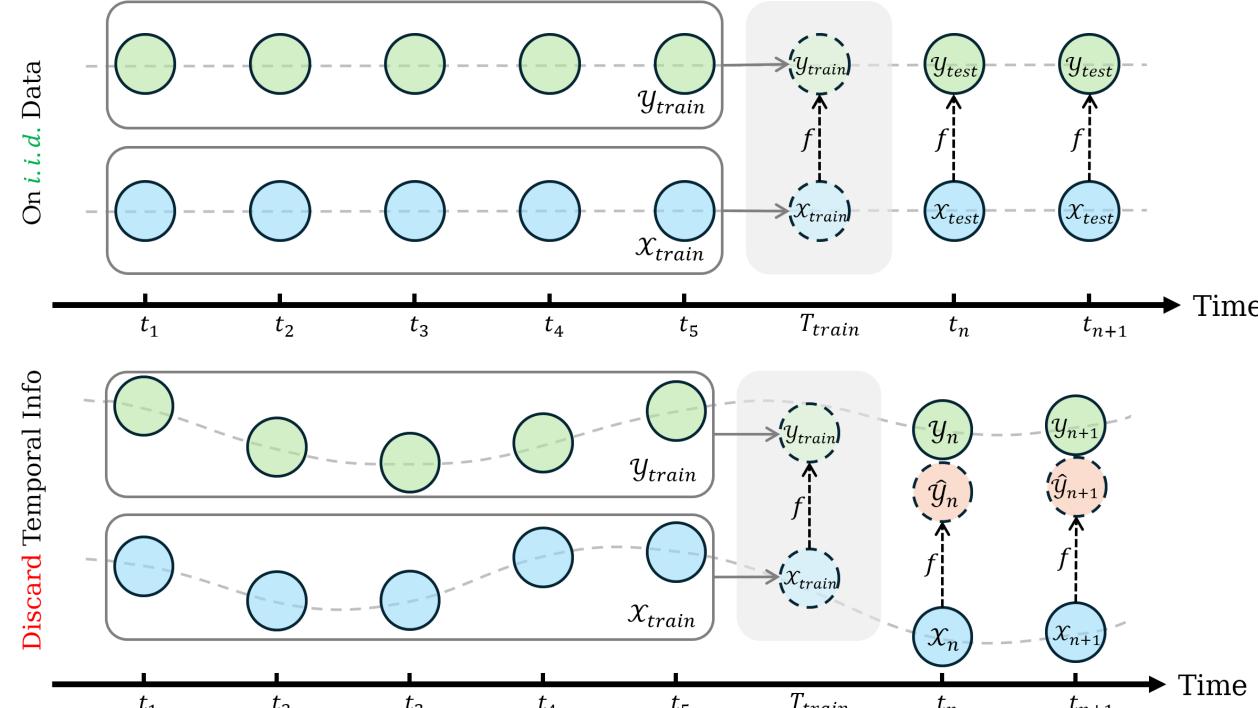




## Challenges in Learning from Temporal Tabular Data

Most machine learning approaches are built on the **assumption of i.i.d. data**. However, tabular data are often **collected over time**, resulting in **temporal shifts** at each time point.

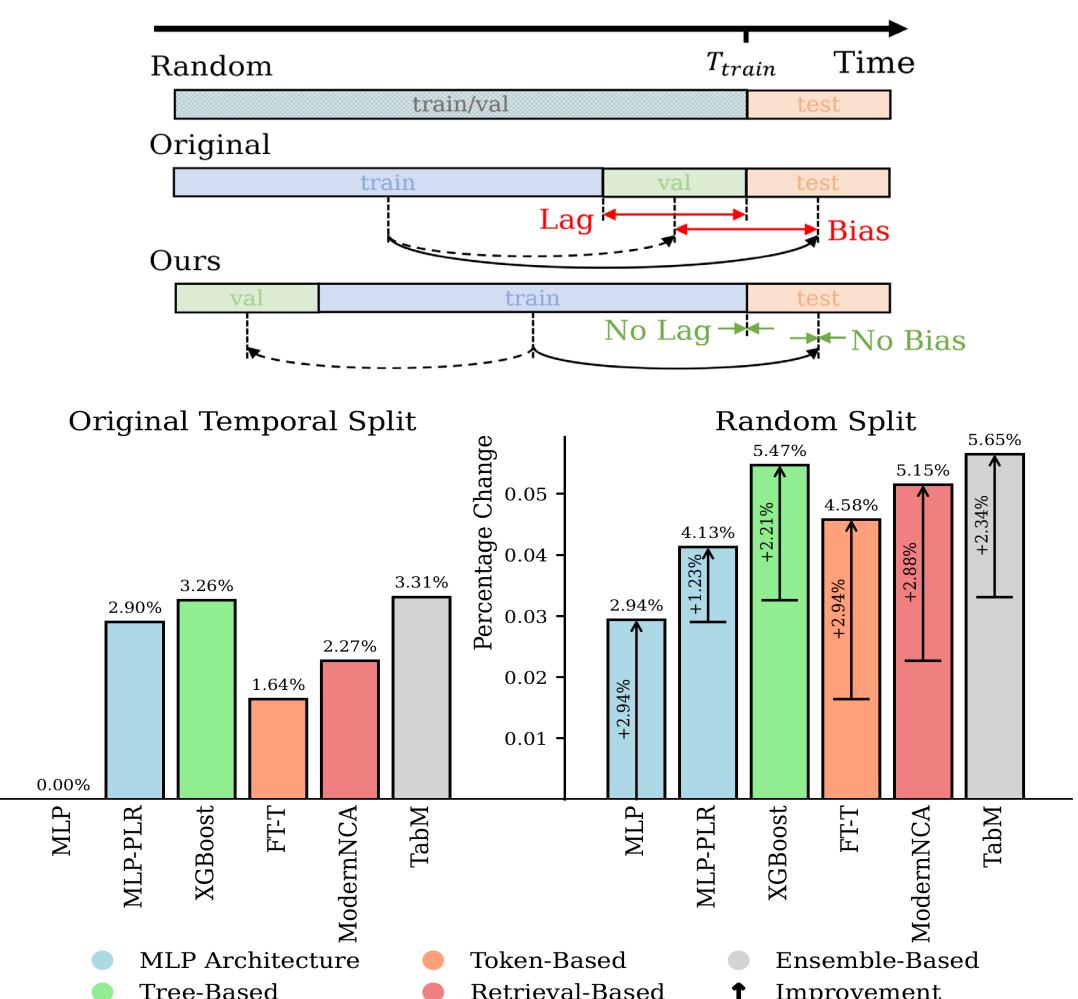


- How can existing models **be better trained** under temporal shifts?
- How can models be equipped with **temporal adaptability**?

## Why Temporal Splits Fail?

TabReD [Rubachev et al., ICLR'25] employs a **temporal validation split**, utilizing earlier data for training and later data for model selection.

We discovered that even when **randomly splitting** the training and validation sets, the model outperformed the temporal split.

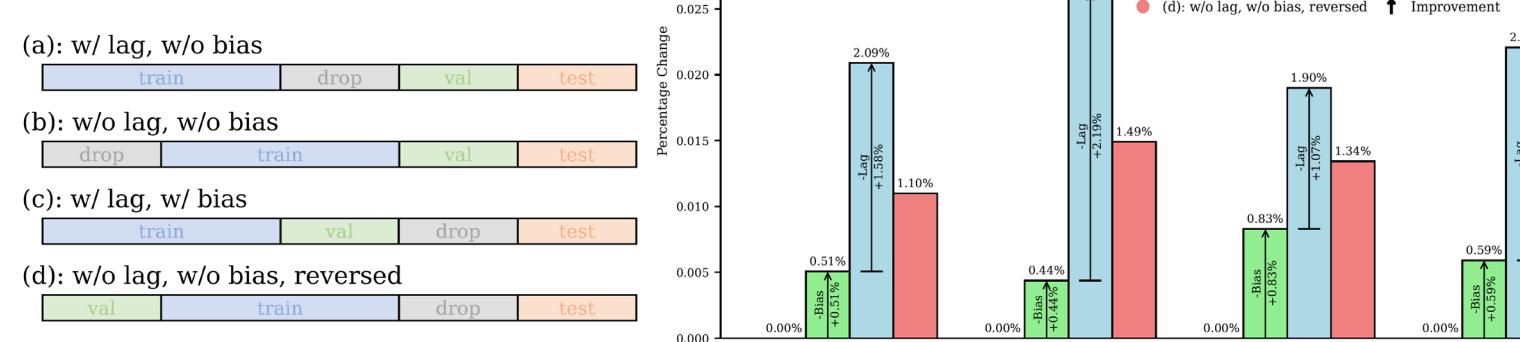


Start from the most intuitive difference:

- **Training lag:** the training-available data closest to the test time are not used for training.
- **Validation bias:** the shift degree of test set relative to validation set is more significant in temporal splits.

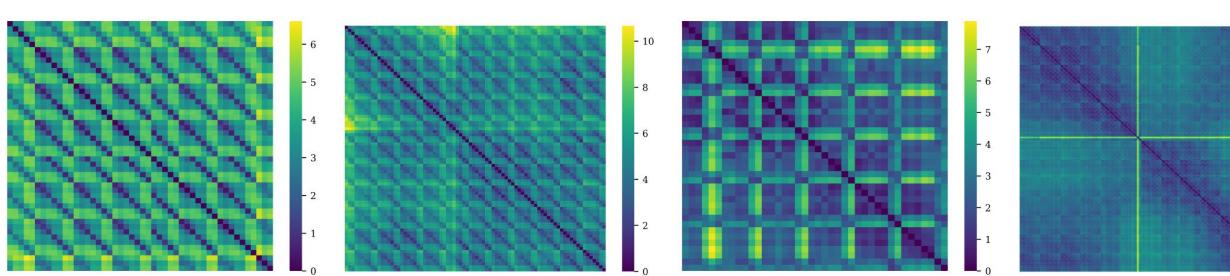
Comparable performance with better stability.

**Ablation studies & loss distribution:** the effectiveness in reducing training lag and validation bias.



- Training lag↓: better *test-time* performance.
- Validation bias↓: better generalization.

**MMD visualization** confirms the empirical uniformity of temporal shifts across time slices.



## Training Protocol

We introduce the following **training protocol** for temporal data:

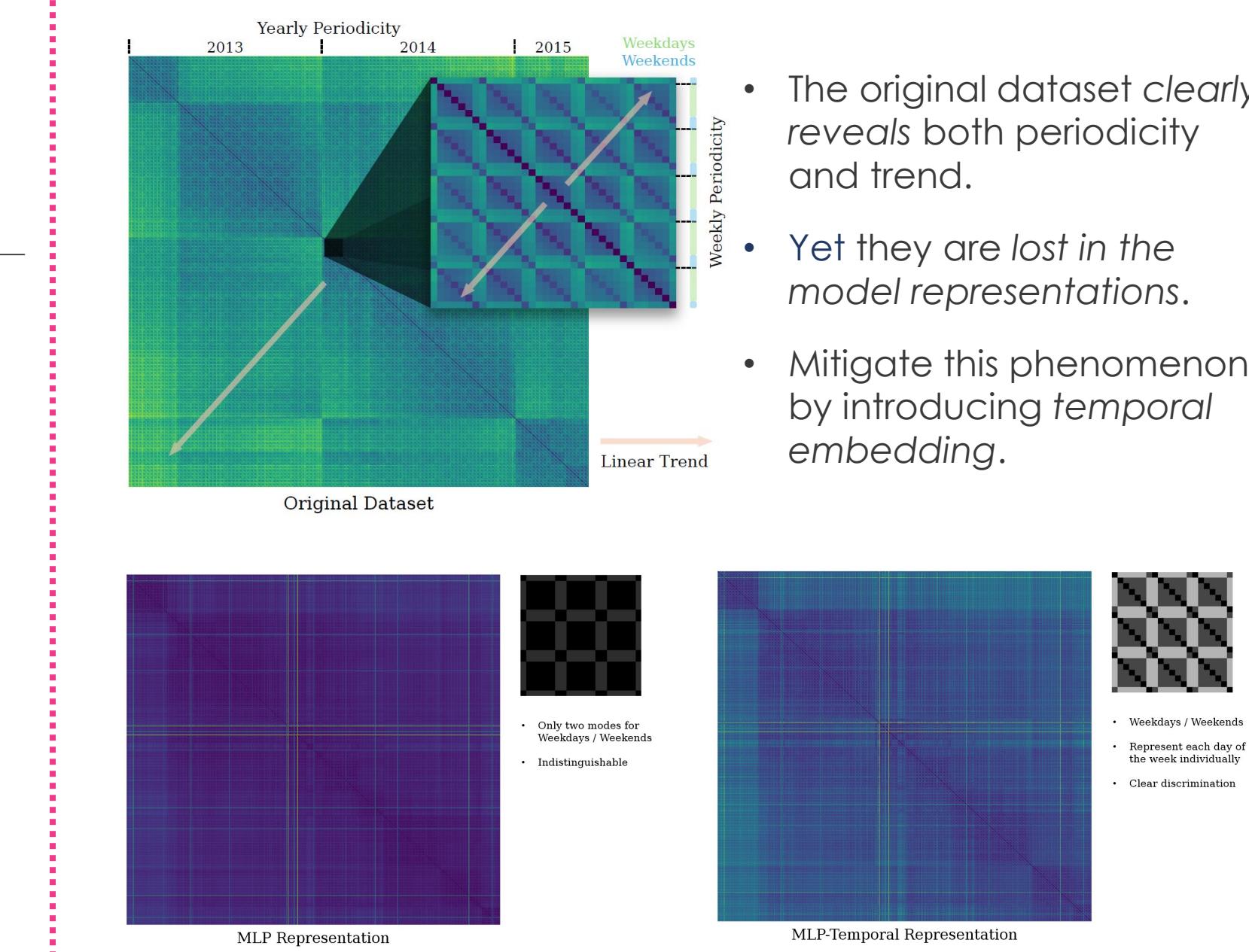
1. The **lag** between **training** and **test** set should be minimized.
2. The **validation bias** should be minimized.
3. Effective validation can be achieved in the **reverse temporal direction** by aligning the shift in the validation set with the actual shift between training and testing data.

	Splits	Avg. Imp.
Mean Performance ↑	Original	-
	Random	+2.17%
	Ours	<b>+2.18%</b>
Standard Deviation ↓	Original	-
	Random	+154%
	Ours	<b>+16.7%</b>

Comparable performance with better stability.

## Model Representation

The **loss of the rich temporal information** during training.



## Temporal Embedding

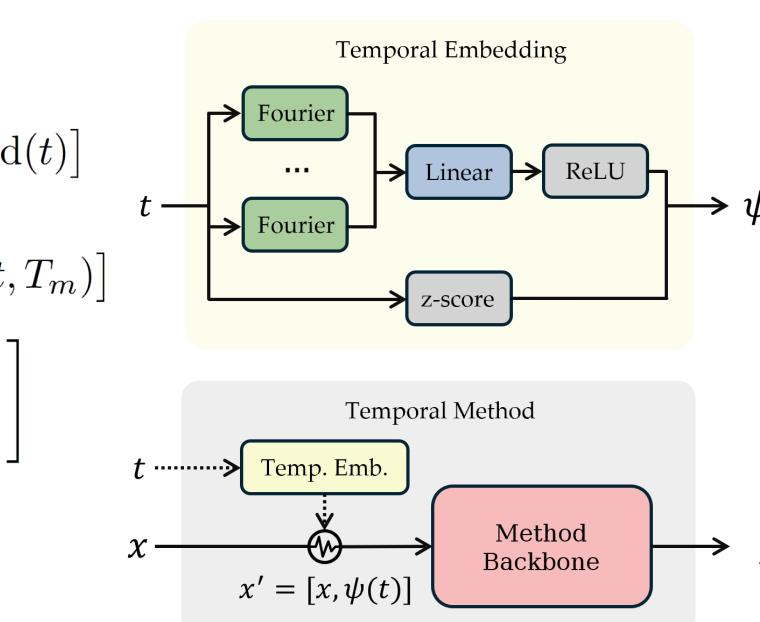
Compensate for temporal information via **temporal embedding**.

$$\psi(t) = [\text{ReLU}(\text{Linear}(\text{Periodic}(t))), \text{Trend}(t)]$$

$$\text{Periodic}(t) = [\text{Fourier}(t, T_1), \dots, \text{Fourier}(t, T_m)]$$

$$\text{Fourier}(t, T) = \left[ \sin\left(\frac{2\pi kt}{T}\right), \cos\left(\frac{2\pi kt}{T}\right) \right]$$

$$\text{Trend}(t) = \text{z-score}(t)$$



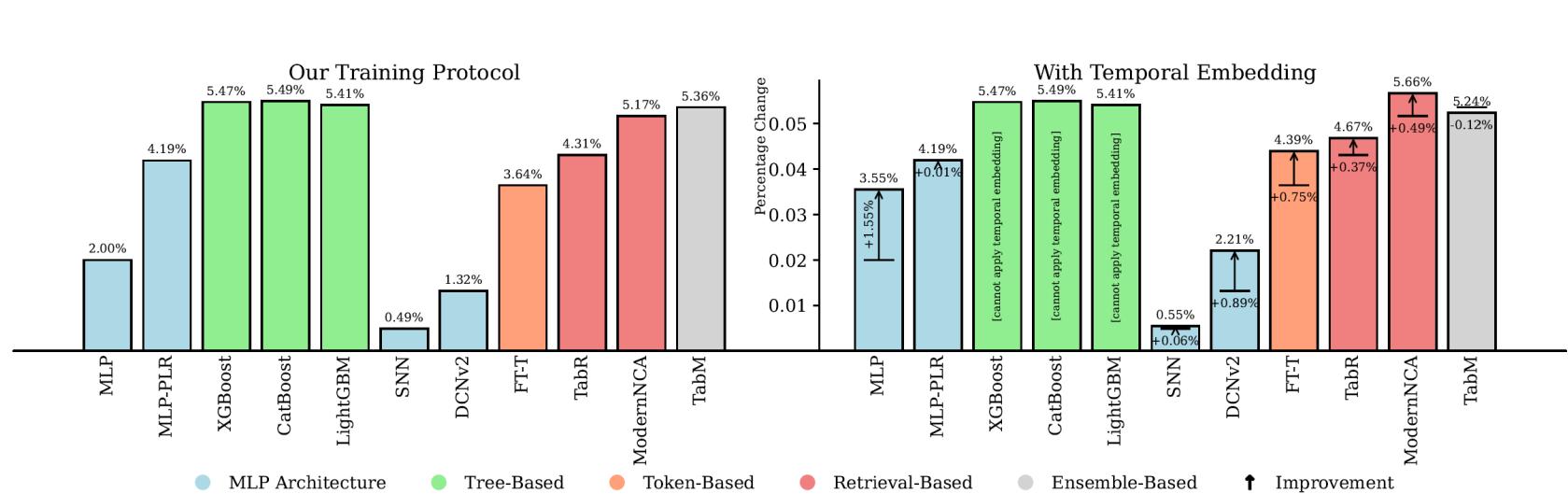
The states in the temporal cycles may exhibit a **square wave** form, e.g., weekdays and weekends, requiring higher-order sine and cosine terms for precise representation.

Emb.	MLP	MLP-PLR	ModernNCA	Avg. Imp.
Num	-	-	-	-0.04%
Time	-	-	-	-0.32%
TabPFN-TS [Hoo et al., NeurIPS'24 WS]	+0.25%	-	-	-0.43%
PLR [Gorishniy et al., NeurIPS'22]	+0.70%	+0.01%	+0.02%	+0.25%
Ours	<b>+1.31%</b>	+0.01%	+0.30%	+0.54%

- **Learnable & scalable.**
- Fourier expansion for precisely capture **periodicity**.
- Uses normalized timestamps as a **trend** feature.
- Leads to a further 0.74% gain in performance.

## Results

**Performance comparison** before and after adopting our temporal embedding into our training protocol on TabReD benchmark.



**Performance rankings** of original temporal split, random split, and our temporal split with and without our temporal embedding.

Splits	MLP	PLR	FT-T	SNN	DCNv2	TabR	MNCA	TabM	XGBoost	CatBoost	LightGBM	SNN	DCNv2	FFT	TabR	ModernNCA	TabM
TabReD	7.750	4.375	6.875	9.375	8.250	7.375	6.500	<b>3.125</b>	3.375	4.250	4.750						
Random	8.250	5.625	5.625	10.250	9.625	8.000	<b>4.750</b>	<b>2.750</b>	3.125	3.125	4.875						
Ours	8.000	5.750	7.500	9.500	8.375	8.125	4.875	4.000	3.375	2.125	4.375						
Ours + temporal embedding	7.875	6.625	6.250	9.625	9.250	6.250	<b>4.625</b>	3.125	4.500	2.875	5.000						

## Contact

