



Multi-Armed Bandit Algorithms for Personalized Recommendation

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My Research Summary



Chapman & Hall/CRC Data Mining and Knowledge Discovery Series

Music Data Mining

EDITED BY Tao Li Mitsunori Ogihara George Tzanetakis

A CRAPMAN & HALL SOON

DATA MINING Where Theory Meets Practice

数据挖掘的应用与实践 ——大数题时代的案例分析

Mining Mining Motor Network Data

> 国际教授的国际地区2.5家 学講 等 著

Oboulennanes.

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EVENT MINING ALGORITHMS AND APPLICATIONS







Recommender Systems



Outline

- Introduction
- Motivation
- Contextual-free Bandit Algorithms
- Contextual Bandit Algorithms
- Our Recent Studies
 - Ensemble Contextual Bandits for Personalized Recommendation
 - Personalized Recommendation via Parameter-Free Contextual Bandits
- Future Work
- Q&A

What is Personalized Recommendation?

- Personalized Recommendation help users find interesting items based the individual interest of each item.
 - Ultimate Goal: maximize user engagement.

NEWS

PRODUC



What is Cold Start Problem?

- Do not have enough observations for new items or new users.
 - How to predict the preference of users if we do not have data?

- Many practical issues for offline data
 - Historical user log data is biased.
 - User interest may change over time.

Approach: Multi-armed Bandit Algorithm

- A gambler walks into a casino
- A row of slot machines providing a random rewards

Objective: Maximize the sum of rewards(Money)!





- Recommend news based on users' interests.
- Goal: Maximize user's Click-Through-Rate.

110	
0.5.	
World	
Politics	
Tech	
Science	
Health	
Odd News	
Local	
Dear Abby	
Comics	
ABC News	
Katie Couric	
Trending	
Photos	
Recommended Gam	nes

YAHOO!



<page-header><text><text><text><complex-block><complex-block>

Trending News Meadow Walker Empire season 2 Salman Khan iPad Pro Destiny the Taken King

Search News

Search Web

xfinity

Man accused of killing Adrian Peterson's son to stand trial

- There are a bunch of articles in the news pool
- Users come sequentially and ready to be entertained



[1] Zhou Li, "News personalization with Multi-armed bandits".

• At each time, we want to select one article for user.



• Goal: maximum CTR.



Update the model with user's feedback



• Update the model once given the feedback



Update the model once given the feedback



Multi-Armed Bandit (MAB) Definition

The MAB problem is a classical paradigm in Machine Learning in which an online algorithm choses from a set of strategies in a sequence of trials so as to maximize the total payoff of the chosen strategies[1].

Application: Clinical Trial

Two treatments with unknown effectiveness



[1] <u>Einstein, A., B. Podolsky, and N. Rosen, 1935, "Can quantum-mechanical description of physical reality be considered complete?"</u>, Phys. Rev. **47**, 777-780

Web advertising



[1] <u>Tang L, Rosales R, Singh A, et al. Automatic ad format selection via contextual bandits[C]</u>, <u>Proceedings of the 22nd ACM</u> international conference on Conference on information & knowledge management. ACM, 2013: 1587-1594.

Playing Golf with multi-balls



[1] Dumitriu, Ioana, Prasad Tetali, and Peter Winkler. "On playing golf with two balls." *SIAM Journal on Discrete Mathematics* 16.4 (2003): 604-615.

Multi-Agent System

K agents tracking N (N > K) targets:



[1] Ny, Jerome Le, Munther Dahleh, and Eric Feron. "Multi-agent task assignment in the bandit framework." Decision and Control, 2006 45th IEEE Conference on. IEEE, 2006.

Some Jargon Terms[1]

- Arm: one idea/strategy
- Bandit: A group of ideas(strategies)
- Pull/Play/Trial: One chance to try your strategy
- Reward: The unit of success we measure after each pull
- Regret: Performance Metric
- Learning through experimentation



Developing, Deploying, and Debugging

O'REILLY*

John Myles White

K-Armed Bandit



- Each Arm a
 - Wins(reward=1) with fixed(unknown) prob. μ_a
 - Loses(reward=0) with fixed(unknown) prob. $(1 \mu_a)$
- How to pull arms to maximize total reward?(estimate the arm's prob. of winning μ_a)

Model of K-Armed Bandit

- Set of k choices(arms)
- Each choice *a* is associated with unknown probability distribution *P_a* in [0, 1]
- We play the game for *T* rounds
- In each round t:
 - We pick some arm *j*
 - We obtain random sample X_t from P_i
- Goal: maximize $\sum_{t=1}^{T} X_t$ (without known μ_a)
- However, every time we pull some arm *a* we get to learn a bit about μ_a .

Performance Metric: Regret

- Let be μ_a the mean of P_a
- Payoff/reward **best arm**: $\mu^* = max\{ \mu_a | a = 1, ..., k \}$
- Let i₁, ... i_T be the sequence of arms pulled
- Instantaneous regret at time t: $r_t = \mu^* \mu_{a_{it}}$
- Total regret:

• $\boldsymbol{R}_T = \sum_{t=1}^T \boldsymbol{r}_t$

• Typical goal: arm allocation strategy that guarantees :

•
$$\frac{R_T}{T} \to 0$$
 as $T \to \infty$

Allocation Strategies

- If we knew the payoffs, which arm should we pull?
 - **best** arm: $\mu^* = max\{ \mu_a | a = 1, ..., k \}$
- What if we only care about estimating payoff μ_a ?
 - Pick each of **k** arms equally often : $\frac{T}{\nu}$

• Estimate :
$$\widehat{\mu_a} = \sum_{j=1}^{\frac{T}{k}} X_{a,j} / (\frac{T}{k}) \implies \frac{k}{T} \sum_{j=1}^{T/k} X_{a,j}$$

• Total regret:

$$\mathbf{R}_T = \frac{T}{k} \sum_{a=1}^k (\mu^* - \mu_a)$$

 $X_{a,j}$ payoff received when pulling an arm *a* for *j*-th time

Exploitation vs. Exploration

- Tradeoff:
 - Only exploitation(making decisions based on history data), you will have bad estimation for "best" items.
 - Exploitation: Pull an arm currently having the highest estimate
 - Only exploration(gathering data about arm payoffs), you will have low user's engagement.
 - Exploration: Pull an arm never pulled before



Algorithm to Exploration & Exploitation



Wynn P. On the convergence and stability of the epsilon algorithm[J]. SIAM Journal on Numerical Analysis, 1966, 3(1): 91-122.
Auer P, Cesa-Bianchi N, Fischer P. Finite-time analysis of the multi-armed bandit problem[J]. Machine learning, 2002, 47(2-3): 235-256.

[3] <u>Agrawal S, Goyal N. Analysis of Thompson sampling for the multi-armed bandit problem[J]. arXiv preprint arXiv:1111.1797, 2011.</u>

[4] Li, Lihong, et al. "A contextual-bandit approach to personalized news article recommendation." *Proceedings of the 19th international conference on World wide web*. ACM, 2010.

Contextual and Contextual- Free

- Contextual
 - Every round receives context
 - User features, arm/item features (e.g., articles reviewed before) at each trial
 - Select items to users based on contextual information about the user and the items
 - Bandits with covariate, bandits with side information, associative bandits
- Contextual-free
 - Both the arm set and contexts are constant at every trial

ε-Greedy Algorithm

It tries to be fair to the two opposite goals of exploration(with prob. ε) and exploitation(1-ε) by using a mechanism: flips a coin.



ε-Greedy Algorithm

- For t=1:T
 - Set $\varepsilon_t = O\left(\frac{1}{t}\right)$
 - With prob. *ɛ_t*: Explore by picking an arm chosen uniformly at random
 - With prob. 1-ε_t: Exploit by picking an arm with highest empirical mean payoff
- Theorem [Auer et al. '02]
 - For suitable choice of ε_t it holds that

$$R_T = O(k \log T) \Rightarrow \frac{R_T}{T} = O\left(\frac{k \log T}{T}\right) \to 0$$

Issues with ε-Greedy Algorithm

- Not elegant" : Algorithm explicitly distinguishes between exploration and exploitation
- More importantly: Exploration makes suboptimal choices(since it picks any arm equally likely)
- Idea: When exploring/exploiting we need to compare arms.

Example : Comparing Arms

- Suppose we have done experiments :
 - Arm 1: 1001110001
 - Arm 2: 1
 - Arm 3: 11010011 11
- Mean arm values:
 - Arm 1: 5/10 Arm 2: 1 Arm 3: 7/10
- Which arm would you choose next?
- Idea: Not only look at the mean but also the confidence!

Confidence Intervals

- A confidence interval is a range of values within which we are sure the mean lies with a certain probability
 - We could believe μ_a is within [0.2,0.5] with probability 0.95
 - If we would have tried an action less often, our estimated reward is less accurate so the confidence interval is larger
 - Interval shrinks as we get more information (try the action more often)

Confidence Based Selection

- Assuming we know the confidence intervals
- Then, instead of trying the action with the highest mean we can try the action with the highest upper bound on its confidence interval.



Confidence intervals vs Sampling times



The estimation of confidence becomes smaller as the number of pulling times increases.

Calculating Confidence Bounds

- Suppose we fix arm a:
 - Let r_{a,1} ... r_{a,m} be the payoffs of arm a in the first m trials

• $r_{a,1} \dots r_{a,m}$ are i.i.d. taking values in [0,1]

- Our estimate : $\widehat{\mu_{a,m}} = \frac{1}{m} \sum_{j=1}^{m} r_{a,j}$
- Want to find b such that with high probability

 $|\mu_a - \widehat{\mu_{a,m}}| \le b$ (want b to be as small as possible)

• Goal : Want to bound $\mathbf{P}(|\mu_a - \widehat{\mu_{a,m}}| \le b)$
UCB1 Algorithm

- UCB1 (Upper confidence sampling) algorithm
 - Let $\widehat{\mu_1} \dots = \widehat{\mu_k} = 0$ and $m_1 = \dots = m_k = 0$
 - $\widehat{\mu_a}$ is our estimate of payoff of arm a
 - m_a is the number of pulls of arm a so far.
 - For t = 1 : T
 - For each arm *a* calculate UCB(a) = $\hat{\mu}_a + \alpha \sqrt{\frac{2\ln t}{m_a}}$
 - Pick arm $j = argmax_a UCB(a)$
 - Pull arm j and observe y_t
 - $m_j = m_j + 1$ and $\hat{\mu}_j = 1/m_j(y_t + (m_j 1)\hat{\mu}_j)$

Hoeffding's Inequality

Hoeffding's Inequality

- Hoeffding's inequality bounds $P(|\mu_a \widehat{\mu_{a,m}}| \le b)$
 - Let X₁ ... X_m be i.i.d. rnd. vars. taking values in [0,1]
 - Let $\mu = E[X]$ and $\widehat{\mu_m} = \frac{1}{m} \sum_{\ell=1}^m X_\ell$

• Then: $P(|\mu - \widehat{\mu_m}| \ge b) \le 2 \exp(-2b^2m) = \delta$

- To find out the confidence interval *b* (for a given confidence level δ) we solve:
 - $2e^{-2b^2m} \leq \delta$ then $-2b^2m \leq \ln(\delta/2)$



[1] CS246 Mining Massive Data Sets 2015, Stanford University

UCB1 Algorithm: Discussion

- Confidence interval grows with the total number of actions t we have taken
- But Shrinks with the number of times m_a we have tried arm a
- This ensures each arm is tried infinitely often but still balances exploration and exploitation
- α plays the role of δ : $\alpha = f\left(\frac{2}{\delta}\right) = 1 + \sqrt{\frac{\ln(2/\delta)}{2}}$
- For each arm *a* calculate UCB(a) = $\widehat{\mu}_a + \alpha \sqrt{\frac{2\ln t}{m_a}}$
 - Pick arm $j = argmax_a UCB(a)$
 - Pull arm j and observe y_t
 - $m_j = m_j + 1$ and $\hat{\mu}_j = 1/m_j(y_t + (m_j 1)\hat{\mu}_j)$

UCB1 Algorithm Performance

• Theorem [Auer et al. 2002]

- Suppose optimal mean payoff is $\mu^* = \max_a \mu_a$
- And for each arm let $\Delta_a = \mu^* \mu_a$
- Then it holds that

$$E[R_T] = \begin{bmatrix} 8 & \sum_{a:\mu_a < \mu^*} \frac{\ln T}{\Delta_a} \end{bmatrix} + \left(1 + \frac{\pi^2}{3}\right) \left(\sum_{i=a}^k \Delta_a\right)$$
$$\frac{O(k \ln T)}{O(k)}$$

• So, we get
$$O\left(\frac{R_T}{T}\right) = k \frac{\ln T}{T}$$

Quick Summary

• Multi-armed bandit problem as a formalization the exploration-exploitation tradeoff

- Simple algorithms for context-free bandits are able to achieve no regret (in the limit)
 - $-\varepsilon$ -Greedy
 - UCB (Upper Confidence Sampling)

Contextual Bandits

- Contextual bandit algorithm in round t
 - Algorithm observers user u_t and a set A of arms together with their features $x_{t,a}$ (context)
 - Based on payoffs from previous trials, algorithm chooses arm $a \in A$ and receives payoff $r_{t,a}$
 - Algorithm improves arm selection strategy with each observation(x_{t,a}, a, r_{t,a})

- Contextual bandit algorithm in round t
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 Expectation of reward of each arm is modeled as a linear function of the context.

 $oldsymbol{ heta}_a^*$ is the unknown coefficient vector we **aim to learn**

Payoff of arm a :
$$E[r_{t,a}|x_{t,a}] = [x_{t,a}]^T \theta_a^*$$

 $x_{t,a}$ is a **d**-dimensional feature vector

 The goal is to minimize regret, defined as the difference between the expectation of the reward of best arms and the expectation of the reward of selected arms.

$$R_t(T) \stackrel{\text{\tiny def}}{=} E\left[\sum_{t=1}^T r_{t,a_t^*}\right] - E\left[\sum_{t=1}^T r_{t,a_t}\right]$$

•
$$E[r_{t,a}|x_{t,a}] = [x_{t,a}]^T \theta_a^*$$

• How to estimate θ_a ?
• Linear regression solution to θ_a is
 $\widehat{\theta_a} = argmin_{\theta} \sum_{m \in D_a} ([x_{t,a}]^T \theta_a - b_a^{(m)})^2$
We can get:
 $\widehat{\theta_a} = (D_a^T D_a + I_d)^{-1} D_a^T b_a$
 D_a is a m × d matrix of m
training inputs $[x_{t,a}]$
 b_a is a m-dimension vector of
responses to $a(\text{click/no-click})$

Using similar techniques as we used for UCB

$$|[x_{t,a}]^T \widehat{\boldsymbol{\theta}_a} - \mathbb{E}[r_{t,a} | x_{t,a}]| \leq \alpha \sqrt{[x_{t,a}]^T (\boldsymbol{D}_a^T \boldsymbol{D}_a + \boldsymbol{I}_d)^{-1} x_{t,a}}$$
$$\alpha = 1 + \sqrt{\ln(2/\delta)/2}$$

• For a given context, we estimate the reward and the confidence interval.

$$\underline{a_{t} \stackrel{\text{def}}{=} argmax_{a \in A_{t}}([x_{t,a}]^{T}\widehat{\boldsymbol{\theta}_{a}} + \alpha \sqrt{[x_{t,a}]^{T}(\boldsymbol{D}_{a}^{T}\boldsymbol{D}_{a} + \boldsymbol{I}_{d})^{-1}x_{t,a})}}_{\text{Estimated }\mu_{a}}$$

- Initialization:
 - For each arm *a*:

•
$$A_a = I_d$$

•
$$b_a = [0]_d$$

- Online algorithm:
 - For t=[1:T]:
 - Observe features for all arms $a : x_{t,a} \in \mathbb{R}^d$
 - For each arm a :

•
$$\theta_a = A_a^{-1} b_a$$
 //regression coefficients

•
$$p_{t,a} = [x_{t,a}]^T \theta_a + \alpha \sqrt{[x_{t,a}]^T A_a^{-1} x_{t,a}}$$

- Choose arm $a_t = argmax_a p_{t,a}$ //choose arm
- $A_{a_t} = A_{a_t} + x_{t,a_t} [x_{t,a_t}]^T$ //update A for the chosen arm a_t
- $b_{a_t} = b_{a_t} + r_t x_{t,a_t}$ //update b for the chosen arm a_t

$$A_a \stackrel{\text{\tiny def}}{=} \boldsymbol{D}_a^T \boldsymbol{D}_a + \boldsymbol{I}_d$$

//identity matrix d ×d //vector of zeros

Different between UCB1 and LinUCB

- UCB1 directly estimates µ_a through experimentation (without any knowledge about arm a)
- LinUCB estimates μ_a by regression $\mu_a = [x_{t,a}]^T \boldsymbol{\theta}_a^*$
 - The hope is that we will be able to learn faster as we consider the context x_a(user, ad) of arm a
 - $\boldsymbol{\theta}_{\boldsymbol{a}}^*$ unknown coefficient vector we aim to learn

LinUCB: Discussion

- LinUCB computational complexity is
 - Linear in the number of arms and
 - At most cubic in the number of features
- LinUCB works well for a dynamic arm set(arms come and go)
 - For example, in news article recommendation, for instance, editors add/remove articles to/from a pool

Thompson Sampling

- A simple natural Bayesian heuristic
 - Maintain a belief(distribution) for the unknown parameters
 - Each time, pull arm *a* and observe a reward *r*
- Initialize priors using belief distribution
 - For t=1:T:
 - Sample random variable X from each arm's belief distribution
 - Select the arm with largest X
 - Observe the result of selected arm
 - Update prior belief distribution for selected arm

Simple Example

- Coin toss: x ~ Bernoulli(θ)
- Let's assume that
 - $\theta \sim \text{Beta}(\alpha_H, \alpha_T)$

•
$$\mathsf{P}(\theta) \propto \theta^{\alpha_H - 1} (1 - \theta)^{\alpha_T - 1}$$

Prior

$$P(\theta|X) = \frac{P(X|\theta)P(\theta)}{\Sigma_{\theta}P(X|\theta)}$$
The prior is conjugate!

TE HERE

Universal Uclick/ooco

Beta distribution

- Theorem [Emilie et al. 2012]
 - Initially assumes arm *i* with prior Beta(1,1) on μ_i
 - $S_i = #$ "Success", $F_i = #$ "Failure"

Algorithm 1: Thompson Sampling for Bernoulli bandits

```
\begin{array}{l} S_i = 0, F_i = 0.\\ \textbf{foreach} \ t = 1, 2, \dots, \textbf{do}\\ & | \quad \text{For each arm } i = 1, \dots, N, \, \text{sample } \theta_i(t) \, \text{from the Beta}(S_i + 1, F_i + 1) \, \text{distribution.}\\ & \text{Play arm } i(t) := \arg \max_i \theta_i(t) \, \text{and observe reward } r_t.\\ & \text{If } r = 1, \, \text{then } S_i = S_i + 1, \, \text{else } F_i = F_i + 1.\\ & \textbf{end} \end{array}
```

 This posterior distribution could then be used as the prior for more samples, with the hyperparameters simply adding each extra piece of information as it comes.

Initialization



- For each round:
 - Sample random variable X from each arm's Beta Distribution



- For each round:
 - Sample random variable X from each arm's Beta Distribution
 - Select the arm with largest X



- For each round:
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Our Recent Research Studies

• Ensemble Contextual Bandits for Personalized Recommendation (RecSys 2014)

 Parameter-free Contextual Bandits for Personalized Recommendation (SIGIR 2015)

Ensemble Contextual Bandits for Personalized Recommendation



[1] Tang, Liang, et al. "Ensemble contextual bandits for personalized recommendation." *Proceedings of the 8th ACM Conference* on Recommender systems. ACM, 2014.

Problem Statement

- Problem Setting: have many different recommendation models (or policies):
 - Different CTR Prediction Algorithms.
 - Different Exploration-Exploitation Algorithms.
 - Different Parameter Choices.
- No data to do model validation
- Problem Statement: how to build an ensemble model that is close to the best model in the cold start situation ?

How Ensemble?

- Classifier ensemble method does not work in this setting
 - Recommendation decision is NOT purely based on the predicted CTR.
- Each individual model only tells us:
 - Which item to recommend.

Not appropriate to adopt majority voting or consensus prediction as the ensemble

Ensemble Method

- Our Method:
 - Allocate recommendation chances to individual models.
- Problem:
 - Better models should have more chances.
 - We do not know which one is good or bad in advance.
 - Ideal solution: allocate all chances to the best one.

Current Practice: Online Evaluation (or A/B testing)

- Let $\pi_1, \pi_2 \dots \pi_m$ be the individual models.
 - Deploy $\pi_1, \pi_2 \dots \pi_m$ into the online system at the same time.
 - Dispatch a small percent user traffic to each model.
 - After a period, choose the model having the best CTR as the production model.

Current Practice: Online Evaluation (or A/B testing)

- Let $\pi_1, \pi_2 \dots \pi_m$ be the individual models.
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 - Dispatch a small percent user traffic to each model.
 - After a period, choose the model having the best CTR as the production model.

If we have too many models, this will hurt the performance of the online system.

Our Idea 1 (HyperTS)

- The CTR of model π_i is a random unknown variable, R_i .
- Goal:
 - maximize $\frac{1}{N} \bigoplus_{t=1}^{N} r_t \quad CTR \text{ of our ensemble model}$ $r_t \text{ is a random number drawn from } R_{s(t)}, s(t)=1,2,..., \text{ or } m.$ For each t=1,...,N, we decide s(t).
- Solution:
 - Bernoulli Thompson Sampling (flat prior: beta(1,1)).
 - $\pi_1, \pi_2 \dots \pi_m$ are bandit arms.

No tricky parameters

In memory, we keep these estimated CTRs for $\pi_1, \pi_2 \dots \pi_{m_1}$





A user visit

0

Estimated CTRs







Two-Layer Decision



Our Idea 2 (HyperTSFB)

- Limitation of Previous Idea:
 - For each recommendation, user feedback is used by only one individual model (e.g., π_k).
- Motivation:
 - Can we update all R₁, R₂, ..., R_m by every user feedback?
 (Share every user feedback to every individual model).

Our Idea 2 (HyperTSFB)

- Assume each model can output the probability of recommending any item given x_t.
 - E.g., for deterministic recommendation, it is 1 or 0.
- For a user visit **x**_t:
 - π_k is selected to perform recommendation (*k*=1,2,..., or *m*).
 - Item A is recommended by π_k given \mathbf{x}_t .
 - Receive a user feedback (click or not click), r_t.
 - Ask every model π₁, π₂ ... π_m, what is the probability of recommending A given x_t.
Our Idea 2 (HyperTSFB)

- Assume each model can output the probability of recommending any item given x_t.
 - E.g., for deterministic recommendation, it is 1 or 0.
- For a user visit **x**_t:
 - π_k is selected to perform
 - Item A is recommended
 - Receive a user feedback (click or not click), r_t
 - Ask every model $\pi_1, \pi_2 \dots \pi_m$, what is the probability of recommending A given $\mathbf{x}_{t.}$

Estimate the CTR of $\pi_1, \pi_2 \dots \pi_m$ (Importance Sampling)

Experimental Setup

Experimental Data

- Yahoo! Today News data logs (randomly displayed).
- KDD Cup 2012 Online Advertising data set.

Evaluation Methods

- Yahoo! Today News: *Replayer* (see <u>Lihong Li et. al's WSDM</u> <u>2011 paper</u>).
- KDD Cup 2012 Data: Simulation by a Logistic Regression Model.

Comparative Methods

- CTR Prediction Algorithm
 - Logistic Regression
- Exploitation-Exploration Algorithms
 - Random, ε-greedy, LinUCB, Softmax, Epoch-greedy, Thompson sampling
- HyperTS and HyperTSFB

Results for Yahoo! News Data

Every 100,000 impressions are aggregated into a bucket.



Results for Yahoo! News Data (Cont.)



Conclusions

- The performance of baseline exploitation-exploration algorithms is very sensitive to the parameter setting.
 - In cold-start situation, no enough data to tune parameter.
- HyperTS and HyperTSFB can be close to the optimal baseline algorithm (No guarantee be better than the optimal one), even though some bad individual models are included.
- For contextual Thompson sampling, the performance depends on the choice of prior distribution for the logistic regression.
 - For online Bayesian learning, the posterior distribution approximation is not accurate(cannot store the past data).

Personalized Recommendation via Parameter-Free Contextual Bandits



[1] Tang, Liang, et al. "Personalized recommendation via parameter-free contextual bandits." *Proceedings of the 38th International* ACM SIGIR Conference on Research and Development in Information Retrieval. ACM, 2015.

How to Balance Tradeoff

- Performance is mainly determined by the tradeoff. Existing algorithms find the tradeoff by user input parameters and data characteristics (e.g., variance of the estimated reward).
- Existing algorithms are all parameter-sensitive.



Chicken-and-Egg Problem for Existing Bandit Algorithms

- Why we use bandit algorithms?
 - Solve the cold start problem (No enough data for estimating user preferences).
- How to find the best input parameters?
 - Tune the parameters online or offline.

if you already have the data or online traffic to tune the parameters, why do you need bandit algorithms?

Our Work

- Parameter-free:
 - It can find the tradeoff by data characteristics automatically.
- Robust:
 - Existing algorithm can have very bad performance if the input parameter is not appropriate.

Solution

- Thompson Sampling
 - Randomly selecting a model coefficient vector from posterior distribution and find the "best" item.
 - Prior is the input parameter for computing posterior.
- Non-Bayesian Thompson Sampling (Our Solution)
 - Randomly selecting a bootstrap sample to find the MLE of model coefficient and find the "best" item.
 - Bootstrapping has no input parameter.

Bootstrap Bandit Algorithm



Online Bootstrap Bandits

- Why Online Bootstrap?
 - Inefficient to generate a bootstrap sample for each recommendation.
- How to online bootstrap?
 - Keep the coefficient estimated by each bootstrap sample in memory.
 - No need to keep all bootstrap samples in memory.
 - When a new data arrives, incrementally update the estimated coefficient for each bootstrap sample [1].

[1] <u>N. C. Oza and S. Russell. Online bagging and boosting. In IEEE international conference on Systems, man and cybernetics, volume 3, pages 2340–2345, 2005.</u>

Experiment Data

- Two public data sets
 - News recommendation data (Yahoo! Today News)
 - News displayed on the Yahoo! Front Page from Oct. 2nd, 2011 to Oct. 16th 2011.
 - 28,041,015 user visit events.
 - 136 dimensions of feature vector for each event.
 - Online advertising data (KDD Cup 2012, Track 2)
 - The data set is collected by a search engine and published by KDD Cup 2012.
 - 1 million user visit events.
 - 1,070,866 dimensions of the context feature vector.

Offline Evaluation Metric and Methods

- Setup
 - Overall CTR (average reward of a trial).
- Evaluation Method
 - The experiment on Yahoo! Today News is evaluated by the replay method [1].
 - The reward on KDD Cup 2012 AD data is simulated with a weight vector for each AD [2].

[1] L. Li, W. Chu, J. Langford, and X. Wang. Unbiased offline evaluation of contextual-bandit-based news article recommendation algorithms. In WSDM, pages 297–306, 2011.

[2] O. Chapelle and L. Li. An empirical evaluation of thompson sampling. In NIPS, pages 2249–2257, 2011.

Experimental Methods

- Our method
 - Bootstrap(B), where B is the number of bootstrap samples.
- Baselines
 - Random: it randomly selects an arm to pull.
 - Exploit: it only consider the exploitation without exploration.
 - ε -greedy(ε): ε is the probability of exploration.
 - LinUCB(α): it pulls the arm with largest score defined by the parameter
 α
 - $TS(q_0)$: Thompson sampling with logistic regression, where q_0^{-1} is the prior variance, 0 is the prior mean.
 - TSNR(q₀): Similar to TS(q₀), but the logistic regression is not regularized by the prior.

Experiment(Yahoo! News Data)

• All numbers are relative to the random model.

Algorithm	Cold Start				Warm Start			
\frown	mean	std	min	max	mean	std	min	max
Bootstrap(1)	1.7350^{*}	0.08327	1.6032	1.9123	1.7029^{*}	0.1392	1.4299	1.8358
Bootstrap(5)	1.8025	0.07676	1.6526	1.9127	1.8366	0.07996	1.7118	1.9514
Bootstrap(10)	1.7536	0.07772	1.6338	1.8814	1.8403	0.08518	1.6673	1.9296
Bootstrap(30)	1.7818	0.08857	1.6092	1.9025	1.8311	0.08699	1.7230	1.9396
ϵ -greely(0.01)	1.7708	0.09383	1.6374	1.9503	1.8466	0.05494	1.7846	1.9755
ϵ -greedy(0.1)	1.7375	0.04992	1.6452	1.8003	1.8132	0.03502	1.7621	1.8721
ϵ -greedy(0.3)	1.5486	0.03703	1.4812	1.5930	1.5976	0.02739	1.5591	1.6491
ϵ -greedy(0.5)	1.3819^{*}	0.02341	1.3489	1.4169	1.3753^{*}	0.02884	1.3173	1.4020
Exploit	1.1782^{*}	0.2449	0.9253	1.5724	1.1576^{*}	0.00198	1.1554	1.1607
LinUCB(0.01)	1.6349	0.08967	1.4849	1.7360	1.8103	0	1.8103	1.8103
LinUCB(0.1)	1.2037	0.02321	1.1682	1.2577	1.2394	0	1.2394	1.2394
LinUCB(0.3)	1.1661	0.01073	1.1552	1.1926	1.1650	1.863e-08	1.1650	1.1650
LinUCB(0.5)	1.1462	0.01215	1.1136	1.1571	1.1752	1.317e-08	1.1752	1.1752
LinUCB(1.0)	1.1361^{*}	0.01896	1.0969	1.1594	1.1594^{*}	1.317e-08	1.1594	1.1594
TS(0.001)	1.2203	0.026	1.1842	1.2670	1.2725	0.03175	1.2301	1.3422
TS(0.01)	1.1880	0.02895	1.1585	1.2466	1.2377	0.01886	1.2132	1.2713
TS(0.1)	1.1527	0.01988	1.1289	1.1811	1.1791	0.02225	1.1437	1.2169
TS(1.0)	1.1205	0.0142	1.1009	1.1472	1.1362	0.02203	1.0971	1.1599
TS(10.0)	0.7669^{*}	0.1072	0.5445	0.9526	0.8808^{*}	0.01557	0.8483	0.9031
TSNR(0.01)	1.2173^{*}	0.03369	1.1430	1.2561	1.2972^{*}	0.02792	1.2479	1.3394
TSNR(0.1)	1.2285	0.01948	1.1915	1.2610	1.3028	0.02121	1.2701	1.3461
TSNR(1.0)	1.2801	0.02365	1.2558	1.3303	1.3250	0.03148	1.2486	1.3634
TSNR(10.0)	1.6657	0.03285	1.6025	1.7125	1.6153	0.05608	1.5210	1.7128
TSNR(100.0)	1.7816	0.07609	1.7093	1.9278	1.8399	0.1134	1.5240	1.9200
TSNR(1000.0)	1.7652	0.09946	1.6123	1.9346	1.8769	0.03731	1.8409	1.9656

Experiment(AD KDD Cup'12)

• All numbers are relative to the random model.

Algorithm	Cold Start				Warm Start			
	mean	std	min	max	mean	std	\min	max
Bootstrap(1)	1.9933	0.01291	1.9692	2.0098	1.9990	0.005678	1.9878	2.0083
Bootstrap(5)	1.9883	0.01106	1.9686	2.0012	1.9964	0.004983	1.9848	2.0022
Bootstrap(10)	1.9862	0.009128	1.9672	1.9977	1.9890	0.005434	1.9829	2.0003
Bootstrap(30)	1.9824^{*}	0.01492	1.9566	2.0088	1.9886^{*}	0.006086	1.9753	1.9954
ϵ -greedy(0.01)	1.9941	0.007293	1.9834	2.0060	1.9971	0.004908	1.9886	2.0038
ϵ -greedy(0.1)	1.9089	0.004887	1.8965	1.9145	1.8952	0.002741	1.8910	1.8986
ϵ -gready(0.3)	1.7039	0.003797	1.6990	1.7101	1.6973	0.009368	1.6834	1.7193
ϵ -greedy(0.5)	1.5018^{*}	0.004335	1.4965	1.5114	1.4983^{*}	0.006319	1.4845	1.5067
Exploit	1.8185^{*}	0.05235	1.7228	1.8934	1.9241^{*}	0.007046	1.9152	1.9370
LinUCB(0.01)	1.8551	0.03543	1.7977	1.9059	1.9279	0.006951	1.9178	1.9371
LinUCB(0.1)	1.9168	0.005466	1.9070	1.9267	1.9202	0.004434	1.9112	1.9266
LinUCB(0.3)	1.8665	0.003644	1.8609	1.8726	1.8610	0.003271	1.8550	1.8661
LinUCB(0.5)	1.7808	0.007009	1.7669	1.7913	1.7903	0.0051	1.7823	1.7988
LinUCB(1.0)	1.6693^{*}	0.004738	1.6634	1.6762	1.6742^{*}	0.003179	1.6704	1.6792
TS(0.001)	1.3587	0.009703	1.3366	1.3736	1.3518	0.01002	1.3297	1.3673
TS(0.01)	1.4597	0.007215	1.4504	1.4749	1.4891	0.006421	1.4771	1.4994
TS(0.1)	1.5714	0.004855	1.5647	1.5791	1.5905	0.004176	1.5826	1.5967
TS(1.0)	1.5345	0.003435	1.5262	1.5384	1.5421	0.003741	1.5376	1.5480
TS(10.0)	0.9388^{*}	0.4236	0.3064	1.5675	1.3174^{*}	0.003157	1.3115	1.3212
TSNR(0.01)	1.4856^{*}	0.01466	1.4657	1.5078	1.5700^{*}	0.02163	1.5499	1.6298
TSNR(C.1)	1.7931	0.01284	1.7774	1.8167	1.8716	0.01035	1.8518	1.8870
TSNR(1.0)	1.9826	0.005853	1.9704	1.9921	1.9952	0.006996	1.9833	2.0047
TSNR(10.0)	2.0118	0.007808	1.9941	2.0208	2.0095	0.005107	2.0022	2.0198
TSNR(100.0)	2.0039	0.008942	1.9912	2.0215	2.0097	0.004586	2.0022	2.0187
TSNR(1000.0)	2.0047	0.01022	1.9894	2.0228	2.0088	0.004644	1.9966	2.0151

CTR over Time Bucket (Yahoo! News Data)



CTR over Time Buckets (KDD Cup Ads Data)



Efficiency

Time cost on different bootstrap sample sizes



Summary of Experiment

- For solving the contextual bandit problem, the algorithms of e-greedy and LinUCB can achieve the optimal performance, but the input parameters that control the exploration need to be tuned carefully.
- The probability matching/Thomson Sampling strategies highly depend on the selection of the prior.
- Our proposed algorithm is a safe choice of building predictive models for contextual bandit problems under the scenario of cold-start.

Conclusion

- Propose a non-Bayesian Thompson Sampling method to solve the personalized recommendation problem.
- Give both theoretical and empirical analysis to show that the performance of Thompson sampling depends on the choice of the prior.
- Conduct extensive experiments on real data sets to demonstrate the efficacy of the proposed method and other contextual bandit algorithms.

Future Work

- MAB with similarity information
- MAB in a changing environment
- Explore-exploit tradeoff in mechanism design
- Explore-exploit learning with limited resources
- Risk vs. reward tradeoff in MAB

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谢谢!

Bandit Algorithm: simple greedy

- Regret is defined in terms of average reward
- So if we can estimate avg. reward, we can minimize regret
- Consider a greedy algorithm that takes the arm with the highest avg. reward
 - Example:
 - Arm1 has reward 1 with prob. 0.2
 - Arm 2 has reward 1 with prob. 0.8
 - Play A1, get reward 1
 - Play A2, get reward 0
 - Now avg. reward of A1 will never drop to 0,and we will never play A2