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EEG Tensor Discriminant Analysis for Brain Computer Interface

Liqing Zhang





Brain Computer Interface

Outline



Background



Problem Formulation



EEG Feature Extraction



BCI Platform and Apps



Perspectives





Research Interests

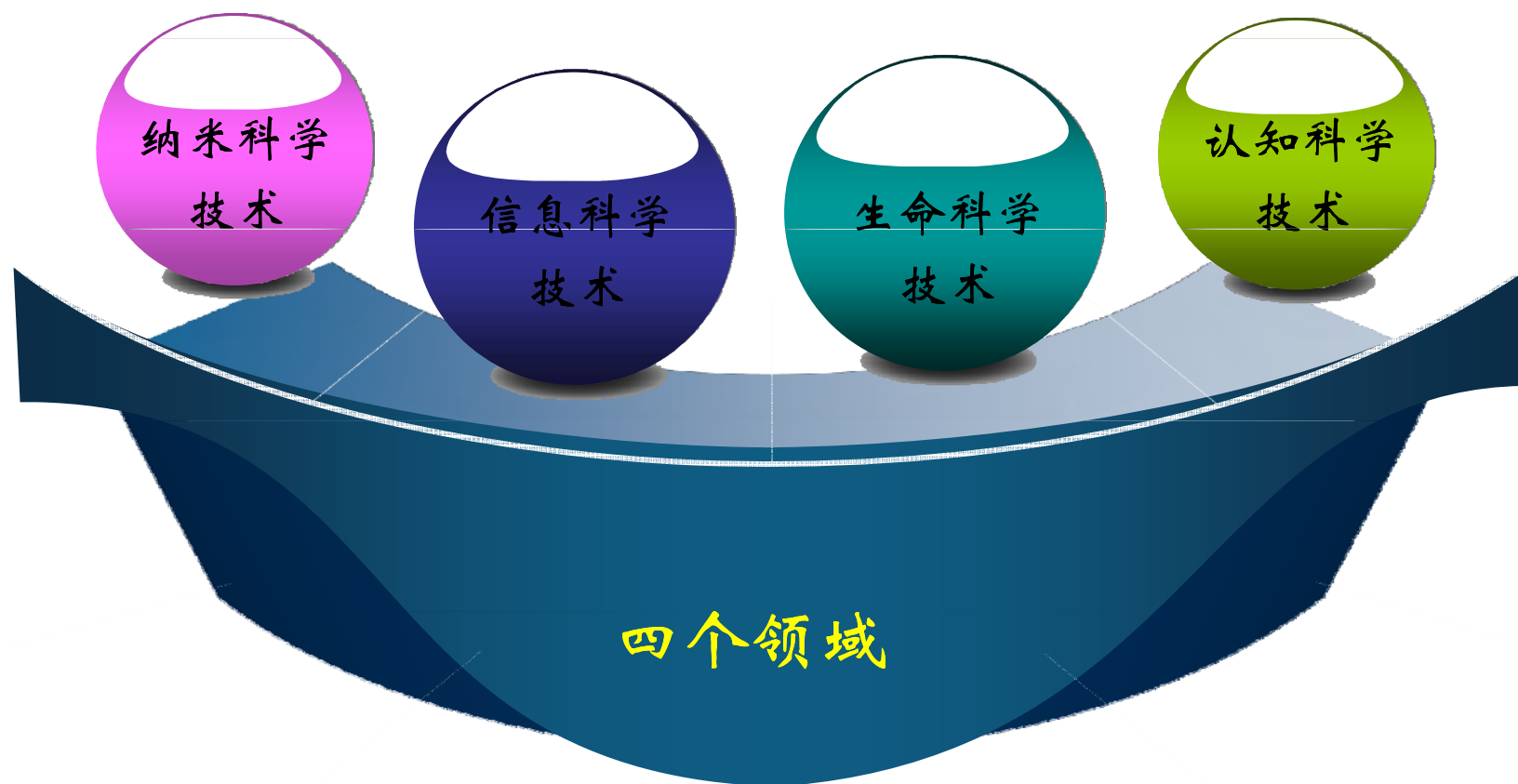
- Natural/Intelligent Human Computer Interaction (HCI)
 - Brain-like Computing (Structure & Principle)
 - Visual Neural Representation and Coding
 - Multimodal (Visual/auditory) Interaction
 - Machine Selective Attention
 - Brain-Computer Interface
 - Wearable Computing (E-Health)
- To build a human-machine integrated System





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为提升人类能力的融合技术



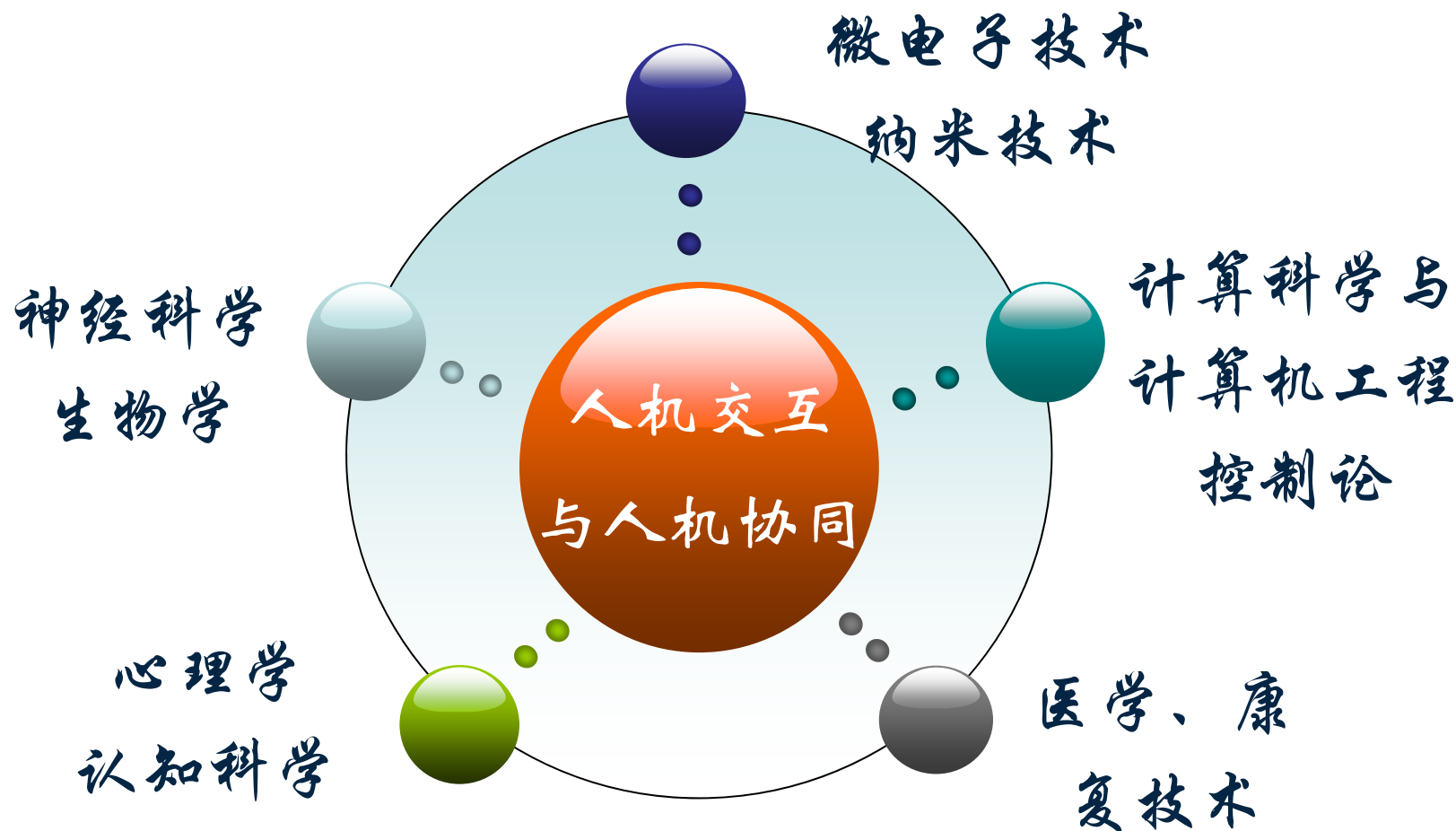
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BCI – 典型汇聚技术



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BCI应用：家电/电话BCI控制

Tsinghua Group Gao et al., 1999, 2002, 2003



家电控制



BCI电话



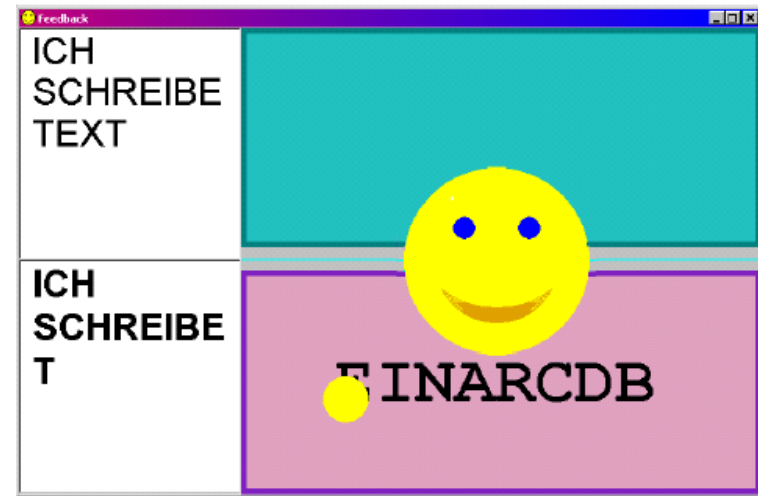
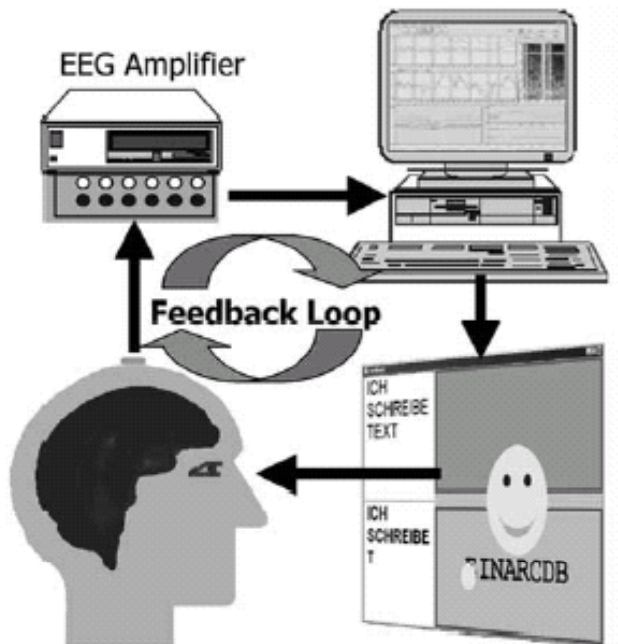
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BCI应用：字符输入

Tübingen Group *Birbaumer et al., 2000, Hinterberger et al., 2004*

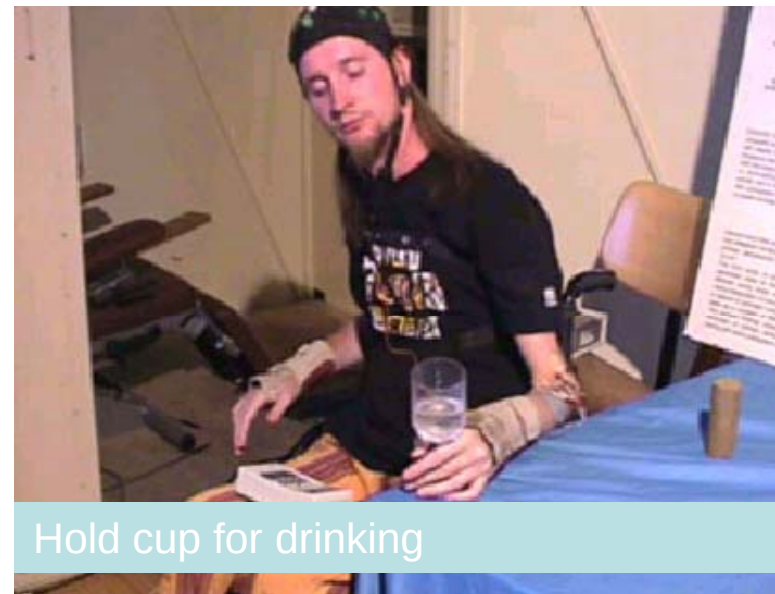




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BCI应用： 残疾人自助

Graz Group *Pfurtscheller et al., 1993, 2000, 2003*



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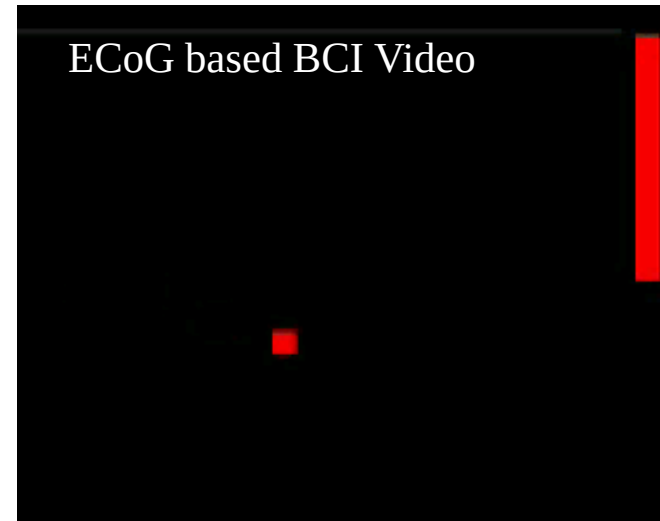




BCI应用： BCI 游戏



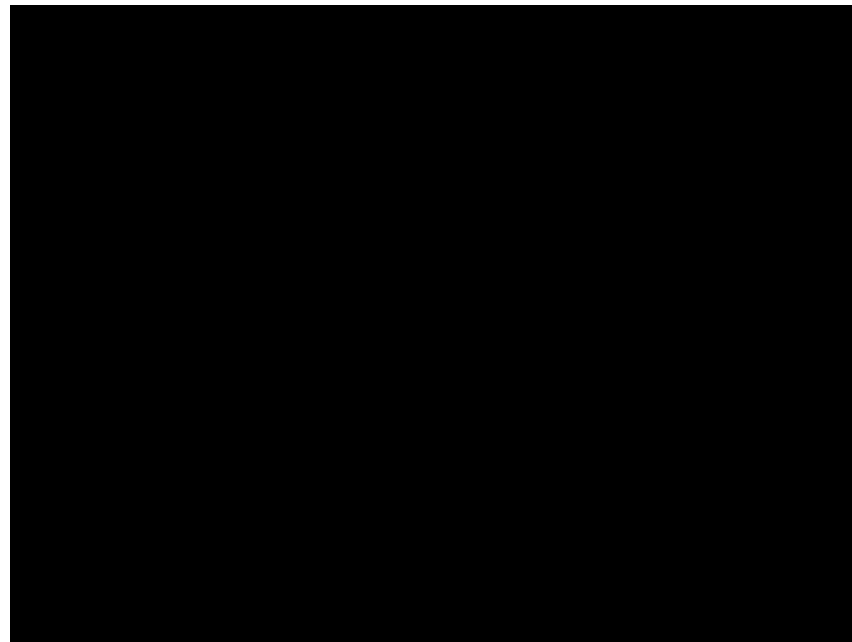
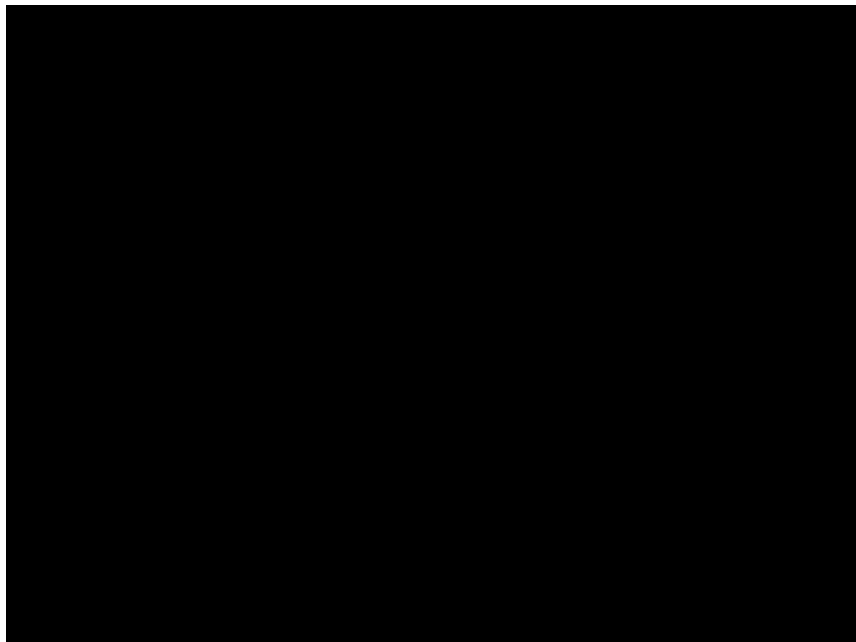
Pfurtscheller et al., 2003



Leuthardt et al., 2004



BCI应用：轮椅车BCI控制



Shanghai Jiao Tong University, 2009



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BCI应用

➤ 生物医学工程领域

- ✓ 肢残人的康复训练、控制假肢、BCI残疾人轮椅
- ✓ 健康监护系统、疾病判别

➤ 认知、心理学研究

- ✓ 情感、警觉度等精神状态估计预测

➤ 军事领域：“心思认知”系统与“意识头盔”

➤ 人工智能领域：理解人类大脑智能信息处理机理和认知过程

➤ 娱乐领域：脑操纵游戏





脑机交互神经机理

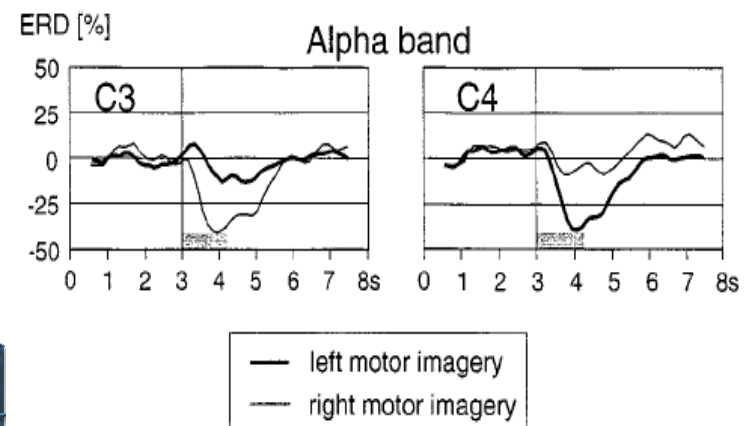
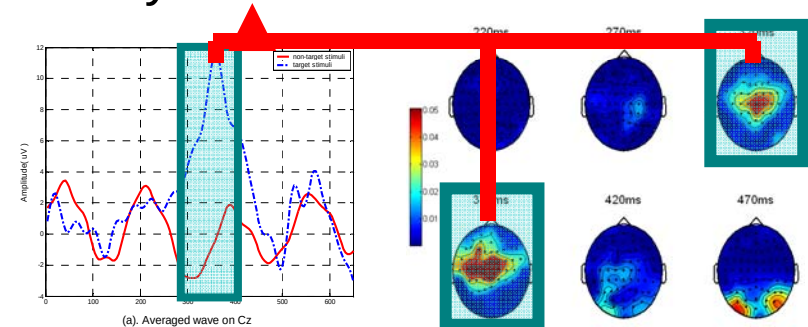
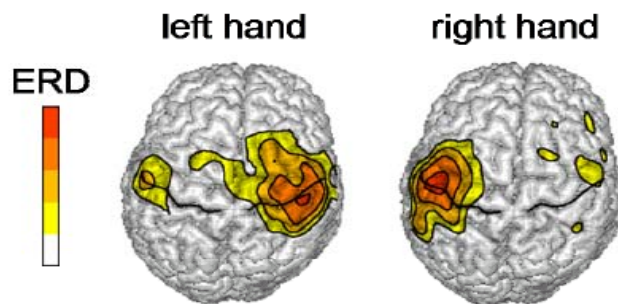
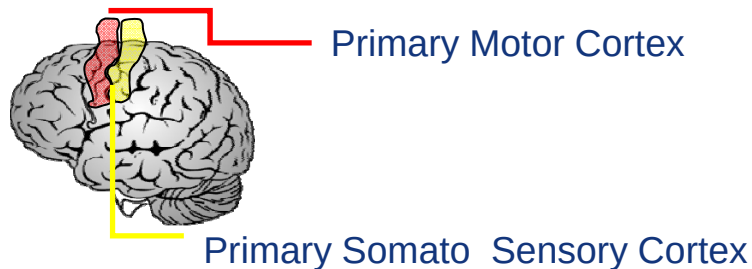
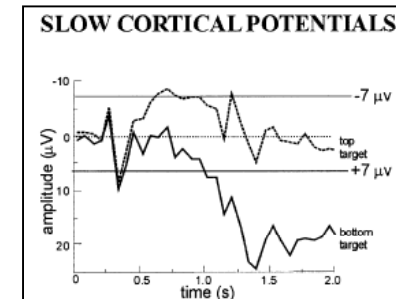
特性	诱发电位			自发电位		
	VEP	SSVEP	P300	SCP	ERD/ERS	TRSD/TRSS
需外部刺激信号	✓	✓	✓	×	×	×
需主动意识参与	×	×	✓	✓	✓	✓
属单次反应	✓	×	✓	×	✓	×
属多次反应	×	✓	×	✓	×	✓
锁时性	✓	×	✓	×	✓	×
锁相性	✓	✓	✓	×	×	×
同步性	✓	×	✓	×	✓	×
异步性	×	✓	×	✓	×	✓
需用户长期训练	×	×	×	✓	×	×





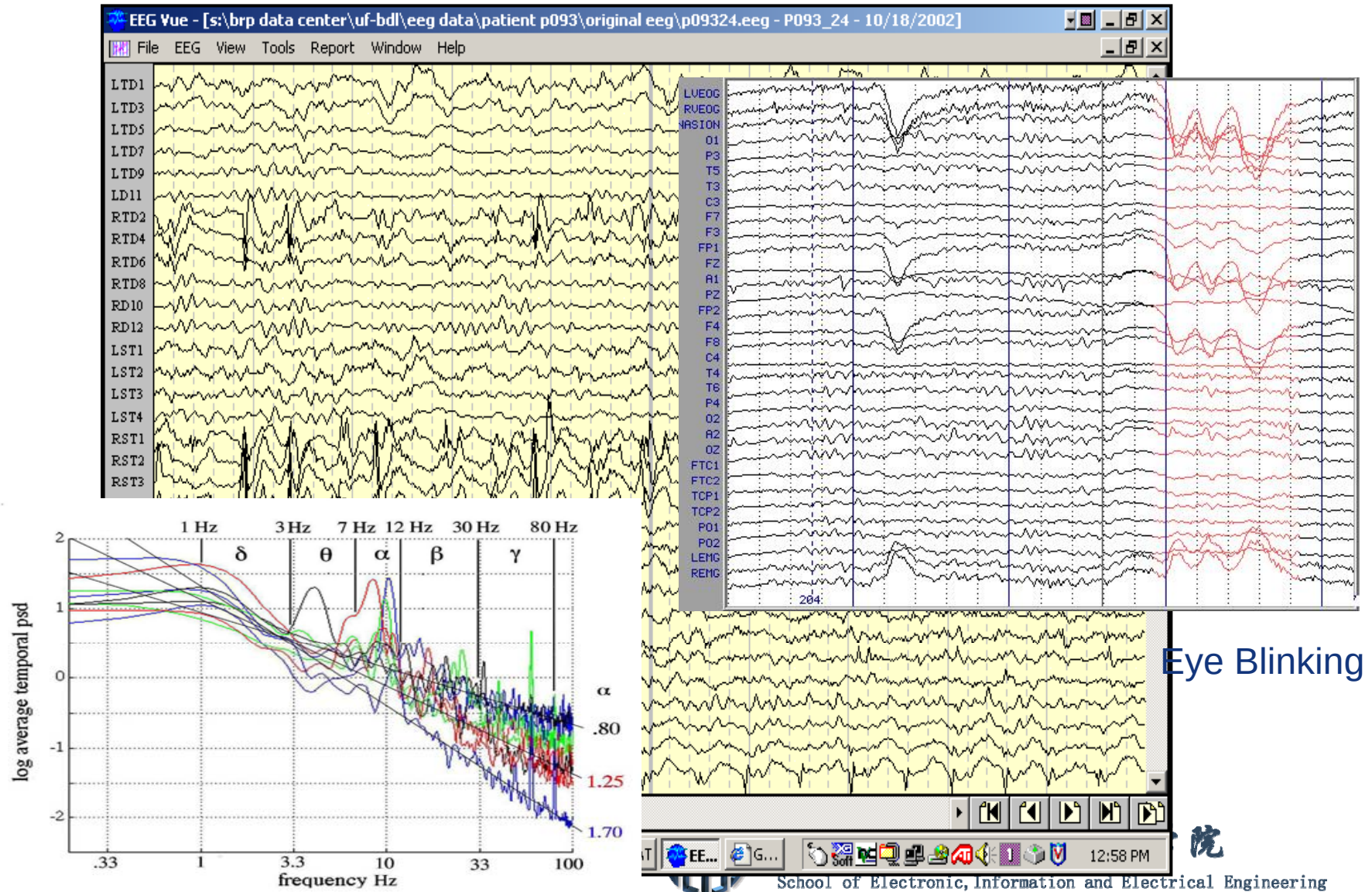
Neurophysiological Fundamentals

- Slow Cortical Potential (SCP)
- Steady state visual evoked potential (SSVEP)
- P300
- The event-related desynchronization and synchronization (ERD/ERS)





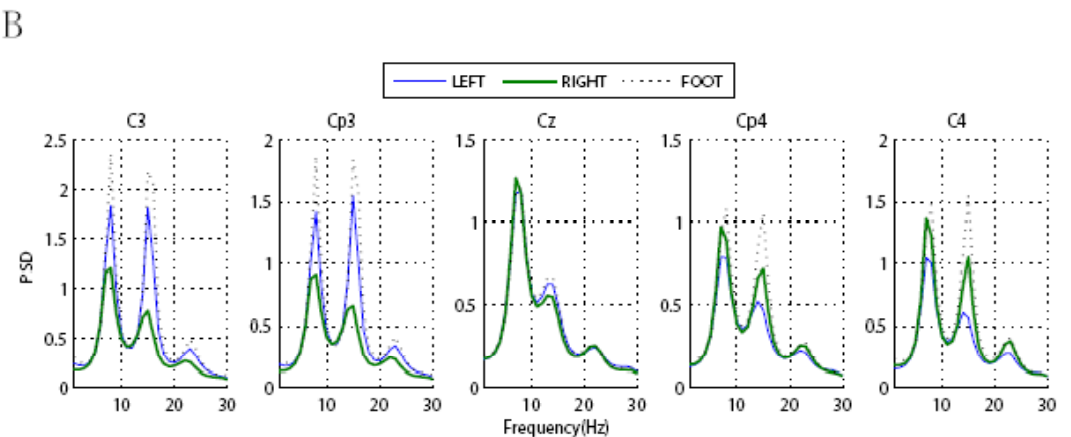
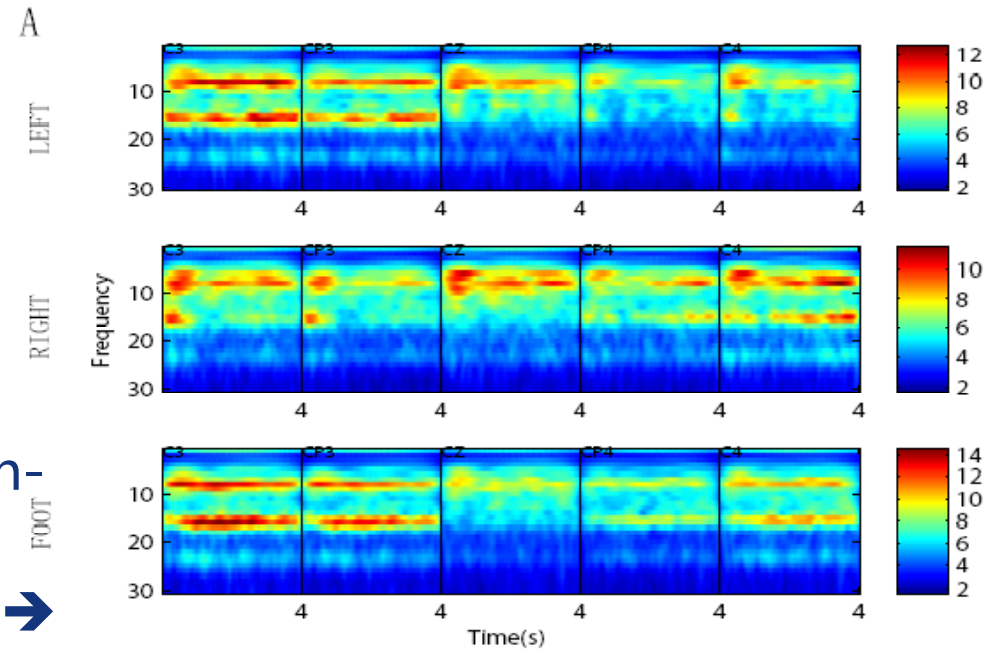
EEG Data





Task-Related Sustained ERD/TRSD

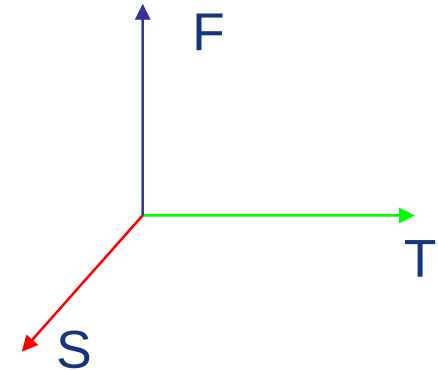
- Repeat Imagery Task
- Sustain ERD for certain period
- ERD- $\rightarrow$ TRSD
- Advantage
 - Non-phase lock; Non-time lock
 - Binary control value $\rightarrow$ real control value
 - New dimension for control





Methods for Feature & Classification

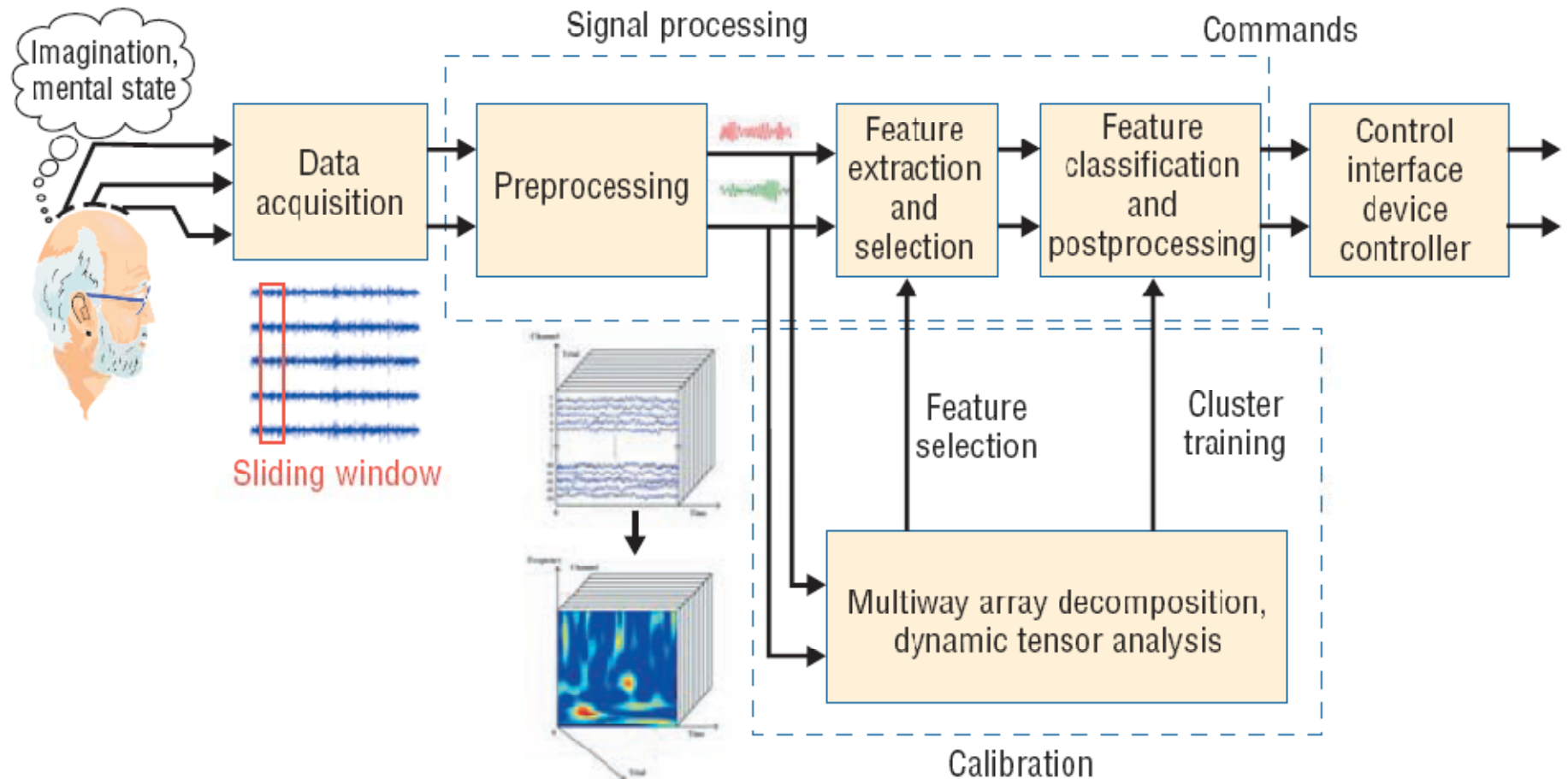
- Preprocessing
 - Temporal filtering; channel selection
 - Denoising and Enhancement (BSS, cICA)
- Feature Extraction
 - Common Spatial-frequency Pattern (CSFP)
 - Incremental CSP (ICSP)
 - Common Tensor Decomposition Analysis (CTDA)
- Pattern Classification
 - Support Vector Machine (SVM)
 - Discriminant Analysis (LDA / FDA)



Extraction method	Time	Freq.	Space	Examples
Time-Frequency Representation	✓	✓	✓	STFT, wavelet
Cell firing rate	✓	✓	✓	-
Power Spectral Density	✗	✓	✓	Welch
Pattern matching	✓	✗	✓	Correlation
Raw signal	✓	✗	✓	Amplitude
Model parameters	✓	✗	✓	AR, AAR, Kalman
Other transforms	✓	✗	✓	ICA, PCA



Feature Extraction Based TF

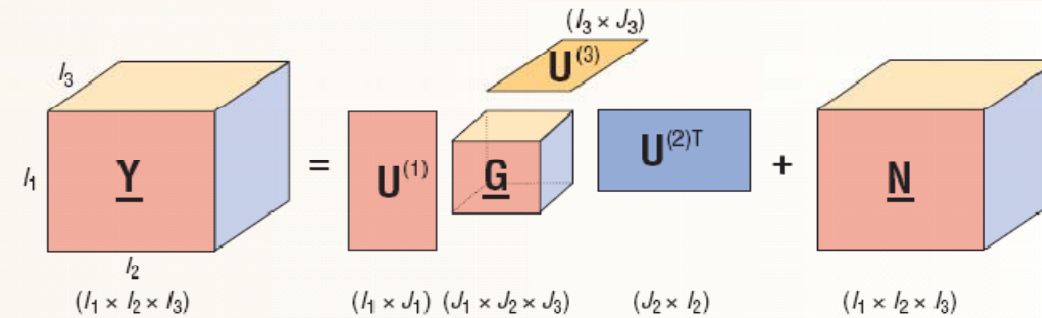




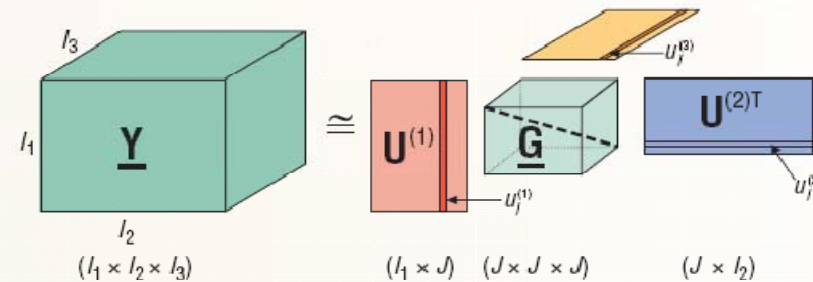
Tensor Decomposition

$$\underline{\mathbf{Y}} = \underline{\mathbf{G}} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{U}^{(2)} \dots \times_N \mathbf{U}^{(N)} + \underline{\mathbf{N}}$$

Tucker



(1)



(2)

PARAFCA

$$= \lambda_1 \mathbf{u}_1^{(1)} \mathbf{u}_1^{(2)} \mathbf{u}_1^{(3)} + \dots + \lambda_J \mathbf{u}_J^{(1)} \mathbf{u}_J^{(2)} \mathbf{u}_J^{(3)}$$

$$\underline{\mathbf{Y}} \cong \sum_{j=1}^J \lambda_j \mathbf{u}_j^{(1)} \circ \mathbf{u}_j^{(2)} \circ \dots \circ \mathbf{u}_j^{(N)} = \underline{\mathbf{\Lambda}} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{U}^{(2)} \dots \times_N \mathbf{U}^{(N)}$$

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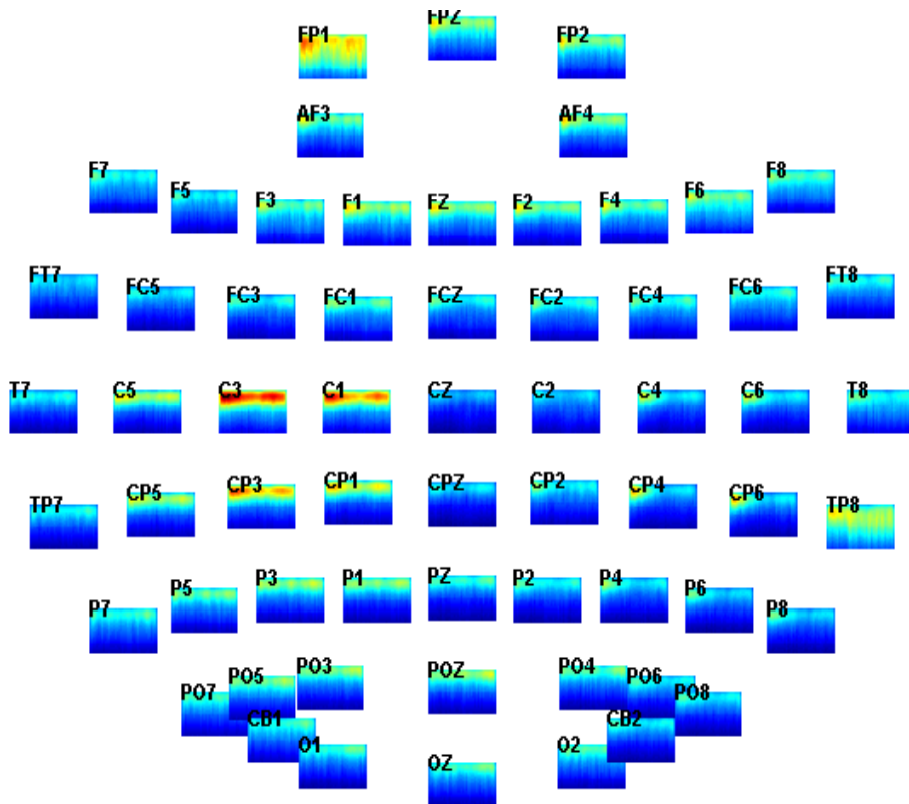
Information and Electrical Engineering



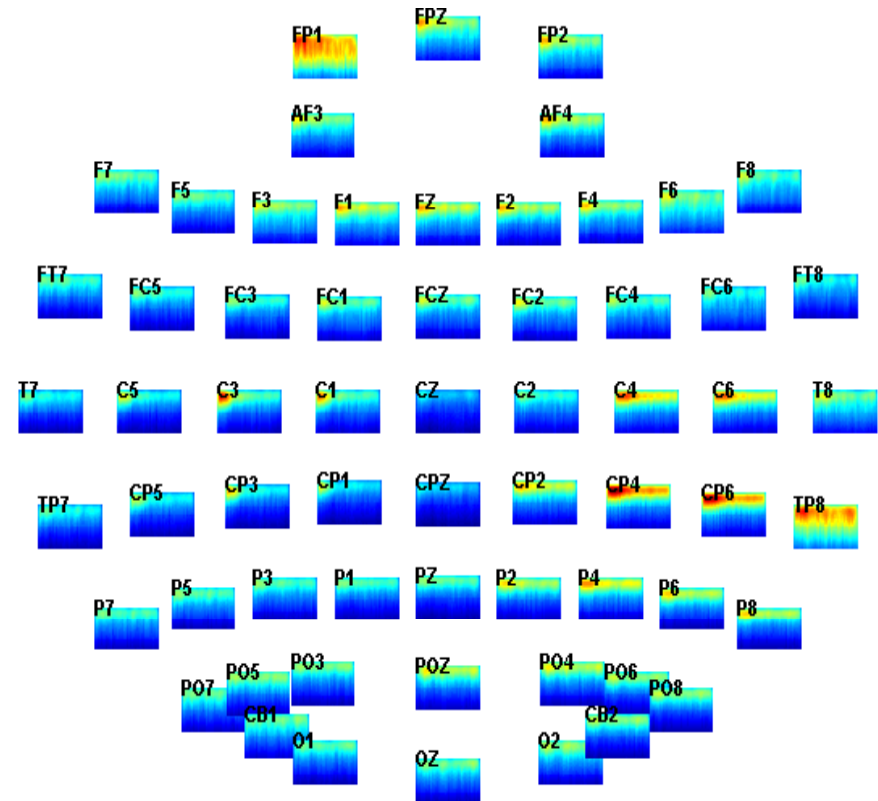
Tensor Representation

➤ Averaged Tensor

Left hand imagery



Right hand imagery



$$\chi^{channel \times frequency \times time \times class}$$





Common Spatial Frequency Pattern

➤ CWT Transform (Morlet Wavelet)

$$W^{c,k}(a, t) = \frac{1}{\sqrt{a}} \int_{-\infty}^{+\infty} x^{c,k}(\tau) \psi\left(\frac{\tau - t}{a}\right) d\tau,$$
$$\mathbf{p}_k^{c,f} = \left\| \hat{W}^{c,k}(f, t) \right\|^2,$$

➤ Temporal-Frequency Vectors

$$\mathbf{U}_k^c = \left(\mathbf{p}_k^{c,f_1} \mathbf{p}_k^{c,f_2} \cdots \mathbf{p}_k^{c,f_m} \right)^T \text{ and } \mathbf{V}_k^f = \left(\mathbf{p}_k^{c_1,f} \mathbf{p}_k^{c_2,f} \cdots \mathbf{p}_k^{c_n,f} \right)^T,$$

➤ Vectorizing

$$\mathbf{Y}_k = \begin{bmatrix} \mathbf{U}_k^{c_1} \\ \mathbf{U}_k^{c_2} \\ \vdots \\ \mathbf{U}_k^{c_n} \end{bmatrix} \quad \text{or} \quad \mathbf{Y}_k = \begin{bmatrix} \mathbf{V}_k^{f_1} \\ \mathbf{V}_k^{f_2} \\ \vdots \\ \mathbf{V}_k^{f_m} \end{bmatrix},$$

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Common Spatial Frequency Pattern (CSFP)

- Objective Function (Multi-task)

$$\operatorname{argmax}_{\mathbf{w}} \frac{\mathbf{w}^T \mathbf{S}_I \mathbf{w}}{\mathbf{w}^T \mathbf{S}_T \mathbf{w}}, \quad \mathbf{S}_I = \Gamma^{(i)}|_{i=1}^M, \quad \mathbf{S}_T = \frac{1}{M} \sum_{i=1}^M \Gamma^{(i)}.$$

- Sub-Component $\mathbf{S}_I \leftarrow \mathbf{S}_I (\mathbf{I} - \frac{\mathbf{w}^T \mathbf{w} \mathbf{S}_T}{\mathbf{w}^T \mathbf{S}_T \mathbf{w}})$

- Projection $\mathbf{Z}_k^p = \sum_{f=f_1}^{f_m} \sum_{c=c_1}^{c_n} \mathbf{w}_p^{c,f} \mathbf{Y}_k^{c,f},$

- Feature Vector $\mathbf{f}_k = \log \left(\frac{\operatorname{diag}(\mathbf{Z}_k \mathbf{Z}_k^T)}{\operatorname{tr}(\mathbf{Z}_k \mathbf{Z}_k^T)} \right)$



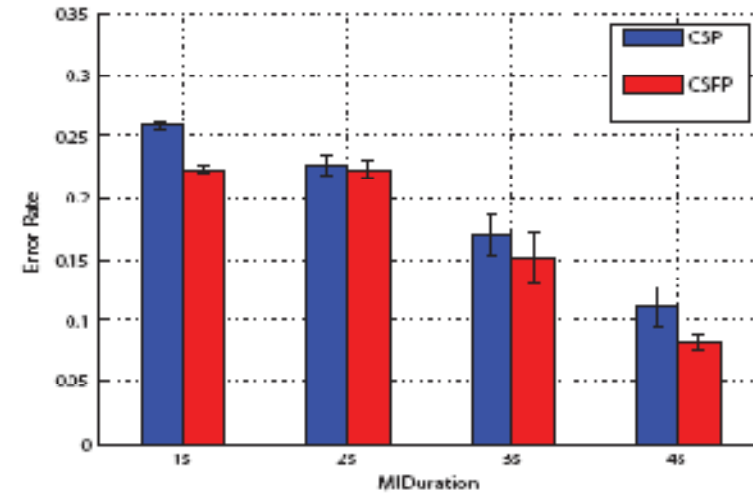
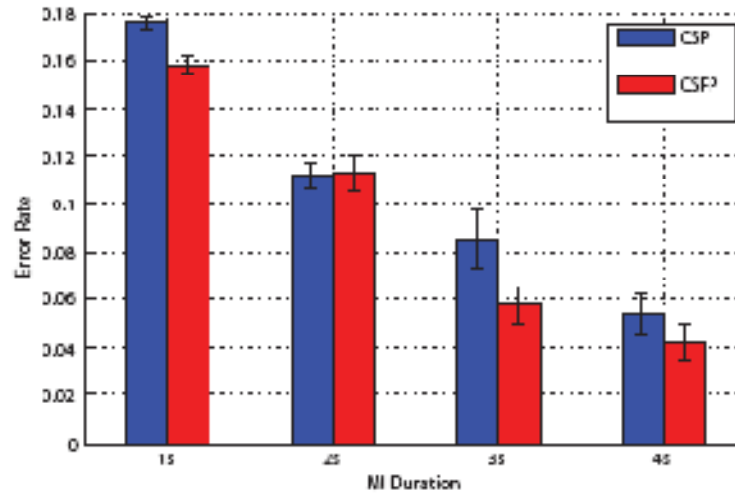


Classification Results:10 cv

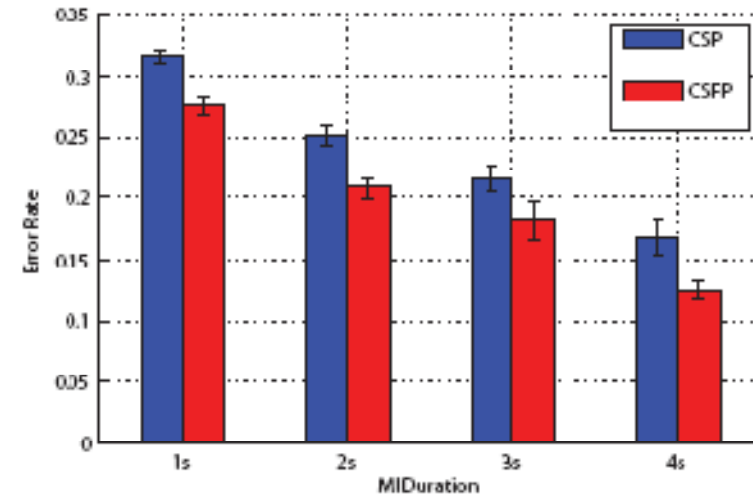
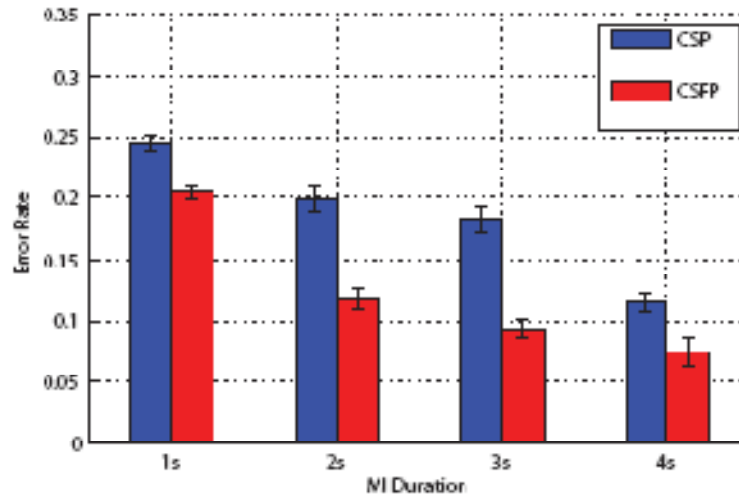
Two Classes

Three Classes

Subject 1

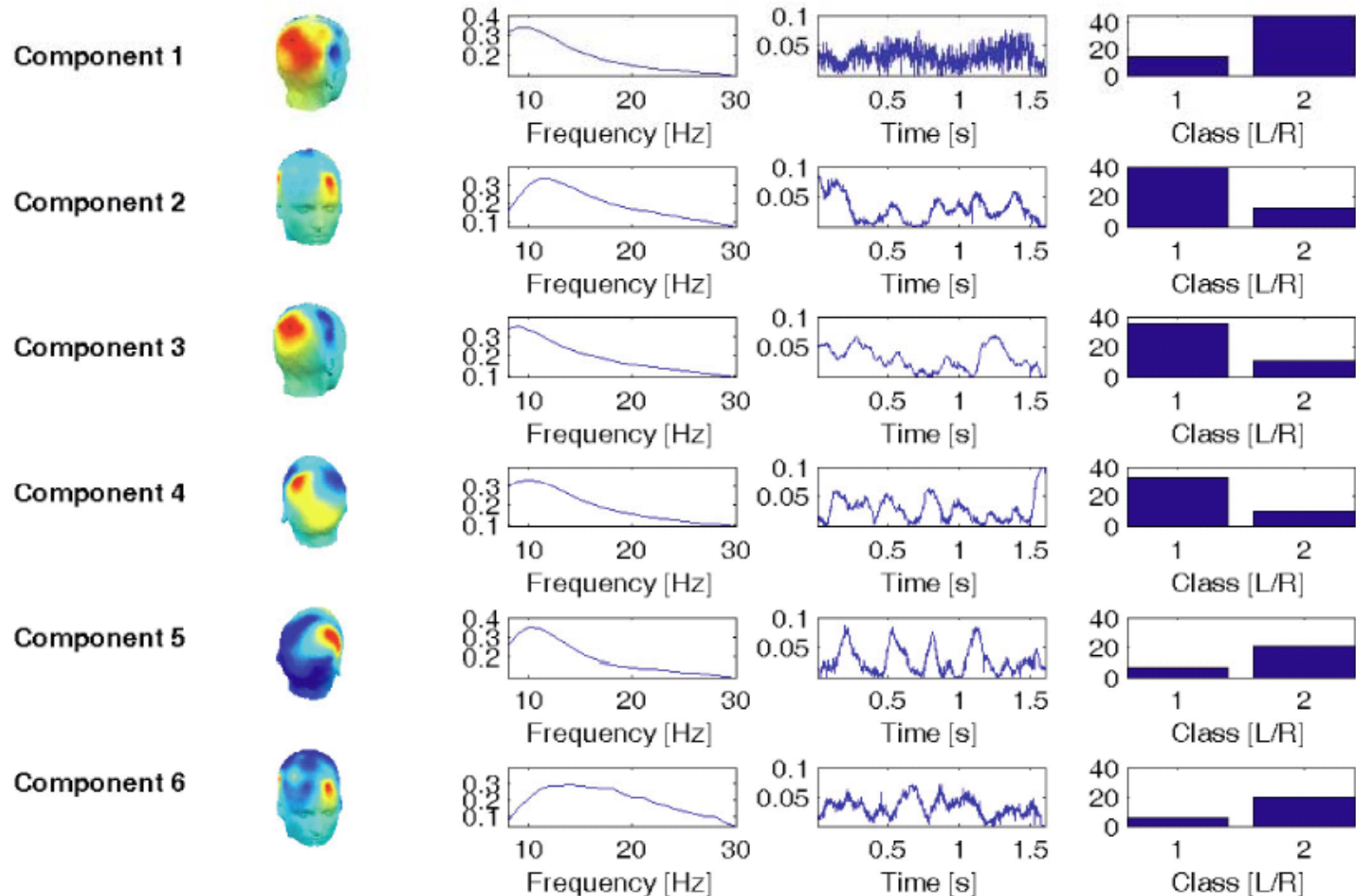


Subject 2



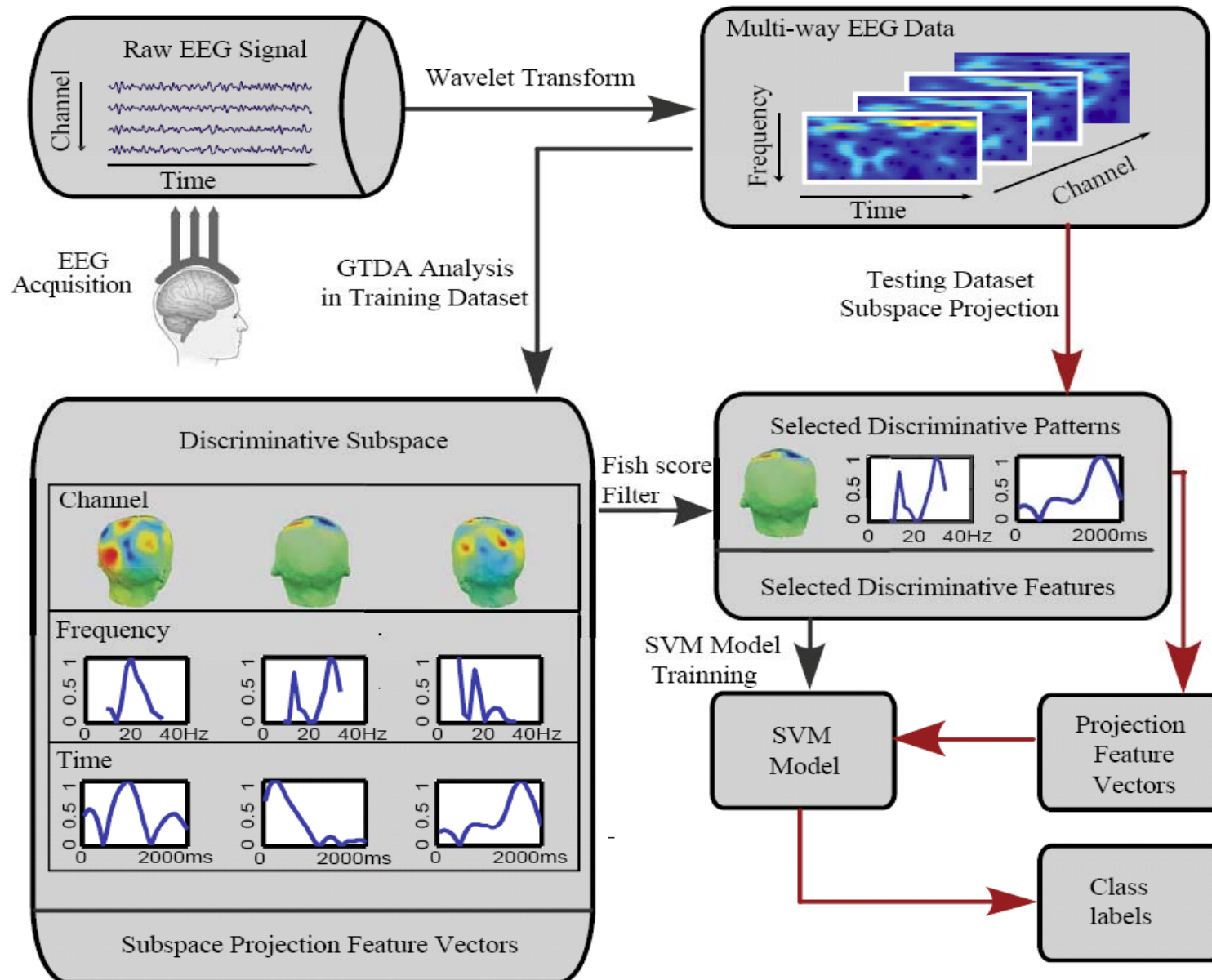


Decomposed Components





Tensor Feature Extraction





Discriminative model

➤ Logistic Regression Model

$$\log \frac{P(y = +1 | \mathcal{X})}{P(y = -1 | \mathcal{X})} = f(\mathcal{X}, \theta) = \mathcal{X} \prod_{d=1}^m \times_d \mathbf{w}_d + b,$$

$$\begin{aligned} \min_{\mathbf{w}_d |_{d=1}^m \in R^{D_d}, b \in R} & \sum_{n=1}^N \log(1 + e^{-y_n f(\mathcal{X}_n, \theta)}) + \sum_{d=1}^m \lambda_d^1 \|\mathbf{w}_d\|^2 + \lambda_d^2 |\mathbf{w}_d| \\ & - \lambda_d^3 (\mathbf{w}_d^T \mathbf{K}_d \mathbf{w}_d), \end{aligned}$$





Common Tensor - CTDA

➤ Tensor Covariance

$$\mathcal{R} = \frac{1}{n} \sum_{i=1}^n [[\mathcal{X}_i \circ \mathcal{X}_i; (M)(M)]]$$

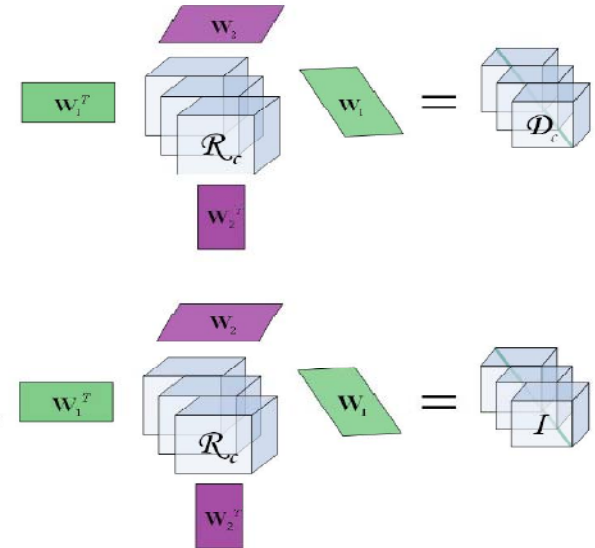
➤ Objective Function

$$\mathcal{R}^{(c)} \times_1 \mathbf{W}_1^{(c)T} \cdots \times_{M-1} \mathbf{W}_{M-1}^{(c)T} \times_M \mathbf{W}_{M-1}^{(c)} \cdots \times_{2(M-1)} \mathbf{W}_1^{(c)} = \mathcal{D}^{(c)}$$

$$\left(\sum_{c=1}^C \mathcal{R}^{(c)} \right) \times_1 \mathbf{W}_1^{(c)T} \cdots \times_{M-1} \mathbf{W}_{M-1}^{(c)T} \times_M \mathbf{W}_{M-1}^{(c)} \cdots \times_{2(M-1)} \mathbf{W}_1^{(c)} = \mathcal{I},$$

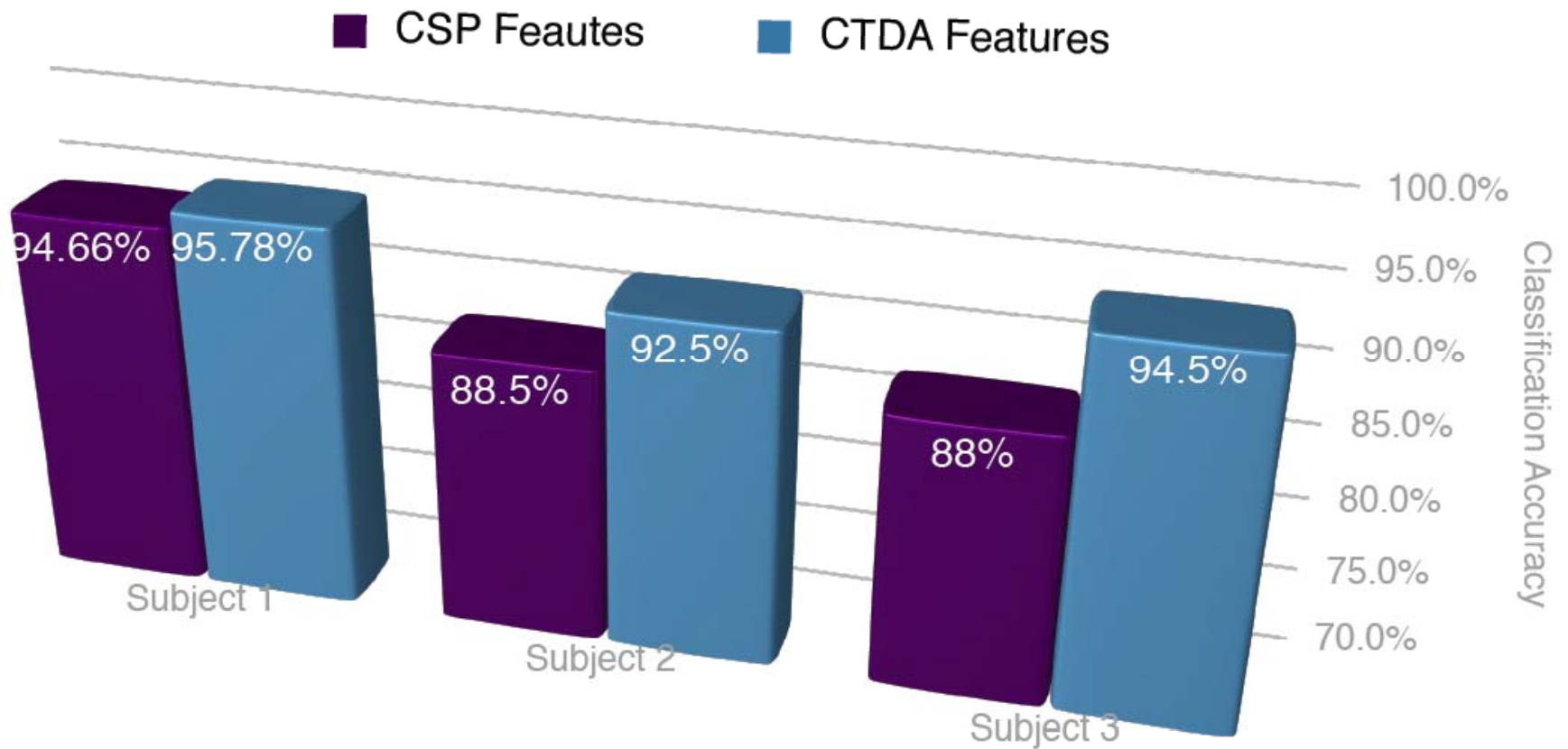
➤ Feature Projection

$$f = \log \left\{ \frac{\text{diag} \left[\text{mat}_M^T \left(\mathcal{X} \prod_{l=1}^{M-1} \times_l \mathbf{W}_l^T \right) \text{mat}_M \left(\mathcal{X} \prod_{l=1}^{M-1} \times_l \mathbf{W}_l^T \right) \right]}{\text{tr} \left[\text{mat}_M^T \left(\mathcal{X} \prod_{l=1}^{M-1} \times_l \mathbf{W}_l^T \right) \text{mat}_M \left(\mathcal{X} \prod_{l=1}^{M-1} \times_l \mathbf{W}_l^T \right) \right]} \right\}$$





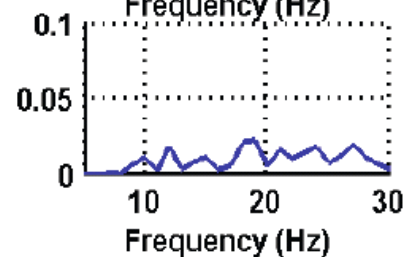
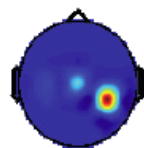
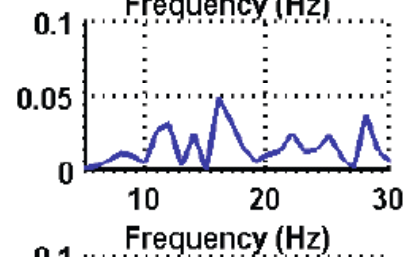
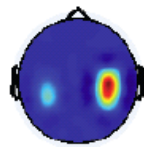
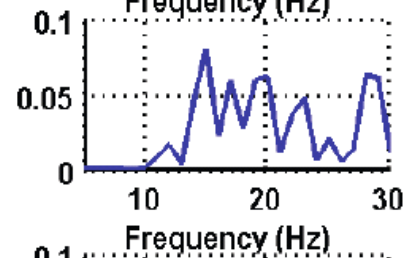
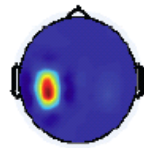
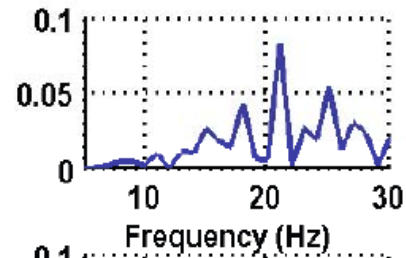
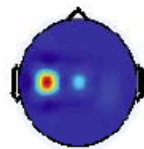
Comparisons: CSP & CTDA





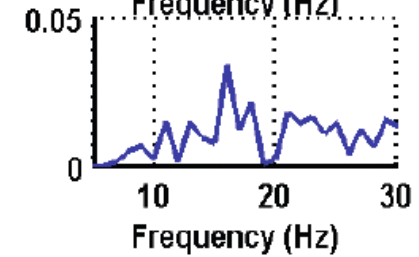
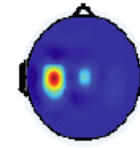
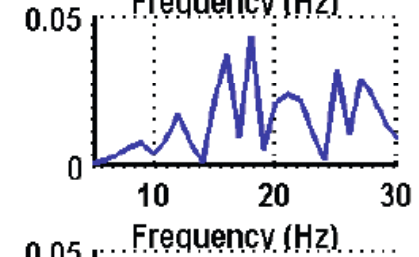
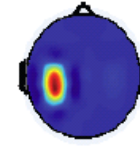
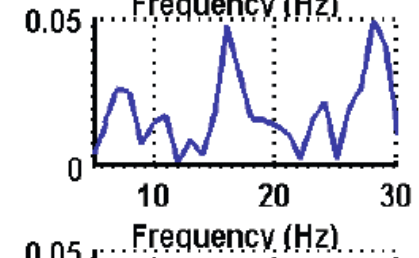
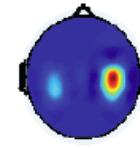
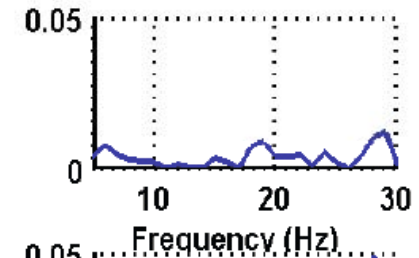
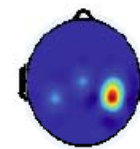
CTDA

First two patterns



(a) Left hand

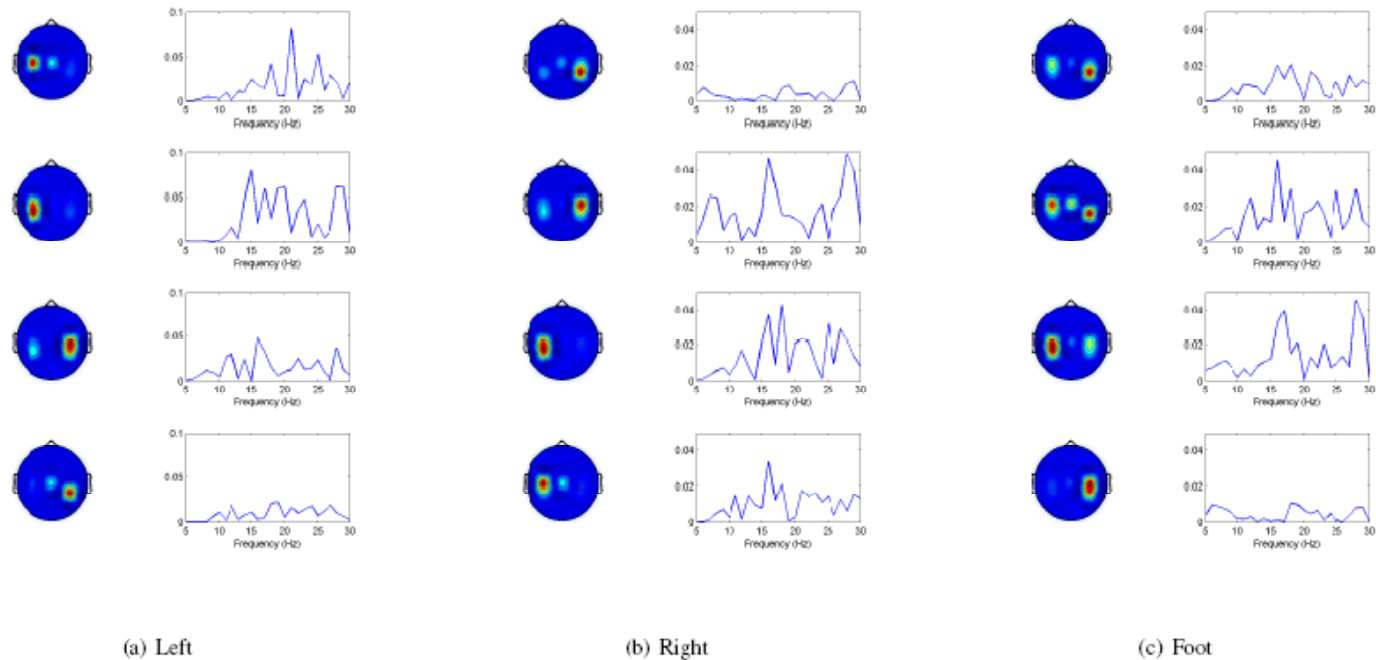
Last two patterns



(b) Right hand



Experiment Results



Projection

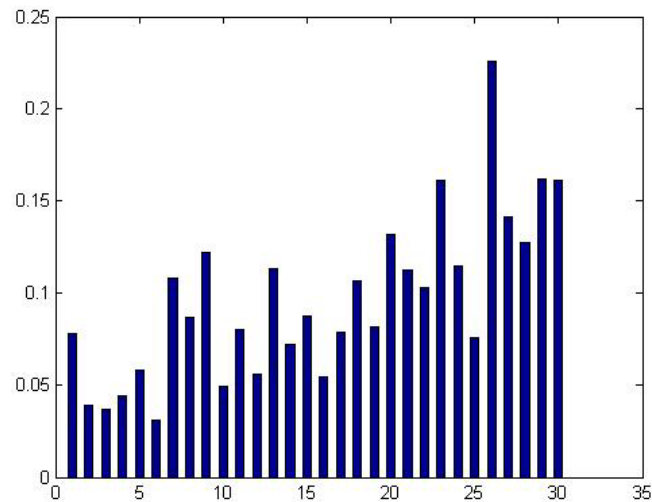
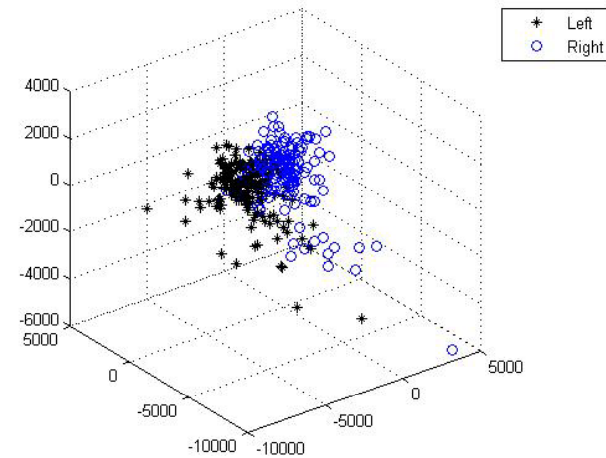
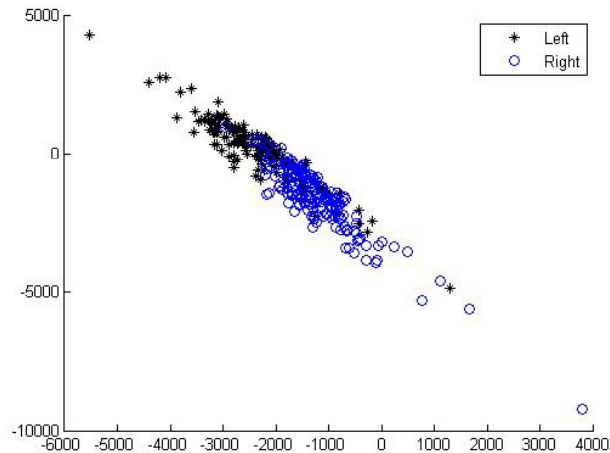
Subjects	2 classes		3 classes	
	CSP	CTDA	CSP	CTDA
S1	94.66±0.84	95.78±0.75	88.95±1.60	91.80±0.57
S2	88.50±0.70	92.50±1.18	83.11±1.39	87.56±0.75
S3	88.00±1.00	94.50±0.67	84.93±0.95	88.33±0.35

Classification
Performance

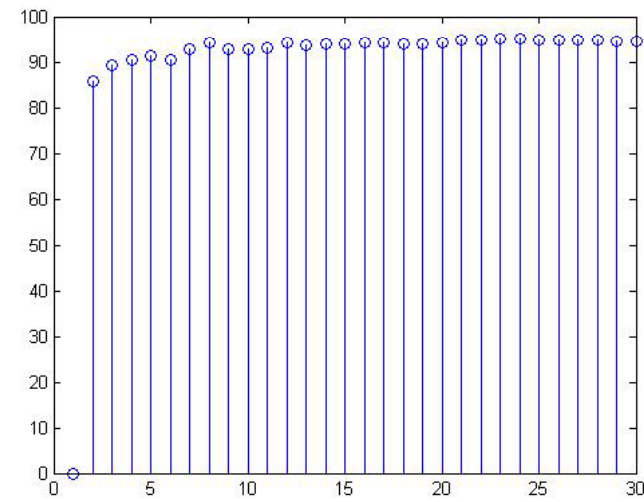
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Classification



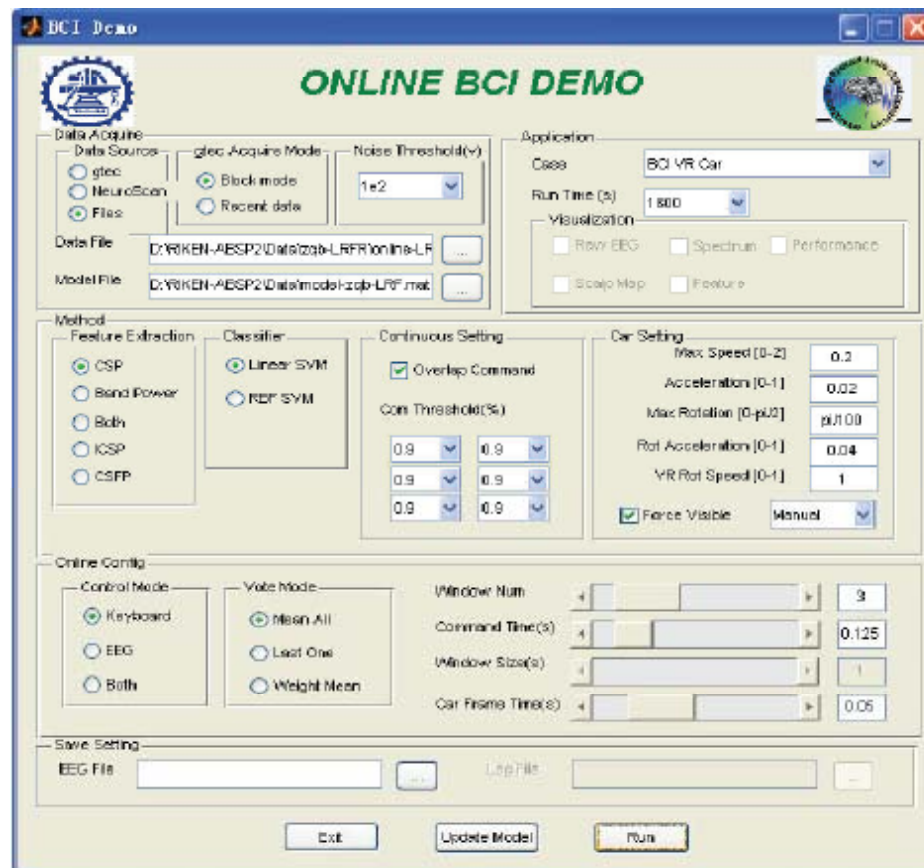
MI between Feature and Class



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Accuracy – Number of features

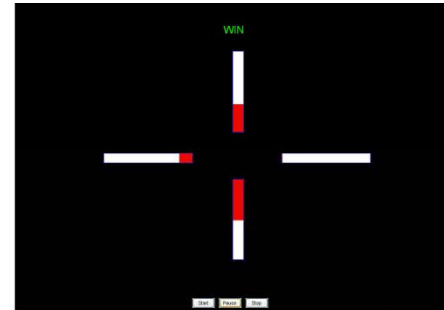
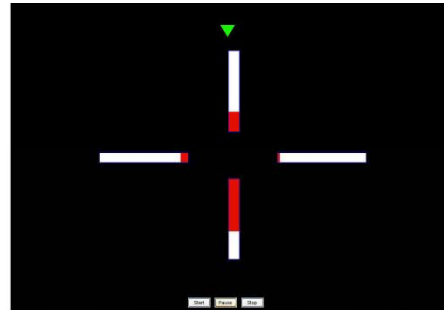
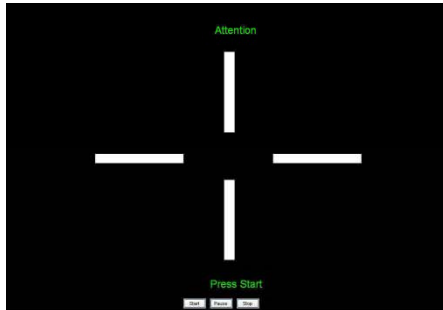


BCI Development Platform





BCI Game



Classification accuracy

受试者	离线分析			在线分析		
	1s	2s	3s	1s	2s	3s
S1	0.78	0.9	0.95	0.62	0.75	0.9
S2	0.88	0.98	1	0.65	0.8	0.93

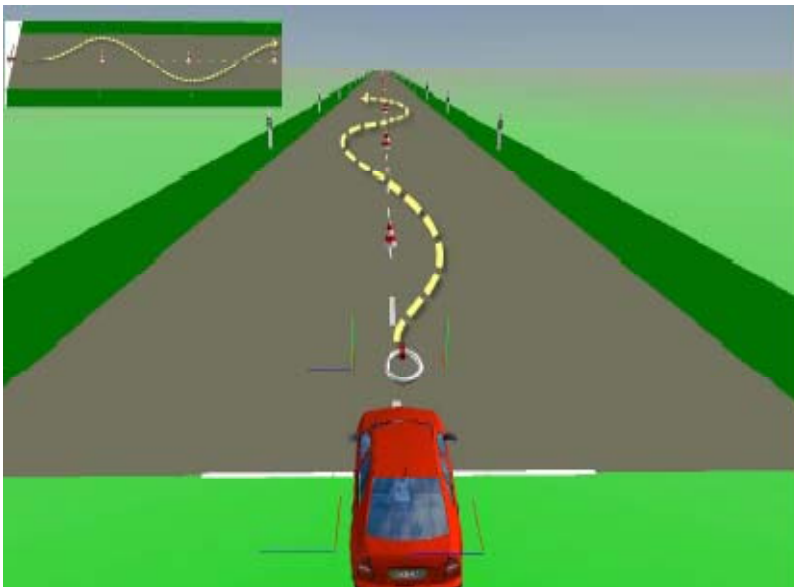




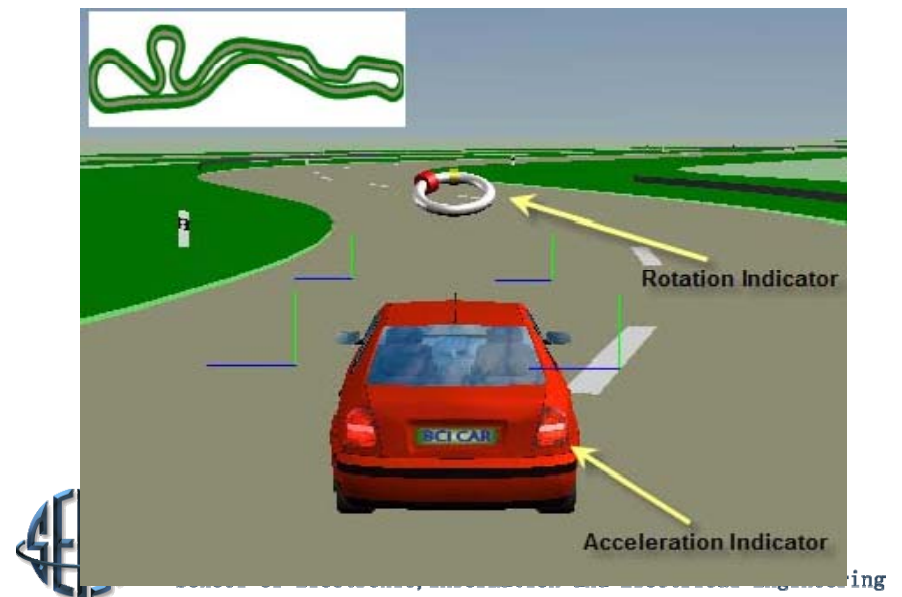
BCI Car Driving System

- Noninvasive, spontaneous and asynchronous
- Two scenarios to test the BCI performance
- Control directions and speed

scenario I

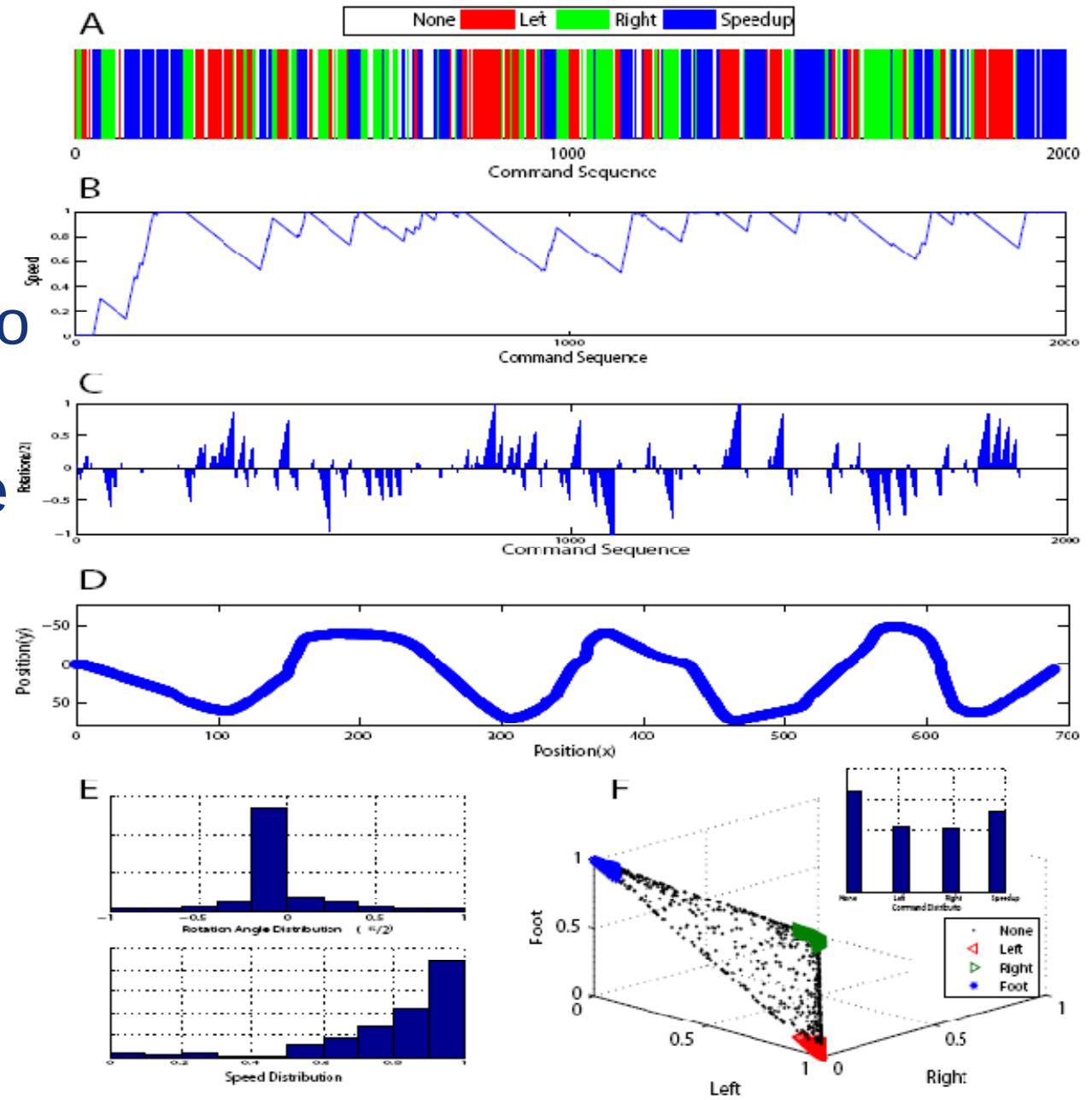


scenario II





- On-line implementation
- No-task state
- Real value control parameter
- Error tolerance





上海交通大学
SHANGHAI JIAO TONG UNIVERSITY

BCI Wheelchair



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School of Electronic, Information and Electrical Engineering



BCI Remote Car Control

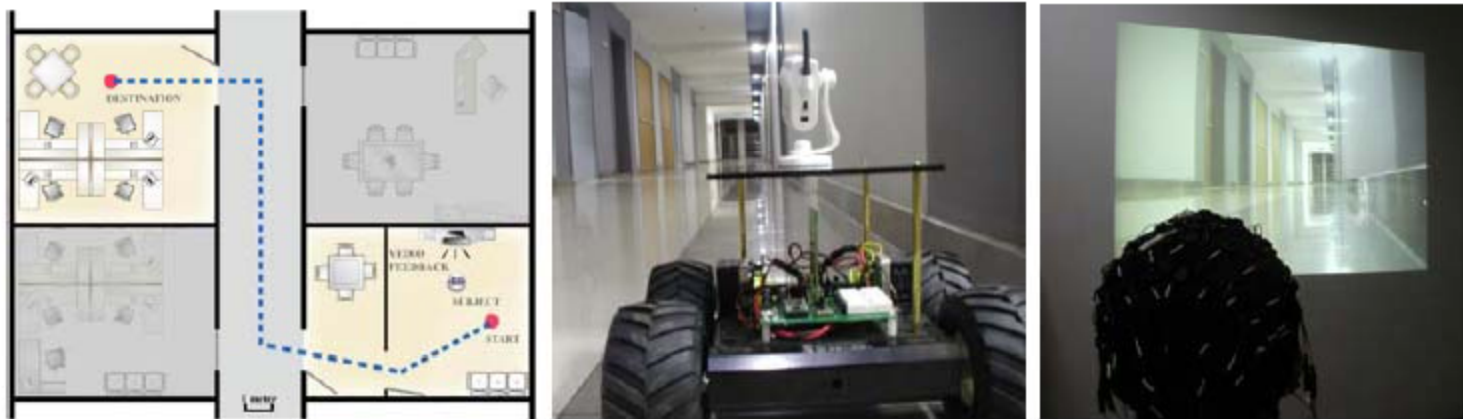
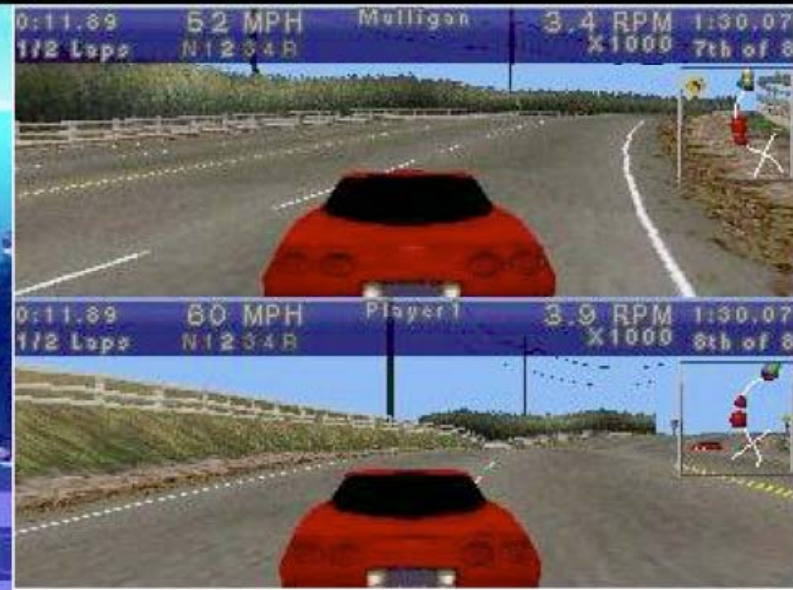
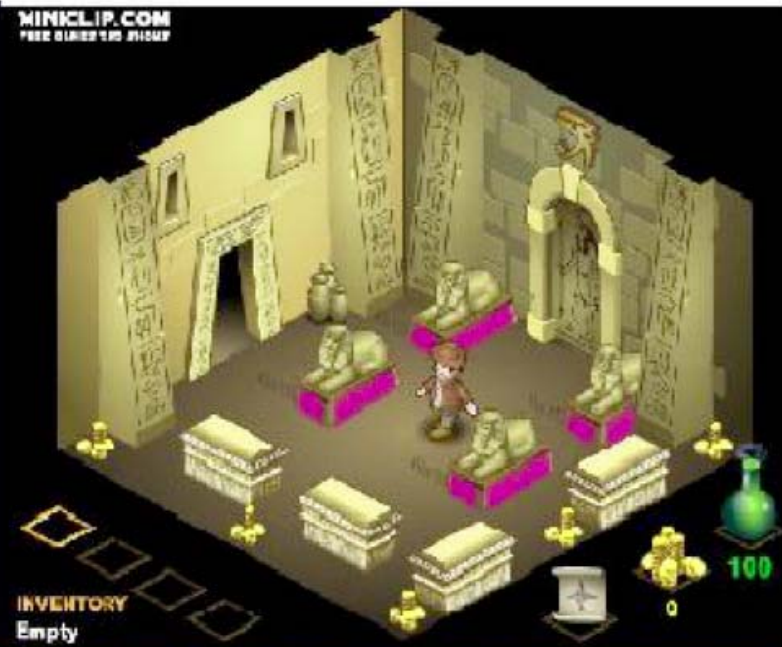


图 4-2 在线远程机械车驾驶







Bilateral Training Framework

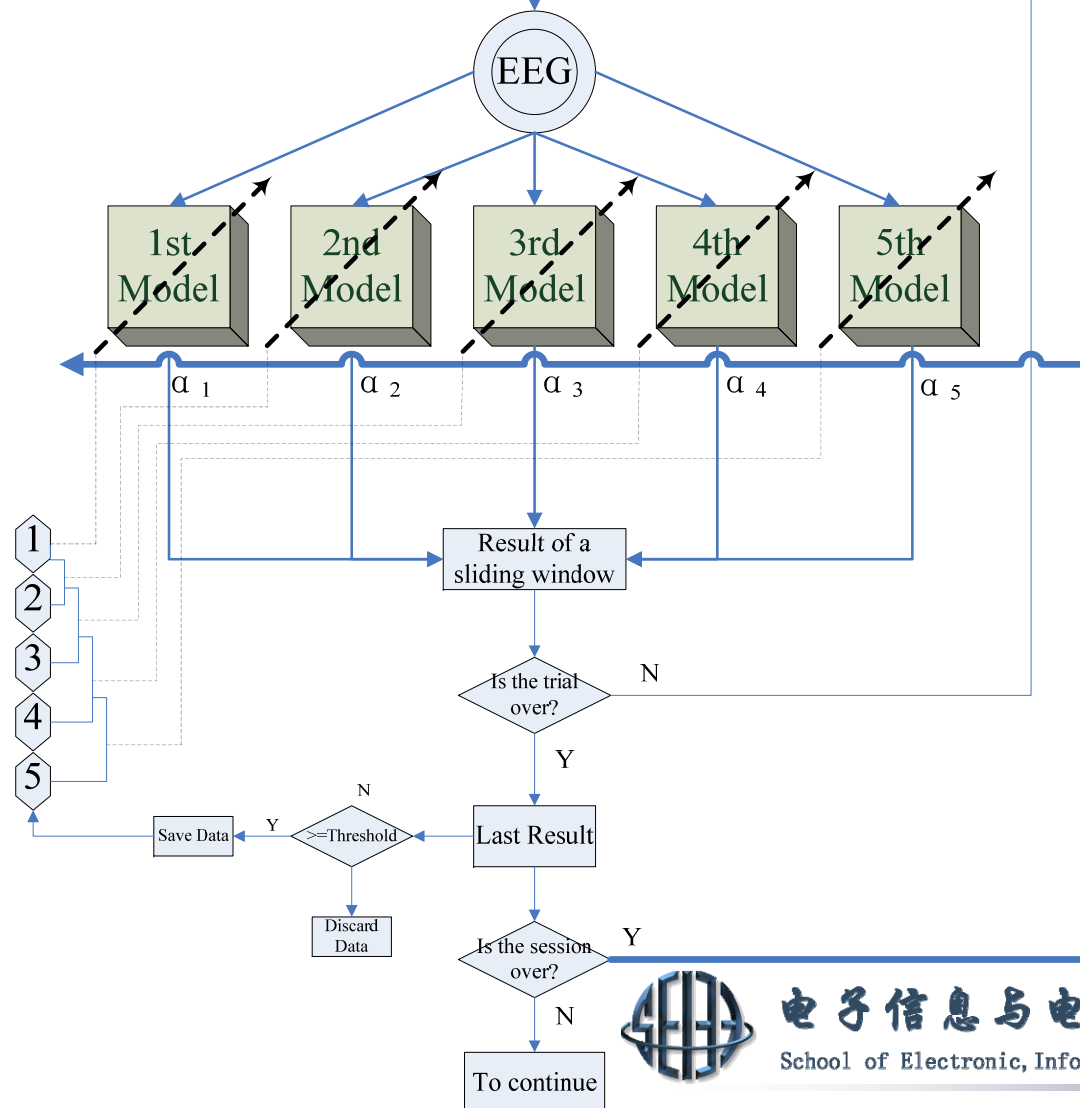


- Sketch map of bilateral training process. Green arrow represents BCI system training. Red arrow represents humans training. Dots mean to continually repeat training over the whole experiment time.





Interaction between humans and BCI system





Latest Demos

- [RIKEN – BCI Control of Wheelchairs\(CCTV\)](#)
- [RIKEN - BCI Control of Wheelchairs\(NHK\)](#)
- [Driving A Car in VR](#)
- BCI Wheelchair ([SJTU](#) / [RIKEN](#) /)
- [BCI Car Racing System](#)
- [BCI Remote Car Control](#)





Related Publications

- Junhua Li and Liqing Zhang, Bilateral Adaptation and Neurofeedback for Brain Computer Interface system, **Journal of Neuroscience Methods** 193: 373–379, (2010)
- Jie Li, Liqing Zhang, Dacheng Tao, Han Sun and Qibin Zhao, A Prior Neurophysiologic Knowledge Free Tensor-based Scheme for Single Trial EEG Classification, **IEEE Transactions on Neural Systems and Rehabilitation Engineering**, 17(2):107-115, 2009
- Jie Li, and Liqing Zhang, Phase Interval Value Analysis for motor imagery task in BCI, **Pattern Recognition Letter**, 2009
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- A. Cichocki, A. Phan, S. Choi, H. Lee, Q. Zhao, L. Zhang, and Y. Li, Noninvasive Brain-Computer Interface: Current Trends and Challenges in Signal Processing - Multiway Array Decompositions, **IEEE Computer**, Vol. 41(10), pp.34-42, October, 2008
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Thanks for Your Attention



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