

# Lecture 8: Knowledge 2

# Previously...

```
function HYBRID-WUMPUS-AGENT(percept) returns an action
  inputs: percept, a list, [stench,breeze,glitter,bump,scream]
  persistent: KB, a knowledge base, initially the atemporal “wumpus physics”
    t, a counter, initially 0, indicating time
    plan, an action sequence, initially empty

  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  TELL the KB the temporal “physics” sentences for time t
  safe  $\leftarrow \{[x, y] : \text{ASK}(KB, OK_{x,y}^t) = \text{true}\}$ 
  if ASK(KB, Glittert) = true then
    plan  $\leftarrow [\text{Grab}] + \text{PLAN-ROUTE}(\text{current}, \{[1,1]\}, \text{safe}) + [\text{Climb}]$ 
  if plan is empty then
    unvisited  $\leftarrow \{[x, y] : \text{ASK}(KB, L_{x,y}^{t'}) = \text{false} \text{ for all } t' \leq t\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{safe}, \text{safe})$ 
  if plan is empty and ASK(KB, HaveArrowt) = true then
    possible_wumpus  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg W_{x,y}) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-SHOT}(\text{current}, \text{possible\_wumpus}, \text{safe})$ 
  if plan is empty then // no choice but to take a risk
    not_unsafe  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg OK_{x,y}^t) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{not\_unsafe}, \text{safe})$ 
  if plan is empty then
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \{[1, 1]\}, \text{safe}) + [\text{Climb}]$ 
    action  $\leftarrow \text{POP}(\text{plan})$ 
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow t + 1$ 
  return action
```

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```
function PLAN-ROUTE(current,goals,allowed) returns an action sequence
  inputs: current, the agent’s current position
    goals, a set of squares; try to plan a route to one of them
    allowed, a set of squares that can form part of the route

  problem  $\leftarrow \text{ROUTE-PROBLEM}(\text{current}, \text{goals}, \text{allowed})$ 
  return A*-GRAPH-SEARCH(problem)
```

# Pros and cons of propositional logic

- 😊 Propositional logic is **declarative**: pieces of syntax correspond to facts
- 😊 Propositional logic allows partial/disjunctive/negated information (unlike most data structures and databases)
- 😊 Propositional logic is **compositional**: meaning of  $B_{1,1} \wedge P_{1,2}$  is derived from meaning of  $B_{1,1}$  and of  $P_{1,2}$
- 😊 Meaning in propositional logic is **context-independent** (unlike natural language, where meaning depends on context)
- 😢 Propositional logic has very limited expressive power (unlike natural language)  
E.g., cannot say “pits cause breezes in adjacent squares” except by writing one sentence for each square

# First-order logic

Whereas propositional logic assumes world contains **facts**, first-order logic (like natural language) assumes the world contains

- **Objects:** people, houses, numbers, theories, Ronald McDonald, colors, baseball games, wars, centuries . . .
- **Relations:** red, round, bogus, prime, multistoried . . ., brother of, bigger than, inside, part of, has color, occurred after, owns, comes between, . . .
- **Functions:** father of, best friend, third inning of, one more than, end of . . .

# Logics in general

Language	Ontological Commitment	Epistemological Commitment
Propositional logic	facts	true/false/unknown
First-order logic	facts, objects, relations	true/false/unknown
Temporal logic	facts, objects, relations, times	true/false/unknown
Probability theory	facts	degree of belief
Fuzzy logic	facts + degree of truth	known interval value

# Syntax of FOL: Basic elements

Constants	<i>KingJohn, 2, UCB, ...</i>
Predicates	<i>Brother, &gt;, ...</i>
Functions	<i>Sqrt, LeftLegOf, ...</i>
Variables	<i>x, y, a, b, ...</i>
Connectives	$\wedge \vee \neg \Rightarrow \Leftrightarrow$
Equality	$=$
Quantifiers	$\forall \exists$

# Atomic sentences

Atomic sentence = *predicate*( $term_1, \dots, term_n$ )  
or  $term_1 = term_2$

Term = *function*( $term_1, \dots, term_n$ )  
or *constant* or *variable*

E.g., *Brother(KingJohn, RichardTheLionheart)*  
*> (Length(LeftLegOf(Richard)), Length(LeftLegOf(KingJohn)))*

# Complex sentences

Complex sentences are made from atomic sentences using connectives

$\neg S, \quad S_1 \wedge S_2, \quad S_1 \vee S_2, \quad S_1 \Rightarrow S_2, \quad S_1 \Leftrightarrow S_2$

E.g.  $Sibling(KingJohn, Richard) \Rightarrow Sibling(Richard, KingJohn)$

$>(1, 2) \vee \leq(1, 2)$

$>(1, 2) \wedge \neg>(1, 2)$

# Truth in first-order logic

Sentences are true with respect to a **model** and an **interpretation**

Model contains  $\geq 1$  objects (**domain elements**) and relations among them

Interpretation specifies referents for

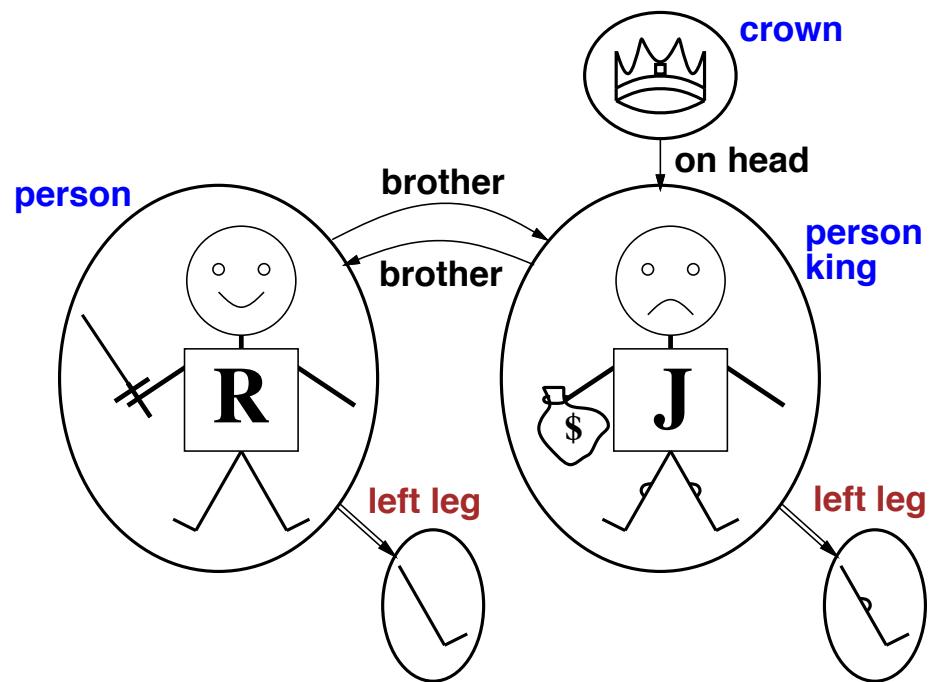
constant symbols  $\rightarrow$  objects

predicate symbols  $\rightarrow$  relations

function symbols  $\rightarrow$  functional relations

An atomic sentence  $\textit{predicate}(\textit{term}_1, \dots, \textit{term}_n)$  is true  
iff the **objects** referred to by  $\textit{term}_1, \dots, \textit{term}_n$   
are in the **relation** referred to by  $\textit{predicate}$

# Models for FOL: Example



Consider the interpretation in which  
*Richard* → Richard the Lionheart  
*John* → the evil King John  
*Brother* → the brotherhood relation

Under this interpretation, *Brother(Richard, John)* is true just in case Richard the Lionheart and the evil King John are in the brotherhood relation in the model

# Models for FOL: Lots!

Entailment in propositional logic can be computed by enumerating models

We **can** enumerate the FOL models for a given KB vocabulary:

For each number of domain elements  $n$  from 1 to  $\infty$

    For each  $k$ -ary predicate  $P_k$  in the vocabulary

        For each possible  $k$ -ary relation on  $n$  objects

            For each constant symbol  $C$  in the vocabulary

                For each choice of referent for  $C$  from  $n$  objects . . .

Computing entailment by enumerating FOL models is not easy!

# Universal quantification

$\forall \langle \text{variables} \rangle \ \langle \text{sentence} \rangle$

Everyone at Berkeley is smart:

$\forall x \ At(x, \text{Berkeley}) \Rightarrow \text{Smart}(x)$

$\forall x \ P$  is true in a model  $m$  iff  $P$  is true with  $x$  being each possible object in the model

Roughly speaking, equivalent to the conjunction of instantiations of  $P$

$$\begin{aligned} & (At(\text{KingJohn}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{KingJohn})) \\ \wedge \ & (At(\text{Richard}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{Richard})) \\ \wedge \ & (At(\text{Berkeley}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{Berkeley})) \\ \wedge \ & \dots \end{aligned}$$

# A common mistake to avoid

Typically,  $\Rightarrow$  is the main connective with  $\forall$

Common mistake: using  $\wedge$  as the main connective with  $\forall$ :

$$\forall x \ At(x, Berkeley) \wedge Smart(x)$$

means “Everyone is at Berkeley and everyone is smart”

# Existential quantification

$\exists \langle \text{variables} \rangle \ \langle \text{sentence} \rangle$

Someone at Stanford is smart:

$\exists x \ At(x, Stanford) \wedge Smart(x)$

$\exists x \ P$  is true in a model  $m$  iff  $P$  is true with  $x$  being **some** possible object in the model

**Roughly** speaking, equivalent to the disjunction of instantiations of  $P$

$(At(KingJohn, Stanford) \wedge Smart(KingJohn))$   
 $\vee (At(Richard, Stanford) \wedge Smart(Richard))$   
 $\vee (At(Stanford, Stanford) \wedge Smart(Stanford))$   
 $\vee \dots$

# Another common mistake to avoid

Typically,  $\wedge$  is the main connective with  $\exists$

Common mistake: using  $\Rightarrow$  as the main connective with  $\exists$ :

$$\exists x \ At(x, Stanford) \Rightarrow Smart(x)$$

is true if there is anyone who is not at Stanford!

# Properties of quantifiers

$\forall x \ \forall y$  is the same as  $\forall y \ \forall x$  (why??)

$\exists x \ \exists y$  is the same as  $\exists y \ \exists x$  (why??)

$\exists x \ \forall y$  is **not** the same as  $\forall y \ \exists x$

$\exists x \ \forall y \ Loves(x, y)$

“There is a person who loves everyone in the world”

$\forall y \ \exists x \ Loves(x, y)$

“Everyone in the world is loved by at least one person”

**Quantifier duality:** each can be expressed using the other

$\forall x \ Likes(x, IceCream)$        $\neg \exists x \ \neg Likes(x, IceCream)$

$\exists x \ Likes(x, Broccoli)$        $\neg \forall x \ \neg Likes(x, Broccoli)$

# Fun with sentences

Brothers are siblings

$$\forall x, y \ Brother(x, y) \Rightarrow Sibling(x, y).$$

“Sibling” is symmetric

$$\forall x, y \ Sibling(x, y) \Leftrightarrow Sibling(y, x).$$

One's mother is one's female parent

$$\forall x, y \ Mother(x, y) \Leftrightarrow (Female(x) \wedge Parent(x, y)).$$

A first cousin is a child of a parent's sibling

$$\forall x, y \ FirstCousin(x, y) \Leftrightarrow \exists p, ps \ Parent(p, x) \wedge Sibling(ps, p) \wedge Parent(ps, y)$$

# Equality

$term_1 = term_2$  is true under a given interpretation  
if and only if  $term_1$  and  $term_2$  refer to the same object

E.g.,  $1 = 2$  and  $\forall x \ \exists (Sqrt(x), Sqrt(x)) = x$  are satisfiable  
 $2 = 2$  is valid

E.g., definition of (full) *Sibling* in terms of *Parent*:

$$\forall x, y \ Sibling(x, y) \Leftrightarrow [\neg(x = y) \wedge \exists m, f \ \neg(m = f) \wedge \\ Parent(m, x) \wedge Parent(f, x) \wedge Parent(m, y) \wedge Parent(f, y)]$$

# Interacting with FOL KBs

Suppose a wumpus-world agent is using an FOL KB and perceives a smell and a breeze (but no glitter) at  $t = 5$ :

$\text{Tell}(KB, \text{Percept}([\text{Smell}, \text{Breeze}, \text{None}], 5))$   
 $\text{Ask}(KB, \exists a \ \text{Action}(a, 5))$

I.e., does  $KB$  entail any particular actions at  $t = 5$ ?

Answer: *Yes*,  $\{a/\text{Shoot}\}$      $\leftarrow$  **substitution** (binding list)

Given a sentence  $S$  and a substitution  $\sigma$ ,

$S\sigma$  denotes the result of plugging  $\sigma$  into  $S$ ; e.g.,

$S = \text{Smarter}(x, y)$

$\sigma = \{x/\text{Hillary}, y/\text{Bill}\}$

$S\sigma = \text{Smarter}(\text{Hillary}, \text{Bill})$

$\text{Ask}(KB, S)$  returns some/all  $\sigma$  such that  $KB \models S\sigma$

# Knowledge base for the wumpus world

## “Perception”

$\forall b, g, t \ Percept([Smell, b, g], t) \Rightarrow Smelt(t)$

$\forall s, b, t \ Percept([s, b, Glitter], t) \Rightarrow AtGold(t)$

**Reflex:**  $\forall t \ AtGold(t) \Rightarrow Action(Grab, t)$

**Reflex with internal state:** do we have the gold already?

$\forall t \ AtGold(t) \wedge \neg Holding(Gold, t) \Rightarrow Action(Grab, t)$

$Holding(Gold, t)$  cannot be observed

$\Rightarrow$  keeping track of change is essential

# Deducing hidden properties

Properties of locations:

$$\forall x, t \ At(\text{Agent}, x, t) \wedge \text{Smelt}(t) \Rightarrow \text{Smelly}(x)$$

$$\forall x, t \ At(\text{Agent}, x, t) \wedge \text{Breeze}(t) \Rightarrow \text{Breezy}(x)$$

Squares are breezy near a pit:

Diagnostic rule—infer cause from effect

$$\forall y \ \text{Breezy}(y) \Rightarrow \exists x \ \text{Pit}(x) \wedge \text{Adjacent}(x, y)$$

Causal rule—infer effect from cause

$$\forall x, y \ \text{Pit}(x) \wedge \text{Adjacent}(x, y) \Rightarrow \text{Breezy}(y)$$

Neither of these is complete—e.g., the causal rule doesn't say whether squares far away from pits can be breezy

Definition for the *Breezy* predicate:

$$\forall y \ \text{Breezy}(y) \Leftrightarrow [\exists x \ \text{Pit}(x) \wedge \text{Adjacent}(x, y)]$$

# Keeping track of change

Facts hold in situations, rather than eternally

E.g., *Holding(Gold, Now)* rather than just *Holding(Gold)*

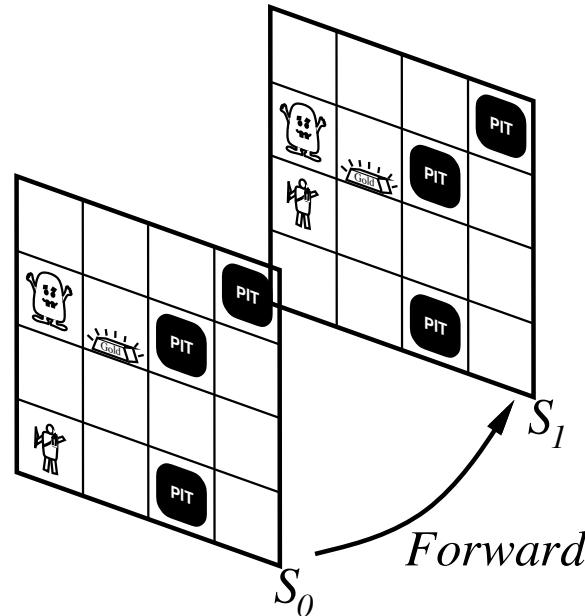
Situation calculus is one way to represent change in FOL:

Adds a situation argument to each non-eternal predicate

E.g., *Now* in *Holding(Gold, Now)* denotes a situation

Situations are connected by the *Result* function

*Result(a, s)* is the situation that results from doing *a* in *s*



# Describing actions I

“Effect” axiom—describe changes due to action

$$\forall s \ AtGold(s) \Rightarrow Holding(Gold, Result(Grab, s))$$

“Frame” axiom—describe **non-changes** due to action

$$\forall s \ HaveArrow(s) \Rightarrow HaveArrow(Result(Grab, s))$$

Frame problem: find an elegant way to handle non-change

- (a) representation—avoid frame axioms
- (b) inference—avoid repeated “copy-overs” to keep track of state

Qualification problem: true descriptions of real actions require endless caveats—  
what if gold is slippery or nailed down or . . .

Ramification problem: real actions have many secondary consequences—  
what about the dust on the gold, wear and tear on gloves, . . .

# Describing actions II

Successor-state axioms solve the representational frame problem

Each axiom is “about” a **predicate** (not an action per se):

$P$  true afterwards  $\Leftrightarrow$  [an action made  $P$  true  
 $\vee$   $P$  true already and no action made  $P$  false]

For holding the gold:

$$\begin{aligned} \forall a, s \ Holding(Gold, Result(a, s)) \Leftrightarrow \\ [(a = Grab \wedge AtGold(s)) \\ \vee (Holding(Gold, s) \wedge a \neq Release)] \end{aligned}$$

# Making plans

Initial condition in KB:

$$\begin{aligned}At(Agent, [1, 1], S_0) \\At(Gold, [1, 2], S_0)\end{aligned}$$

Query:  $Ask(KB, \exists s \ Holding(Gold, s))$

i.e., in what situation will I be holding the gold?

Answer:  $\{s / Result(Grab, Result(Forward, S_0))\}$

i.e., go forward and then grab the gold

This assumes that the agent is interested in plans starting at  $S_0$  and that  $S_0$  is the only situation described in the KB

# Making plans: A better way

Represent **plans** as action sequences  $[a_1, a_2, \dots, a_n]$

$\text{PlanResult}(p, s)$  is the result of executing  $p$  in  $s$

Then the query  $\text{Ask}(KB, \exists p \text{ Holding(Gold, PlanResult}(p, S_0)))$   
has the solution  $\{p/[Forward, Grab]\}$

Definition of  $\text{PlanResult}$  in terms of  $\text{Result}$ :

$$\forall s \text{ } \text{PlanResult}([], s) = s$$

$$\forall a, p, s \text{ } \text{PlanResult}([a|p], s) = \text{PlanResult}(p, \text{Result}(a, s))$$

Planning systems are special-purpose reasoners designed to do this type of inference more efficiently than a general-purpose reasoner

First-order logic:

- objects and relations are semantic primitives
- syntax: constants, functions, predicates, equality, quantifiers

Increased expressive power: sufficient to define wumpus world

Situation calculus:

- conventions for describing actions and change in FOL
- can formulate planning as inference on a situation calculus KB

# A brief history of reasoning

450B.C.	Stoics	propositional logic, inference (maybe)
322B.C.	Aristotle	“syllogisms” (inference rules), quantifiers
1565	Cardano	probability theory (propositional logic + uncertainty)
1847	Boole	propositional logic (again)
1879	Frege	first-order logic
1922	Wittgenstein	proof by truth tables
1930	Gödel	$\exists$ complete algorithm for FOL
1930	Herbrand	complete algorithm for FOL (reduce to propositional)
1931	Gödel	$\neg\exists$ complete algorithm for arithmetic
1960	Davis/Putnam	“practical” algorithm for propositional logic
1965	Robinson	“practical” algorithm for FOL—resolution

# Universal instantiation (UI)

Every instantiation of a universally quantified sentence is entailed by it:

$$\frac{\forall v \ \alpha}{\text{SUBST}(\{v/g\}, \alpha)}$$

for any variable  $v$  and ground term  $g$

E.g.,  $\forall x \ King(x) \wedge Greedy(x) \Rightarrow Evil(x)$  yields

$$King(John) \wedge Greedy(John) \Rightarrow Evil(John)$$

$$King(Richard) \wedge Greedy(Richard) \Rightarrow Evil(Richard)$$

$$King(Father(John)) \wedge Greedy(Father(John)) \Rightarrow Evil(Father(John))$$

# Existential instantiation (EI)

For any sentence  $\alpha$ , variable  $v$ , and constant symbol  $k$   
that does not appear elsewhere in the knowledge base:

$$\frac{\exists v \ \alpha}{\text{SUBST}(\{v/k\}, \alpha)}$$

E.g.,  $\exists x \ Crown(x) \wedge OnHead(x, John)$  yields

$$Crown(C_1) \wedge OnHead(C_1, John)$$

provided  $C_1$  is a new constant symbol, called a **Skolem constant**

Another example: from  $\exists x \ d(x^y)/dy = x^y$  we obtain

$$d(e^y)/dy = e^y$$

provided  $e$  is a new constant symbol

UI can be applied several times to **add** new sentences;  
the new KB is logically equivalent to the old

EI can be applied once to **replace** the existential sentence;  
the new KB is **not** equivalent to the old,  
but is satisfiable iff the old KB was satisfiable

# Reduction to propositional inference

Suppose the KB contains just the following:

$$\begin{aligned} \forall x \ King(x) \wedge Greedy(x) &\Rightarrow Evil(x) \\ King(John) \\ Greedy(John) \\ Brother(Richard, John) \end{aligned}$$

Instantiating the universal sentence in **all possible** ways, we have

$$\begin{aligned} King(John) \wedge Greedy(John) &\Rightarrow Evil(John) \\ King(Richard) \wedge Greedy(Richard) &\Rightarrow Evil(Richard) \\ King(John) \\ Greedy(John) \\ Brother(Richard, John) \end{aligned}$$

The new KB is propositionalized: proposition symbols are

$$King(John), Greedy(John), Evil(John), King(Richard) \text{ etc.}$$

# Reduction to propositional inference

Claim: a ground sentence\* is entailed by new KB iff entailed by original KB

Claim: every FOL KB can be propositionalized so as to preserve entailment

Idea: propositionalize KB and query, apply resolution, return result

Problem: with function symbols, there are infinitely many ground terms,  
e.g., *Father(Father(Father(John)))*

Theorem: Herbrand (1930). If a sentence  $\alpha$  is entailed by an FOL KB,  
it is entailed by a **finite** subset of the propositional KB

Idea: For  $n = 0$  to  $\infty$  do  
    create a propositional KB by instantiating with depth- $n$  terms  
    see if  $\alpha$  is entailed by this KB

Problem: works if  $\alpha$  is entailed, loops if  $\alpha$  is not entailed

Theorem: Turing (1936), Church (1936), entailment in FOL is **semidecidable**

# Problems with propositionalization

Propositionalization seems to generate lots of irrelevant sentences.

E.g., from

$\forall x \ King(x) \wedge Greedy(x) \Rightarrow Evil(x)$

$King(John)$

$\forall y \ Greedy(y)$

$Brother(Richard, John)$

it seems obvious that  $Evil(John)$ , but propositionalization produces lots of facts such as  $Greedy(Richard)$  that are irrelevant

With  $p$   $k$ -ary predicates and  $n$  constants, there are  $p \cdot n^k$  instantiations

With function symbols, it gets much much worse!

# Unification

We can get the inference immediately if we can find a substitution  $\theta$  such that  $King(x)$  and  $Greedy(x)$  match  $King(John)$  and  $Greedy(y)$

$\theta = \{x/John, y/John\}$  works

$\text{UNIFY}(\alpha, \beta) = \theta$  if  $\alpha\theta = \beta\theta$

$p$	$q$	$\theta$
$Knows(John, x)$	$Knows(John, Jane)$	$\{x/Jane\}$
$Knows(John, x)$	$Knows(y, OJ)$	$\{x/OJ, y/John\}$
$Knows(John, x)$	$Knows(y, Mother(y))$	$\{y/John, x/Mother(John)\}$
$Knows(John, x)$	$Knows(x, OJ)$	$fail$

Standardizing apart eliminates overlap of variables, e.g.,  $Knows(z_{17}, OJ)$

# Generalized Modus Ponens (GMP)

(前件推理)

$$\frac{p_1', p_2', \dots, p_n', (p_1 \wedge p_2 \wedge \dots \wedge p_n \Rightarrow q)}{q\theta} \quad \text{where } p_i'\theta = p_i\theta \text{ for all } i$$

$p_1'$  is  $King(John)$

$p_1$  is  $King(x)$

$p_2'$  is  $Greedy(y)$

$p_2$  is  $Greedy(x)$

$\theta$  is  $\{x/John, y/John\}$   $q$  is  $Evil(x)$

$q\theta$  is  $Evil(John)$

GMP used with KB of **definite clauses** (**exactly** one positive literal)

All variables assumed universally quantified

# Soundness of GMP

Need to show that

$$p_1', \dots, p_n', (p_1 \wedge \dots \wedge p_n \Rightarrow q) \models q\theta$$

provided that  $p_i'\theta = p_i\theta$  for all  $i$

Lemma: For any definite clause  $p$ , we have  $p \models p\theta$  by UI

1.  $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \models (p_1 \wedge \dots \wedge p_n \Rightarrow q)\theta = (p_1\theta \wedge \dots \wedge p_n\theta \Rightarrow q\theta)$
2.  $p_1', \dots, p_n' \models p_1' \wedge \dots \wedge p_n' \models p_1'\theta \wedge \dots \wedge p_n'\theta$
3. From 1 and 2,  $q\theta$  follows by ordinary Modus Ponens

# Example knowledge base

The law says that it is a crime for an American to sell weapons to hostile nations. The country Nono, an enemy of America, has some missiles, and all of its missiles were sold to it by Colonel West, who is American.

Prove that Col. West is a criminal

... it is a crime for an American to sell weapons to hostile nations:

$\text{American}(x) \wedge \text{Weapon}(y) \wedge \text{Sells}(x, y, z) \wedge \text{Hostile}(z) \Rightarrow \text{Criminal}(x)$

Nono ... has some missiles, i.e.,  $\exists x \text{ Owns}(\text{Nono}, x) \wedge \text{Missile}(x)$ :

$\text{Owns}(\text{Nono}, M_1)$  and  $\text{Missile}(M_1)$

... all of its missiles were sold to it by Colonel West

$\forall x \text{ Missle}(x) \wedge \text{Owns}(\text{Nono}, x) \Rightarrow \text{Sells}(\text{West}, x, \text{Nono})$

Missiles are weapons:

$\text{Missile}(x) \Rightarrow \text{Weapon}(x)$

An enemy of America counts as "hostile":

$\text{Enemy}(x, \text{America}) \Rightarrow \text{Hostile}(x)$

West, who is American ...

$\text{American}(\text{West})$

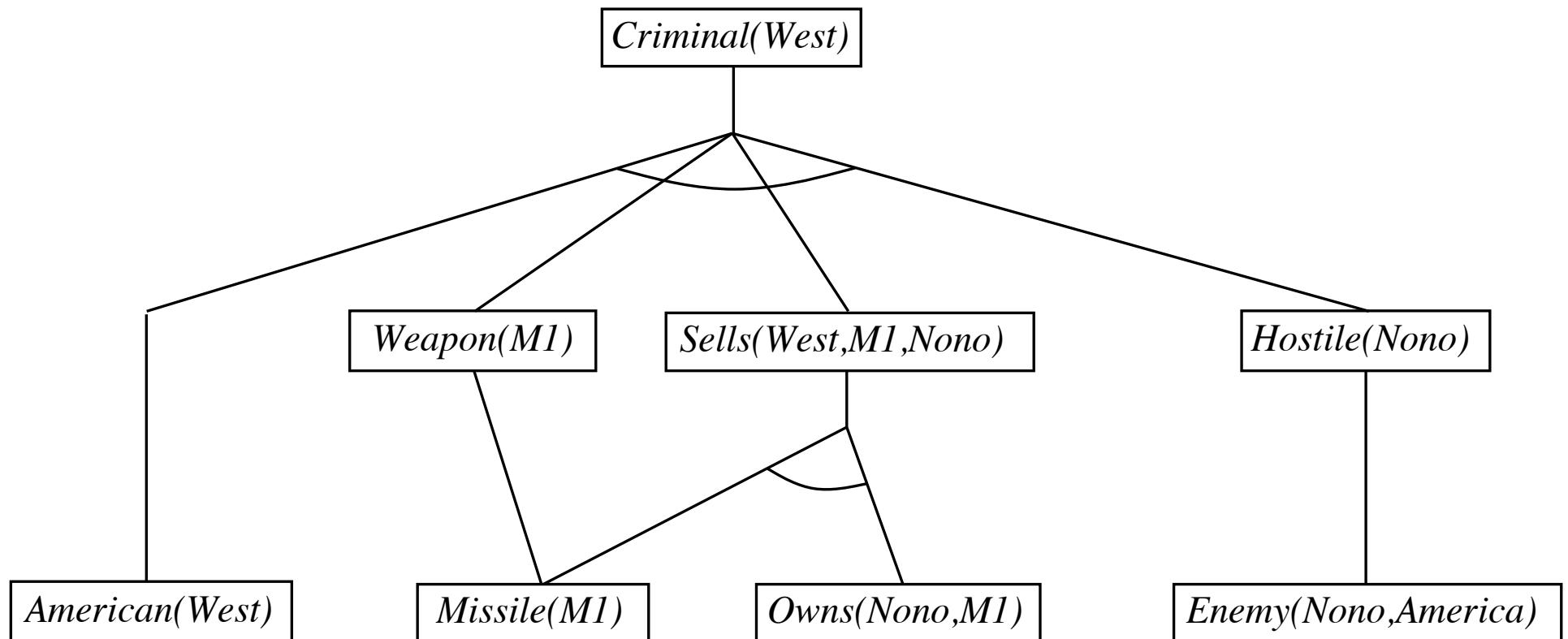
The country Nono, an enemy of America ...

$\text{Enemy}(\text{Nono}, \text{America})$

# Forward chaining algorithm

```
function FOL-FC-ASK( $KB, \alpha$ ) returns a substitution or false
repeat until  $new$  is empty
   $new \leftarrow \{ \}$ 
  for each sentence  $r$  in  $KB$  do
     $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-APART}(r)$ 
    for each  $\theta$  such that  $(p_1 \wedge \dots \wedge p_n)\theta = (p'_1 \wedge \dots \wedge p'_n)\theta$ 
      for some  $p'_1, \dots, p'_n$  in  $KB$ 
         $q' \leftarrow \text{SUBST}(\theta, q)$ 
        if  $q'$  is not a renaming of a sentence already in  $KB$  or  $new$  then do
          add  $q'$  to  $new$ 
           $\phi \leftarrow \text{UNIFY}(q', \alpha)$ 
          if  $\phi$  is not fail then return  $\phi$ 
  add  $new$  to  $KB$ 
return false
```

# Forward chaining proof



# Properties of forward chaining

Sound and complete for first-order definite clauses  
(proof similar to propositional proof)

Datalog = first-order definite clauses + **no functions** (e.g., crime KB)  
FC terminates for Datalog in poly iterations: at most  $p \cdot n^k$  literals

May not terminate in general if  $\alpha$  is not entailed

This is unavoidable: entailment with definite clauses is semidecidable

# Efficiency of forward chaining

Simple observation: no need to match a rule on iteration  $k$  if a premise wasn't added on iteration  $k - 1$

⇒ match each rule whose premise contains a newly added literal

Matching itself can be expensive

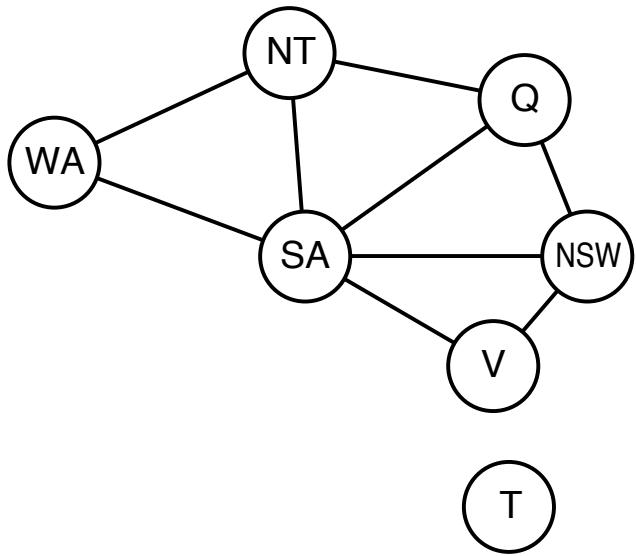
Database indexing allows  $O(1)$  retrieval of known facts

e.g., query  $\text{Missile}(x)$  retrieves  $\text{Missile}(M_1)$

Matching conjunctive premises against known facts is NP-hard

Forward chaining is widely used in deductive databases

# Hard matching example



$$\begin{aligned}
 & \text{Diff}(wa, nt) \wedge \text{Diff}(wa, sa) \wedge \\
 & \text{Diff}(nt, q) \wedge \text{Diff}(nt, sa) \wedge \\
 & \text{Diff}(q, nsw) \wedge \text{Diff}(q, sa) \wedge \\
 & \text{Diff}(nsw, v) \wedge \text{Diff}(nsw, sa) \wedge \\
 & \text{Diff}(v, sa) \Rightarrow \text{Colorable}()
 \end{aligned}$$

$$\begin{aligned}
 & \text{Diff}(Red, Blue) \quad \text{Diff}(Red, Green) \\
 & \text{Diff}(Green, Red) \quad \text{Diff}(Green, Blue) \\
 & \text{Diff}(Blue, Red) \quad \text{Diff}(Blue, Green)
 \end{aligned}$$

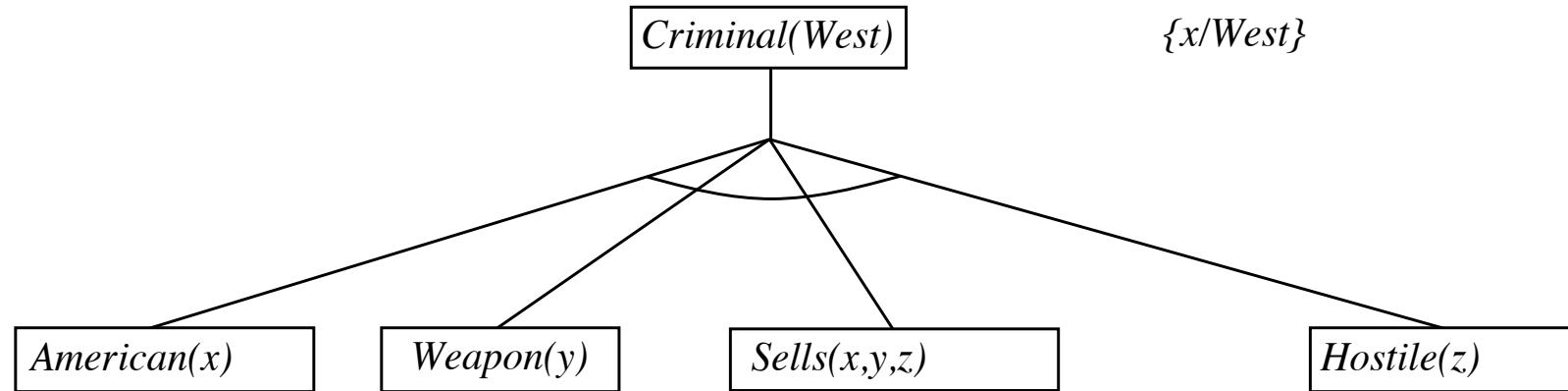
*Colorable()* is inferred iff the CSP has a solution

CSPs include 3SAT as a special case, hence matching is NP-hard

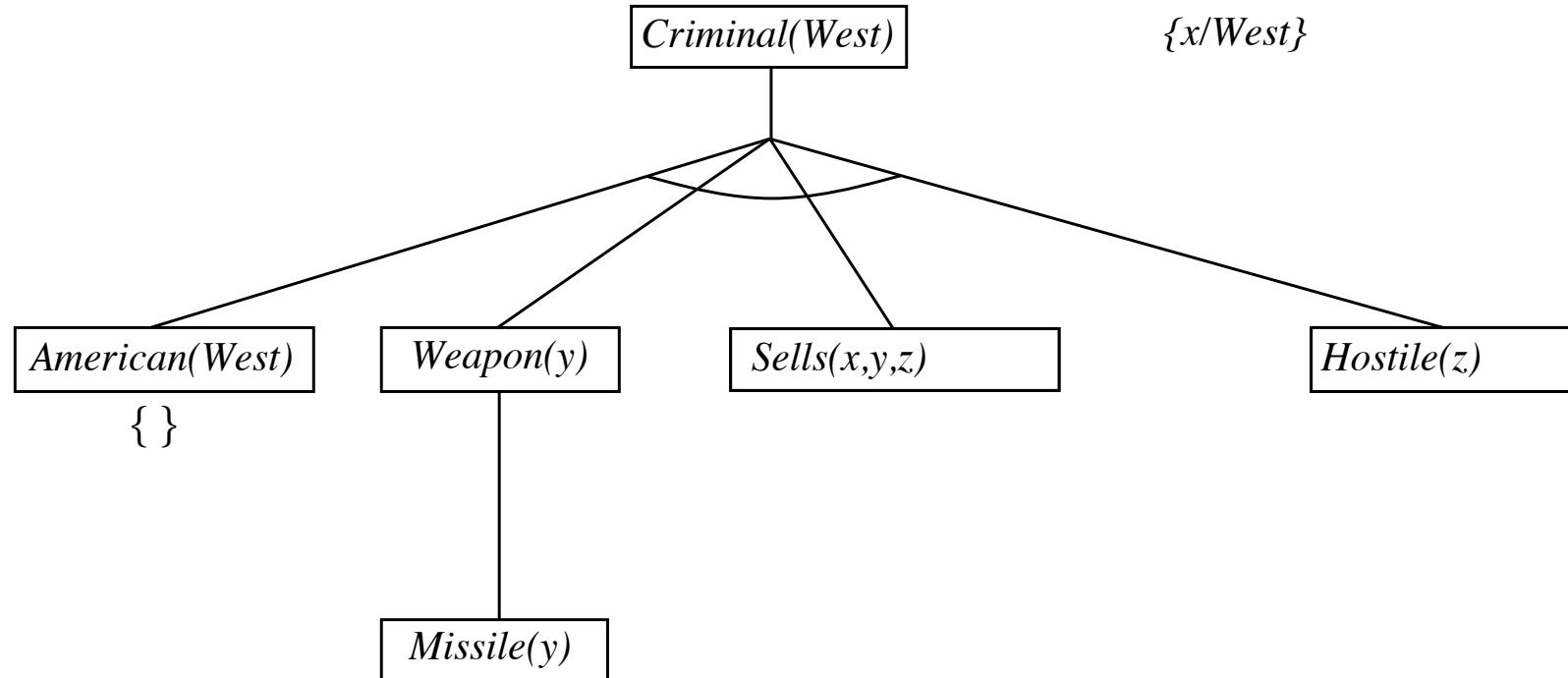
# Backward chaining algorithm

```
function FOL-BC-ASK(KB, goals, θ) returns a set of substitutions
  inputs: KB, a knowledge base
            goals, a list of conjuncts forming a query ( $\theta$  already applied)
             $\theta$ , the current substitution, initially the empty substitution  $\{ \}$ 
  local variables: answers, a set of substitutions, initially empty
  if goals is empty then return  $\{ \theta \}$ 
   $q' \leftarrow \text{SUBST}(\theta, \text{FIRST}(\text{goals}))$ 
  for each sentence r in KB
    where  $\text{STANDARDIZE-APART}(r) = (p_1 \wedge \dots \wedge p_n \Rightarrow q)$ 
    and  $\theta' \leftarrow \text{UNIFY}(q, q')$  succeeds
     $new\_goals \leftarrow [p_1, \dots, p_n | \text{REST}(\text{goals})]$ 
     $answers \leftarrow \text{FOL-BC-ASK}(KB, new\_goals, \text{COMPOSE}(\theta', \theta)) \cup answers$ 
  return answers
```

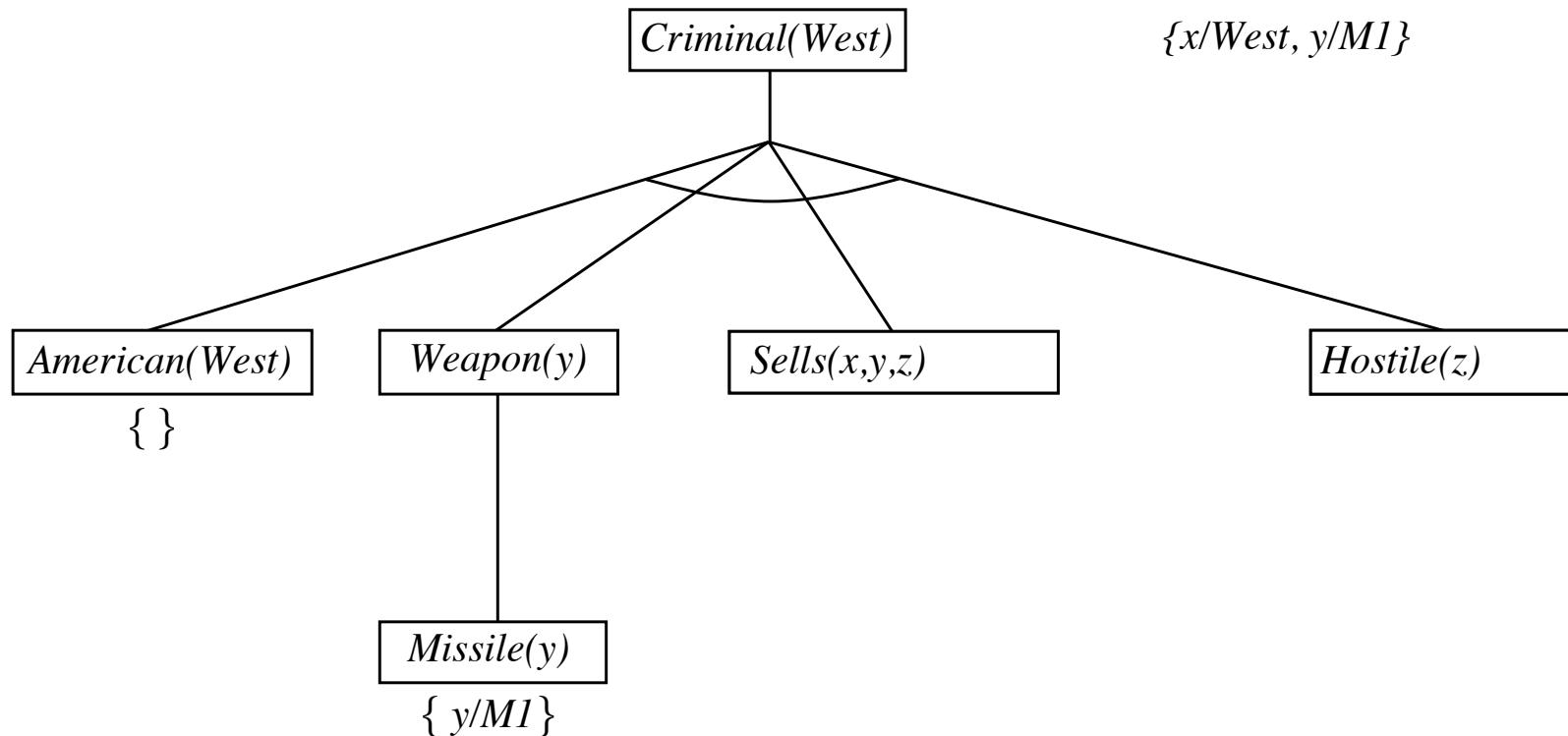
# Backward chaining example



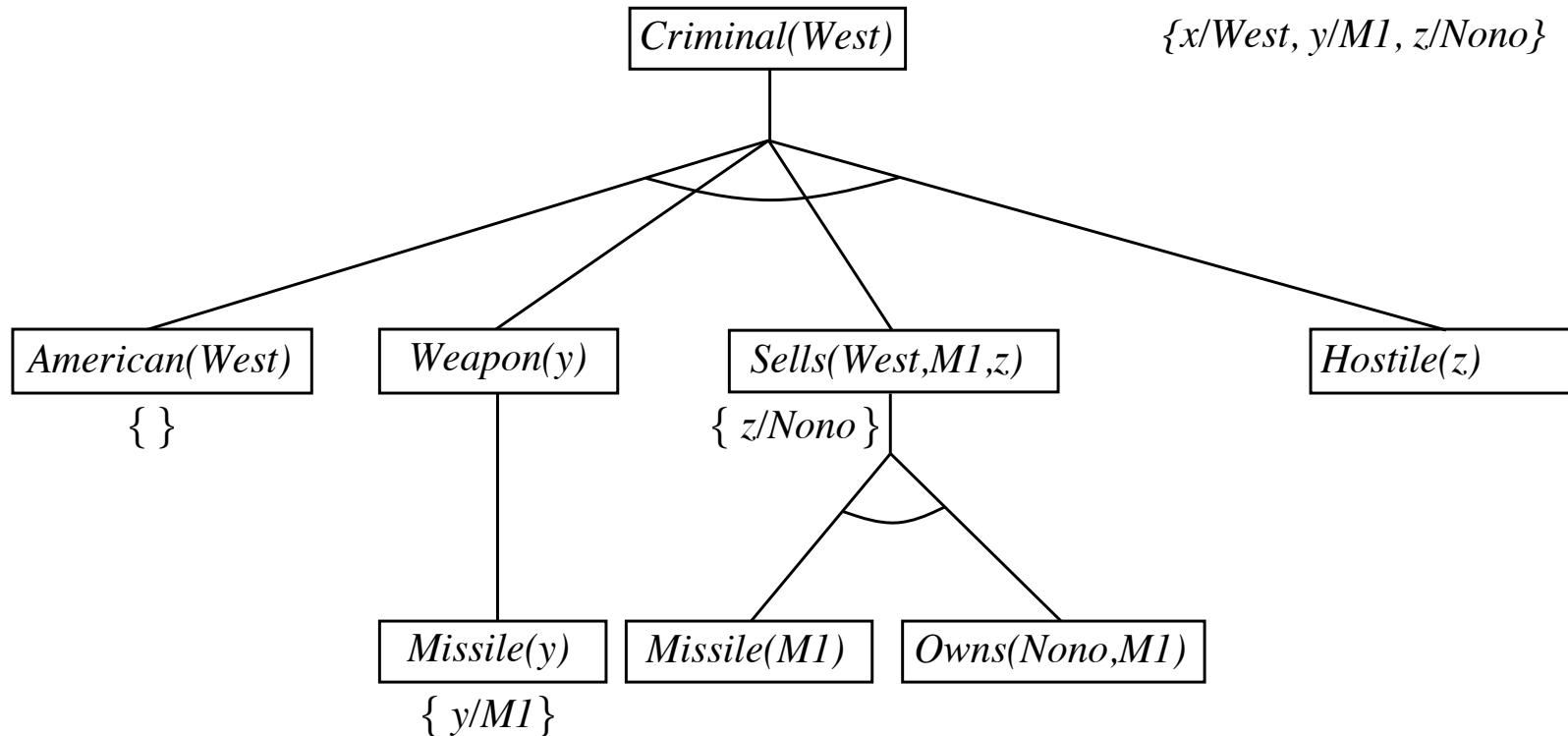
# Backward chaining example



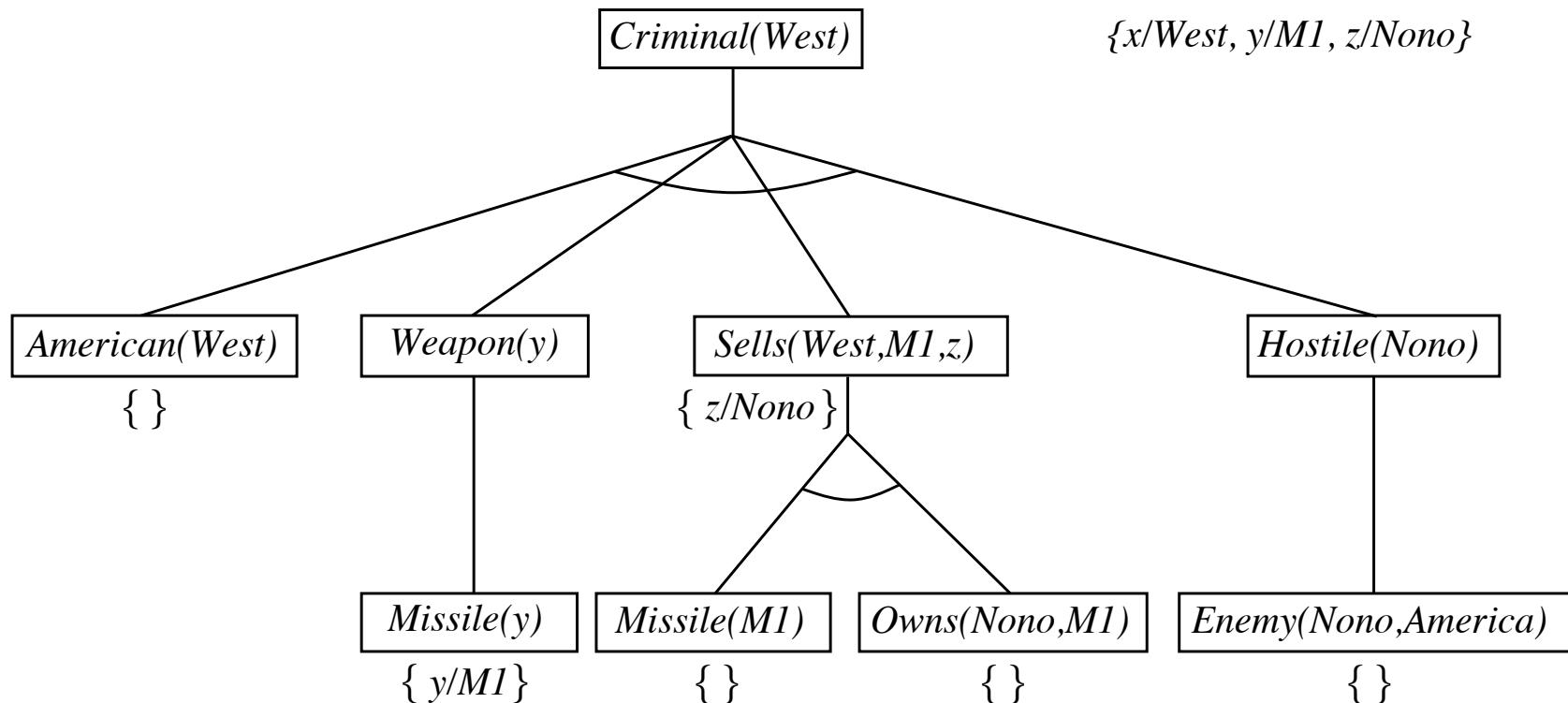
# Backward chaining example



# Backward chaining example



# Backward chaining example



# Properties of backward chaining

Depth-first recursive proof search: space is linear in size of proof

Incomplete due to infinite loops

⇒ fix by checking current goal against every goal on stack

Inefficient due to repeated subgoals (both success and failure)

⇒ fix using caching of previous results (extra space!)

Widely used (without improvements!) for logic programming

# Logic programming

Sound bite: computation as inference on logical KBs

## Logic programming

1. Identify problem
2. Assemble information
3. Tea break
4. Encode information in KB
5. Encode problem instance as facts
6. Ask queries
7. Find false facts

## Ordinary programming

- Identify problem
- Assemble information
- Figure out solution
- Program solution
- Encode problem instance as data
- Apply program to data
- Debug procedural errors

Should be easier to debug  $\text{Capital}(\text{NewYork}, \text{US})$  than  $x := x + 2$  !

# Prolog systems

Basis: backward chaining with Horn clauses + bells & whistles

Widely used in Europe, Japan (basis of 5th Generation project)

Compilation techniques  $\Rightarrow$  approaching a billion LIPS

Program = set of clauses = `head :- literal1, ... literaln.`

```
criminal(X) :- american(X), weapon(Y), sells(X,Y,Z), hostile(Z).
```

Efficient unification by [open coding](#)

Efficient retrieval of matching clauses by direct linking

Depth-first, left-to-right backward chaining

Built-in predicates for arithmetic etc., e.g., `X is Y*Z+3`

Closed-world assumption (“negation as failure”)

e.g., given `alive(X) :- not dead(X).`

`alive(joe)` succeeds if `dead(joe)` fails

# Prolog examples

Depth-first search from a start state X:

```
dfs(X) :- goal(X).  
dfs(X) :- successor(X,S),dfs(S).
```

No need to loop over S: successor succeeds for each

Appending two lists to produce a third:

```
append([],Y,Y).  
append([X|L],Y,[X|Z]) :- append(L,Y,Z).
```

query: append(A,B,[1,2]) ?

answers: A=[] B=[1,2]  
A=[1] B=[2]  
A=[1,2] B=[]

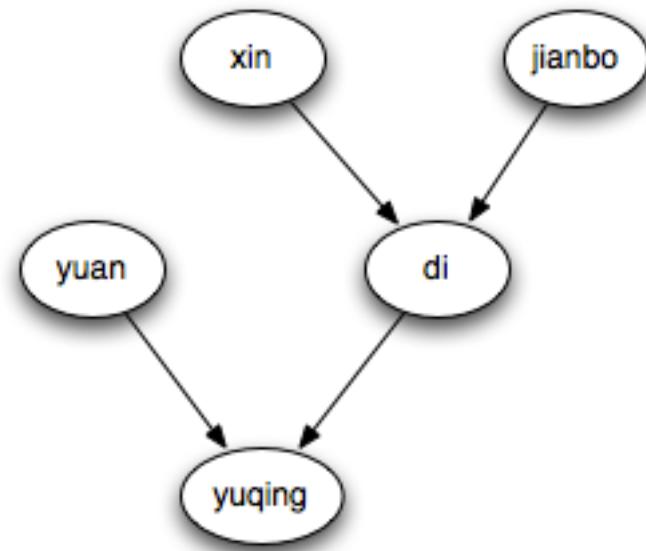
# Prolog example

Let's try

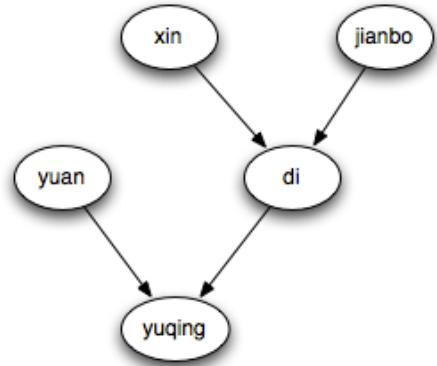
```
member(1,[1,2,3,4,5])
```

query: grandfather(X,yuqing)?

```
male(di).  
male(jianbo).  
female(xin).  
female(yuan).  
female(yuqing).  
father(jianbo,di).  
father(di,yuqing).  
mother(xin,di).  
mother(yuan,yuqing).  
grandfather(X,Y):-father(X,Z),father(Z,Y).  
grandmother(X,Y):-mother(X,Z),father(Z,Y).  
daughter(X,Y):-father(X,Y),female(Y).
```



# Prolog example



```
eyounxRMBP15:AI17 yuy$
```

# Resolution: brief summary

Full first-order version:

$$\frac{\ell_1 \vee \dots \vee \ell_k, \quad m_1 \vee \dots \vee m_n}{(\ell_1 \vee \dots \vee \ell_{i-1} \vee \ell_{i+1} \vee \dots \vee \ell_k \vee m_1 \vee \dots \vee m_{j-1} \vee m_{j+1} \vee \dots \vee m_n)\theta}$$

where  $\text{UNIFY}(\ell_i, \neg m_j) = \theta$ .

For example,

$$\frac{\neg \text{Rich}(x) \vee \text{Unhappy}(x) \quad \text{Rich}(\text{Ken})}{\text{Unhappy}(\text{Ken})}$$

with  $\theta = \{x/\text{Ken}\}$

Apply resolution steps to  $\text{CNF}(KB \wedge \neg \alpha)$ ; complete for FOL

# Conversion to CNF

Everyone who loves all animals is loved by someone:

$$\forall x \ [\forall y \ Animal(y) \Rightarrow Loves(x, y)] \Rightarrow [\exists y \ Loves(y, x)]$$

1. Eliminate biconditionals and implications

$$\forall x \ [\neg\forall y \ \neg Animal(y) \vee Loves(x, y)] \vee [\exists y \ Loves(y, x)]$$

2. Move  $\neg$  inwards:  $\neg\forall x, p \equiv \exists x \ \neg p$ ,  $\neg\exists x, p \equiv \forall x \ \neg p$ :

$$\forall x \ [\exists y \ \neg(\neg Animal(y) \vee Loves(x, y))] \vee [\exists y \ Loves(y, x)]$$

$$\forall x \ [\exists y \ \neg\neg Animal(y) \wedge \neg Loves(x, y)] \vee [\exists y \ Loves(y, x)]$$

$$\forall x \ [\exists y \ Animal(y) \wedge \neg Loves(x, y)] \vee [\exists y \ Loves(y, x)]$$

# Conversion to CNF

3. Standardize variables: each quantifier should use a different one

$$\forall x \ [\exists y \ Animal(y) \wedge \neg Loves(x, y)] \vee [\exists z \ Loves(z, x)]$$

4. Skolemize: a more general form of existential instantiation.

Each existential variable is replaced by a **Skolem function** of the enclosing universally quantified variables:

$$\forall x \ [Animal(F(x)) \wedge \neg Loves(x, F(x))] \vee Loves(G(x), x)$$

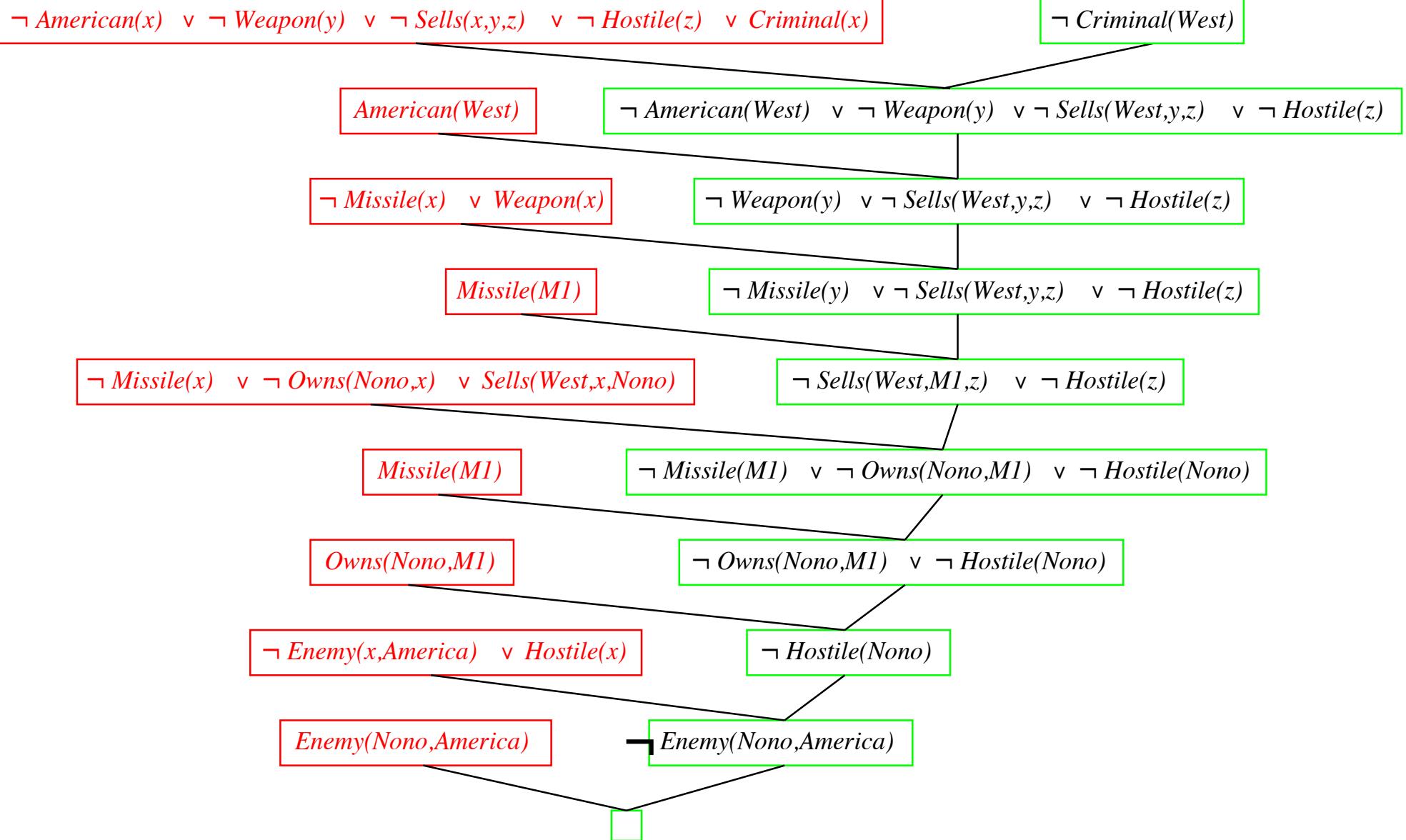
5. Drop universal quantifiers:

$$[Animal(F(x)) \wedge \neg Loves(x, F(x))] \vee Loves(G(x), x)$$

6. Distribute  $\wedge$  over  $\vee$ :

$$[Animal(F(x)) \vee Loves(G(x), x)] \wedge [\neg Loves(x, F(x)) \vee Loves(G(x), x)]$$

# Resolution proof: definite clauses



## Propositional Logic

PL-Forward chaining

PL-Backward chaining

PL-Resolution

## First Order Logic (FOL)

Instantiation

FOL-Forward chaining

FOL-Backward chaining

FOL-Resolution

# Planning

There are many languages description the world  
Planning Domain Definition Language

1.2, 2.1, 2.2, 3.0, 3.1

state s

Action(s)

Result(s,a)

*Action(Fly( $p$ ,  $from$ ,  $to$ ),*

PRECOND:  $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT:  $\neg At(p, from) \wedge At(p, to)$ )

*Action(Fly( $P_1$ ,  $SFO$ ,  $JFK$ ),*

PRECOND:  $At(P_1, SFO) \wedge Plane(P_1) \wedge Airport(SFO) \wedge Airport(JFK)$

EFFECT:  $\neg At(P_1, SFO) \wedge At(P_1, JFK)$ )

# Precondition

action **a** is **applicable** in state **s** if the preconditions are satisfied by **s**

$$(a \in \text{ACTIONS}(s)) \Leftrightarrow s \models \text{PRECOND}(a)$$

$$\forall p, from, to \ (Fly(p, from, to) \in \text{ACTIONS}(s)) \Leftrightarrow \\ s \models (At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to))$$

removing the fluents that appear as negative literals in the action's effects (what we call the **delete list** or  $\text{DEL}(a)$ ), and adding the fluents that are positive literals in the action's effects (what we call the **add list** or  $\text{ADD}(a)$ )

$$\text{RESULT}(s, a) = (s - \text{DEL}(a)) \cup \text{ADD}(a) .$$

*Action*( $\text{Fly}(P_1, SFO, JFK)$ ),

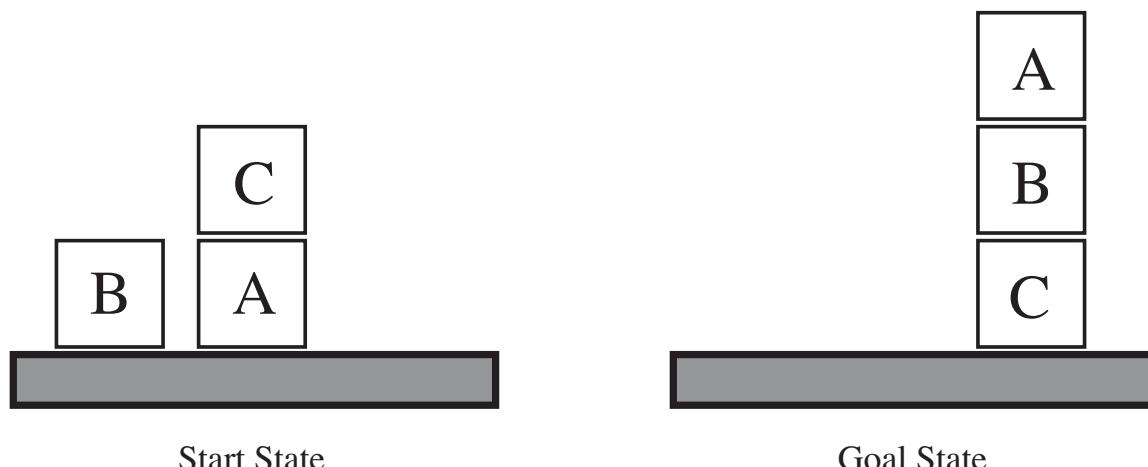
PRECOND:  $\text{At}(P_1, SFO) \wedge \text{Plane}(P_1) \wedge \text{Airport}(SFO) \wedge \text{Airport}(JFK)$

EFFECT:  $\neg \text{At}(P_1, SFO) \wedge \text{At}(P_1, JFK)$ )

# Example

```
Init(On(A, Table) ∧ On(B, Table) ∧ On(C, A)
     ∧ Block(A) ∧ Block(B) ∧ Block(C) ∧ Clear(B) ∧ Clear(C))
Goal(On(A, B) ∧ On(B, C))
Action(Move(b, x, y),
       PRECOND: On(b, x) ∧ Clear(b) ∧ Clear(y) ∧ Block(b) ∧ Block(y) ∧
                  (b≠x) ∧ (b≠y) ∧ (x≠y),
       EFFECT: On(b, y) ∧ Clear(x) ∧ ¬On(b, x) ∧ ¬Clear(y))
Action(MoveToTable(b, x),
       PRECOND: On(b, x) ∧ Clear(b) ∧ Block(b) ∧ (b≠x),
       EFFECT: On(b, Table) ∧ Clear(x) ∧ ¬On(b, x))
```

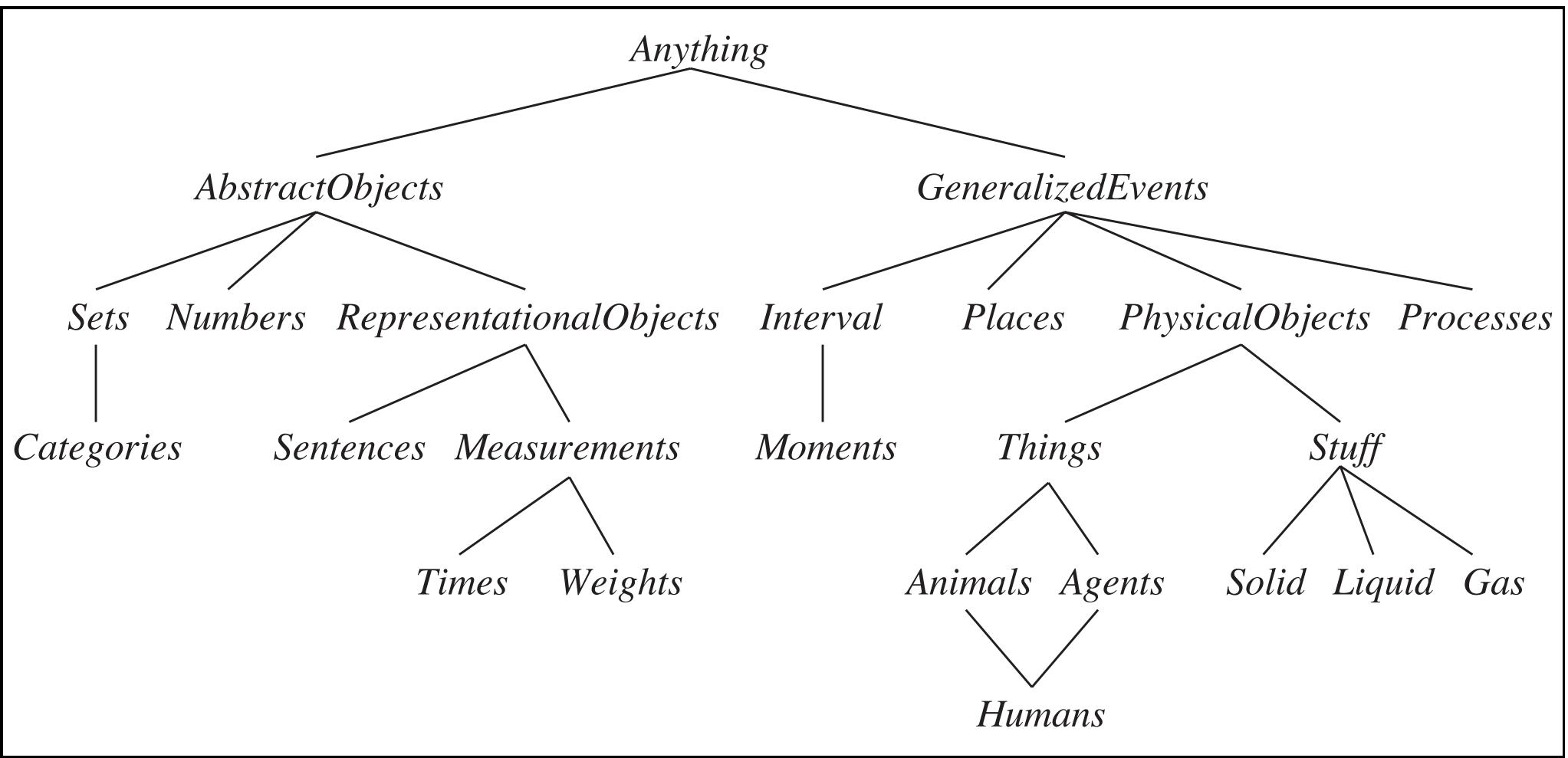
**Figure 10.3** A planning problem in the blocks world: building a three-block tower. One solution is the sequence [ $\text{MoveToTable}(C, A)$ ,  $\text{Move}(B, \text{Table}, C)$ ,  $\text{Move}(A, \text{Table}, B)$ ].



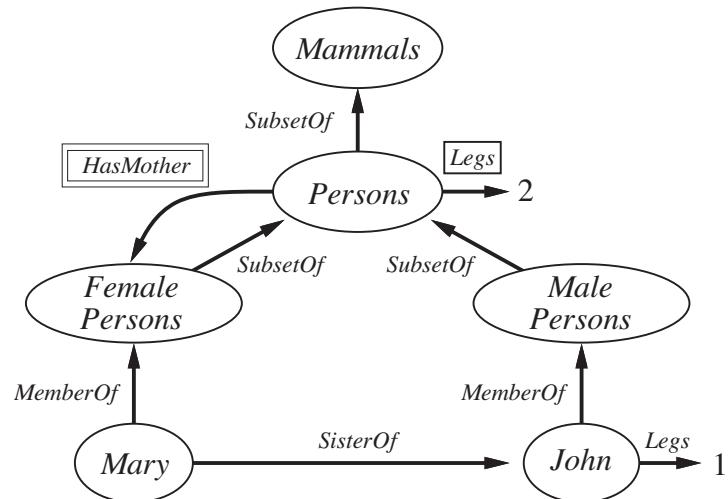
**Figure 10.4** Diagram of the blocks-world problem in Figure 10.3.

# Ontology and Semantic Web

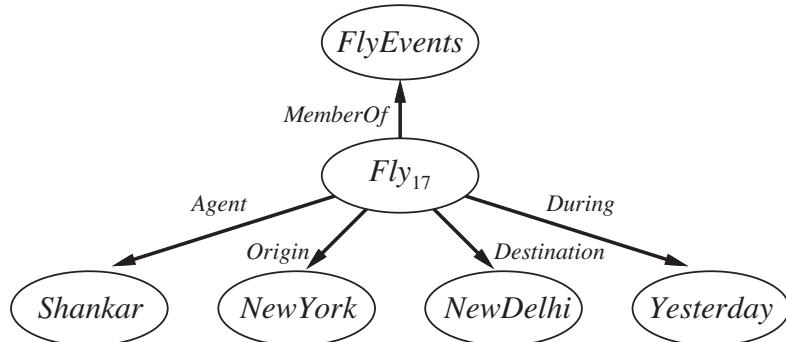
# Up ontology



# Domain ontology



**Figure 12.5** A semantic network with four objects (John, Mary, 1, and 2) and four categories. Relations are denoted by labeled links.



**Figure 12.6** A fragment of a semantic network showing the representation of the logical assertion  $\text{Fly}(\text{Shankar}, \text{NewYork}, \text{NewDelhi}, \text{Yesterday})$ .

# Example: Wordnet

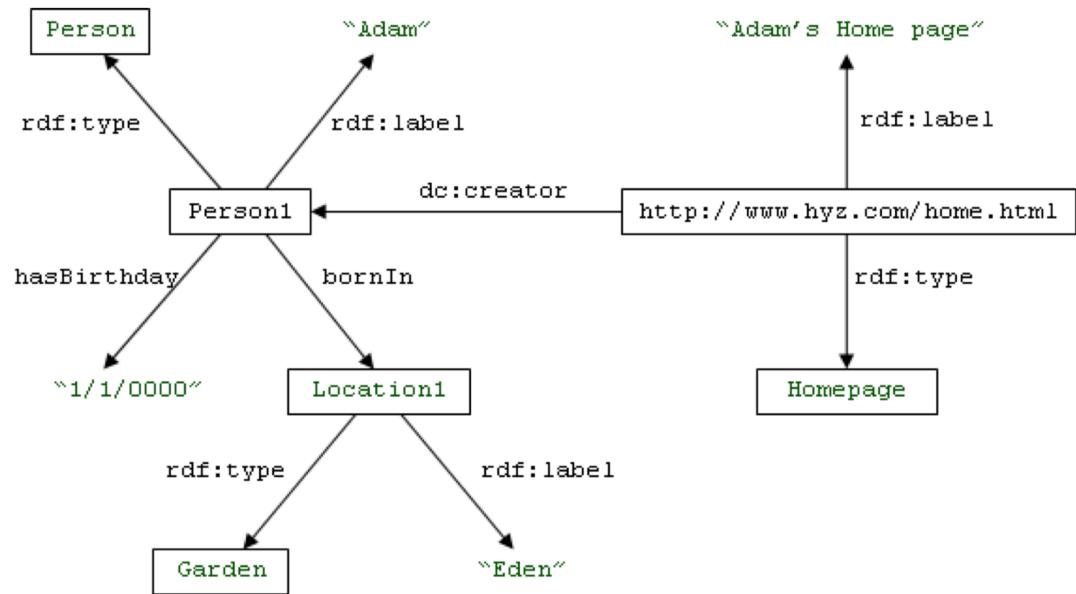
## **Hamburger**

- Hamburger (an inhabitant of Hamburg)
  - direct hypernym:
    - German (a person of German nationality)
  - sister term
    - German (a person of German nationality)
      - East German (a native/inhabitant of the former GDR)
      - Bavarian (a native/inhabitant of Bavaria)
  - derivationally related form
    - Hamburg (a port city in northern Germany on the Elbe River that was founded by Chalemagne in the...)

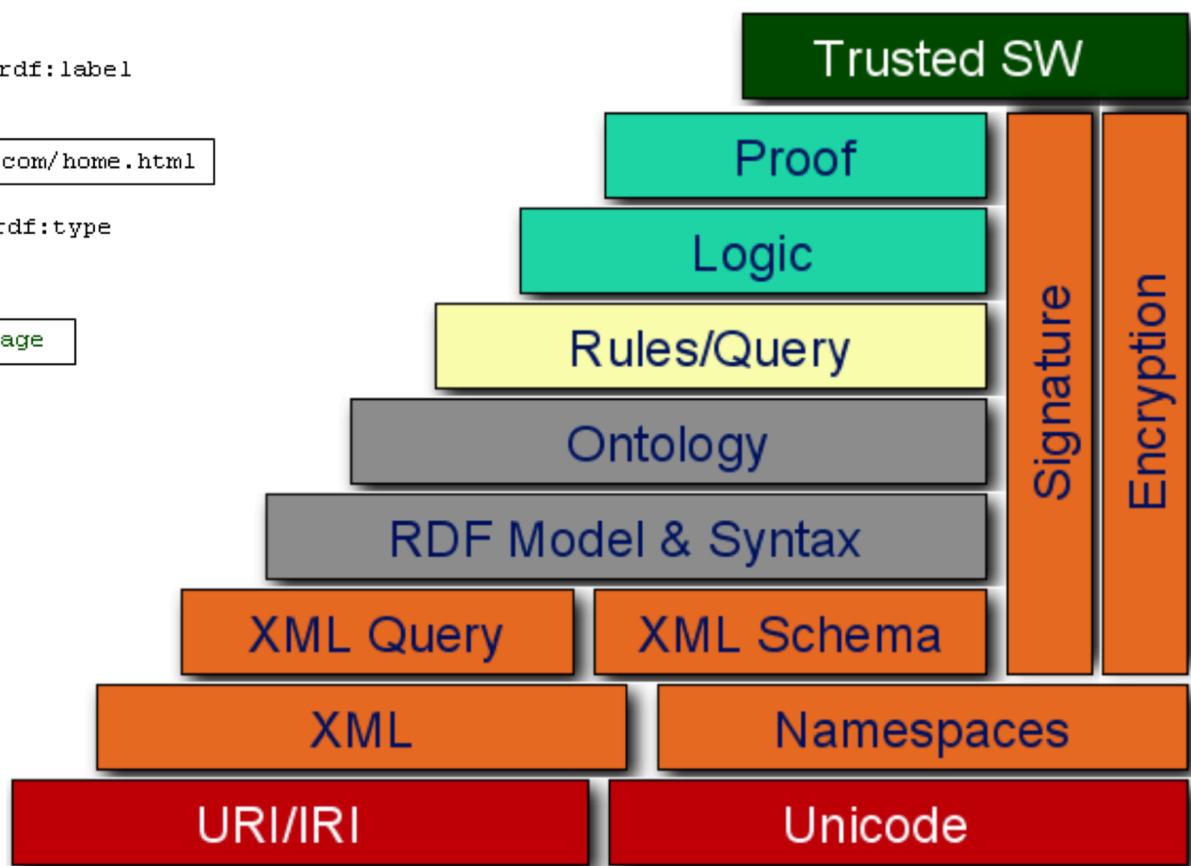
[from wikipedia]

# Semantic web

- handling complex and heterogeneous information resources
- retrieving documents based on a set of relationships that are external to these documents
- providing multiple search options for richer investigation
- targeting and sifting results more efficiently
- using authoritative information resources more effectively as guides to searching



An RDF graph



Hey there! Are you maybe looking for [Firebase](#) instead?

## Data Dumps

 The Firebase API will be completely shut-down on Aug 31 2016. This page provides access to the last available data dump. [Read more...](#)

Data Dumps are a downloadable version of the data in Freebase. They constitute a snapshot of the data stored in Freebase and the Schema that structures it, and are provided under the same CC-BY license. The Freebase/Wikidata mappings are provided under the CC0 license.

## Freebase Triples

This dataset contains every fact currently in Freebase.

Total triples: 1.9 billion

Updated: Weekly

### Data Format: N-

The RDF data is serialized using the N-Triples format, encoded as [L](#)

RDF

```
<http://rdf.freebase.com/ns/g.11vzjz1ynm> <http://rdf.fr  
<http://rdf.freebase.com/ns/g.11vzjz1ynm> <http://rdf.f  
<http://rdf.freebase.com/ns/g.11vzjz1ynm> <http://rdf.f  
<http://rdf.freebase.com/ns/g.11vzjz1ynm> <http://rdf.f  
<http://rdf.freebase.com/ns/g.11vzjz1ynm> <http://www.w
```

★ If you're writing your own code to parse the RDF dumps its often more efficient extracting the data first and then processing the uncompressed data.

<subject> <predicate> <object>

Note: In Freebase, objects have MIDs that look like `/m/012rkqx`. In Freebase schema like `/common/topic` are written as `common_top`.

The *subject* is the ID of a Freebase object. It can be a Freebase MID or a readable ID (ex. `common.topic`) for schema

**RDFS** Freebase foreign key namespaces are also used as predicates to make it easier to look up keys by namespace.

The object field may contain a Freebase MID for an object or a human-readable ID for schema from Freebase or other RDF vocabularies. It may also include literal values like strings, booleans and numeric values.

目录

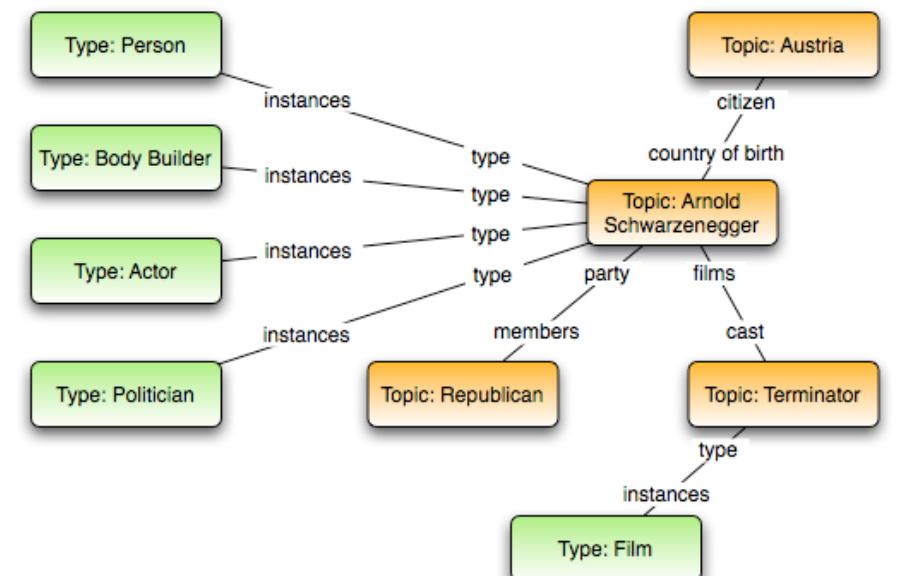
## Freebase Triples

## Freebase Deleted Triples

## Freebase/Wikidata

## Mappings

## Licensing

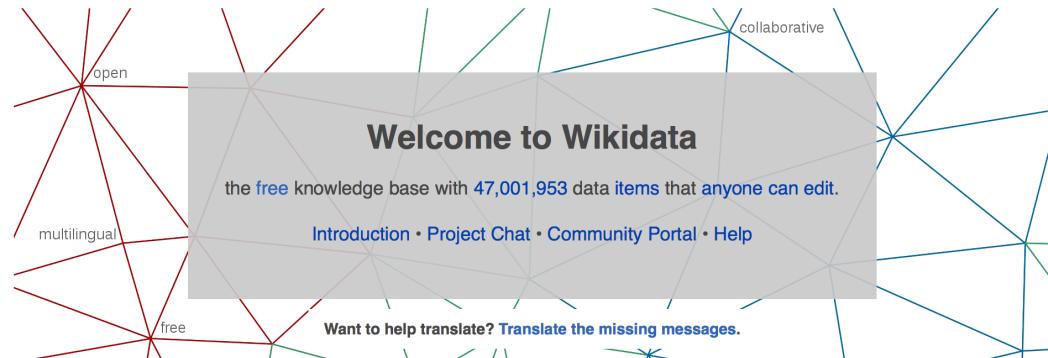


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## Welcome to Wikidata

the free knowledge base with 47,001,953 data items that anyone can edit.

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Wikidata is a free and open knowledge base that can be read and edited by both humans and machines.

Wikidata acts as central storage for the **structured data** of its Wikimedia sister projects including Wikipedia, Wikivoyage, Wikisource, and others.

Wikidata also provides support to many other sites and services beyond just Wikimedia projects! The content of Wikidata is [available](#) under a free license, exported using standard formats, and can be interlinked to other open data sets on the linked data web.

### value

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#### qualifiers

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- Explore Wikidata by looking at a featured showcase item for author [Douglas Adams](#).
- Get started with Wikidata's [SPARQL query service](#).

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item: [Earth \(Q2\)](#)

property: [highest point \(P610\)](#)

custom value: [Mount Everest \(Q513\)](#)

### Popular items

- 2018 Toronto van attack (Q52152274)
- 2018 Giro dell'Appennino (Q51687919)
- Liège–Bastogne–Liège for Women 2018 (Q42116955)
- Saleh Ali al-Sammad (Q19429078)
- Marguerite Rouvière (Q51954596)
- Karen Karapetyan (Q1979923) (pictured)
- Semiramis Hotel bombing (Q2086153)



### Discover

label — **Douglas Adams** (Q42) —

description English writer and humorist  
Douglas Noël Adams | Douglas Noel Adams  
► [In more languages](#)

property — [educated at](#) —

rank

statement group

**Statements**

**educated at** (Q42)

St John's College

end time 1974  
academic major English literature  
academic degree Bachelor of Arts  
start time 1971

2 references

stated in Encyclopædia Britannica Online  
reference URL <http://www.nndb.com/people/731/000023662/>  
original language of work English  
retrieved 7 December 2013  
publisher NNDDB  
title Douglas Adams (English)

+ add reference

Brentwood School

end time 1970  
start time 1959

0 references

+ add (statement)

# Example application

NJUAI

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**张飞\_百度百科**

职业：武将  
主要成就：当阳挡曹军、取西川、宕渠大胜  
简介：张飞（？—221年），字益德，幽州涿郡（今河北省保定市涿州市）人氏，三国时期蜀汉名将。刘备长坂坡败退，张飞仅...  
[人物生平](#) [历史评价](#) [后世地位](#) [艺术造诣](#) [轶事典故](#) [更多>>](#)  
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baike.baidu.com/ 2014-10-12

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[zhidao.baidu.com/link?...](#) - 80%好评  
[张飞的真正死因!](#) 10个回答 2013-07-17  
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月活跃用户: 3224人 累计发贴: 10万

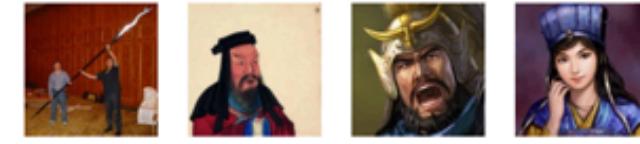
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赵云 三国时期蜀汉名将  
关羽 五虎上将关云长  
吕布 三国第一猛将  
貂蝉 舍锦绣年华得美名千秋

**相关人物** 展开▼

  
刘备 三国时期蜀汉开国皇帝  
荀彧 东汉末年著名政治家  
水镜八奇 八奇中的最强者  
许褚 三国时期曹操猛将

**其他人还搜** 展开▼

  
丈八蛇矛 张飞所用兵器  
曹操 可爱的奸雄  
八虎骑 曹操帐下八位虎将  
诸葛亮 谢谢你的女儿之名



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成立	人工智能学院	...	教授	毕飞宇	...
简称	南大	...	党委书记	张异宾	...
国际关系研究院院长	朱锋	...	商学院院长	赵曙明	...

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