluations

Comparison on WFG1



The population after 10⁶ fitness evaluations

Summary

Multi-objective optimization

NSGA-II

SMS-EMOA

Popular variants

of MOEA

MOEA/D

References

- A. E. Eiben and J. E. Smith. Introduction to Evolutionary Computing. Chapter 12.
- K. Deb. Multi-objective optimization using evolutionary algorithms. John Wiley & Sons, 2001.
- K. Deb, A. Pratap, S. Agarwal and T. Meyarivan. A fast and elitist multiobjective genetic algorithm: NSGA-II. *IEEE Transactions on Evolutionary Computation*, 2002.
- Q. Zhang and H. Li. MOEA/D: A multiobjective evolutionary algorithm based on decomposition. *IEEE Transactions on Evolutionary Computation*, 2007.
- N. Beume, B. Naujoks and M. Emmerich. SMS-EMOA: Multiobjective selection based on dominated hypervolume. *European Journal of Operational Research*, 2007.

Assignment - 4

Task:

 Apply NSGA-II and MOEA/D to solve the multi-objective weighted Max-Cut problem

Deadline: Jan. 26