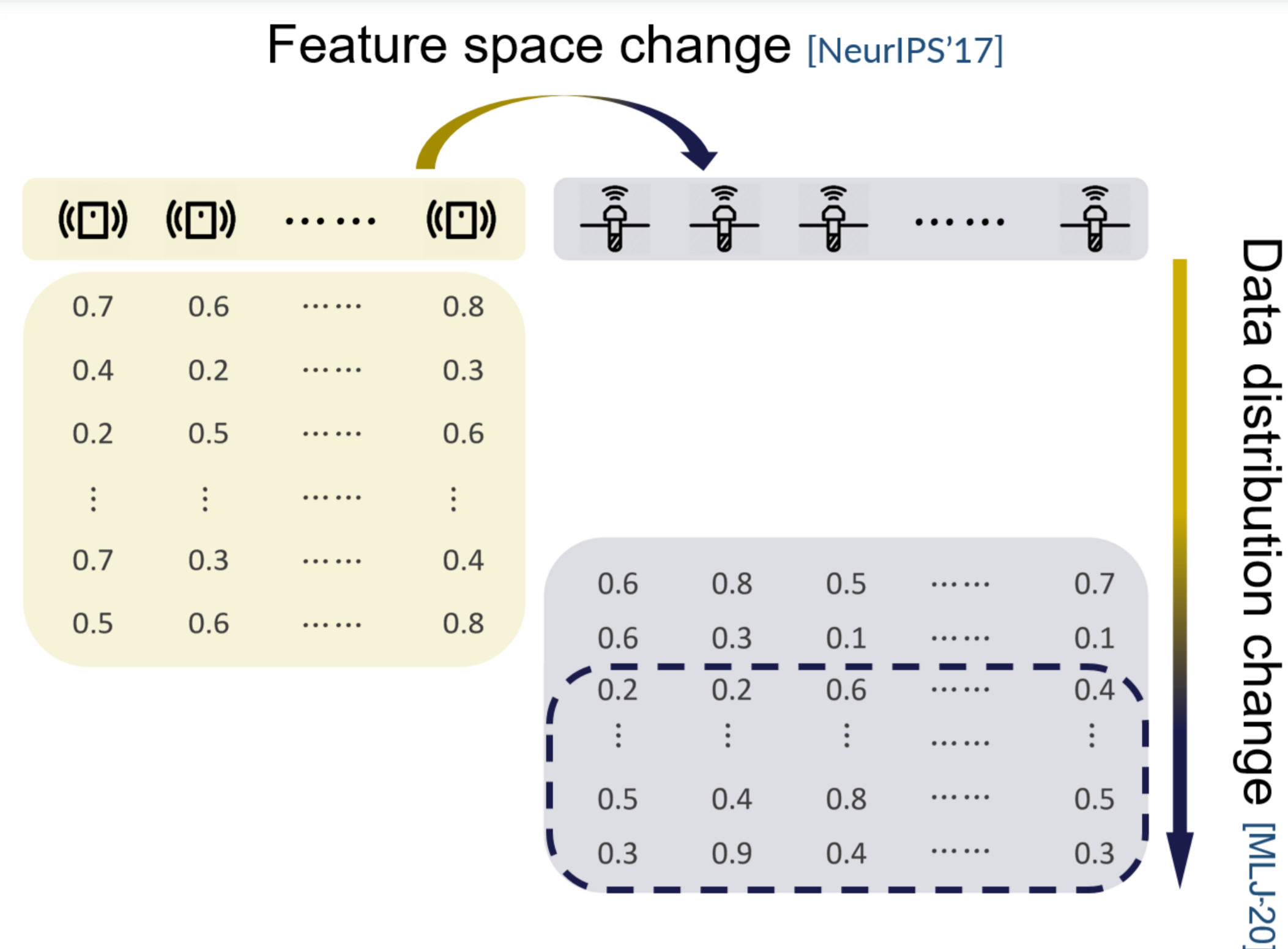


Feature and Distribution Evolvable Streams

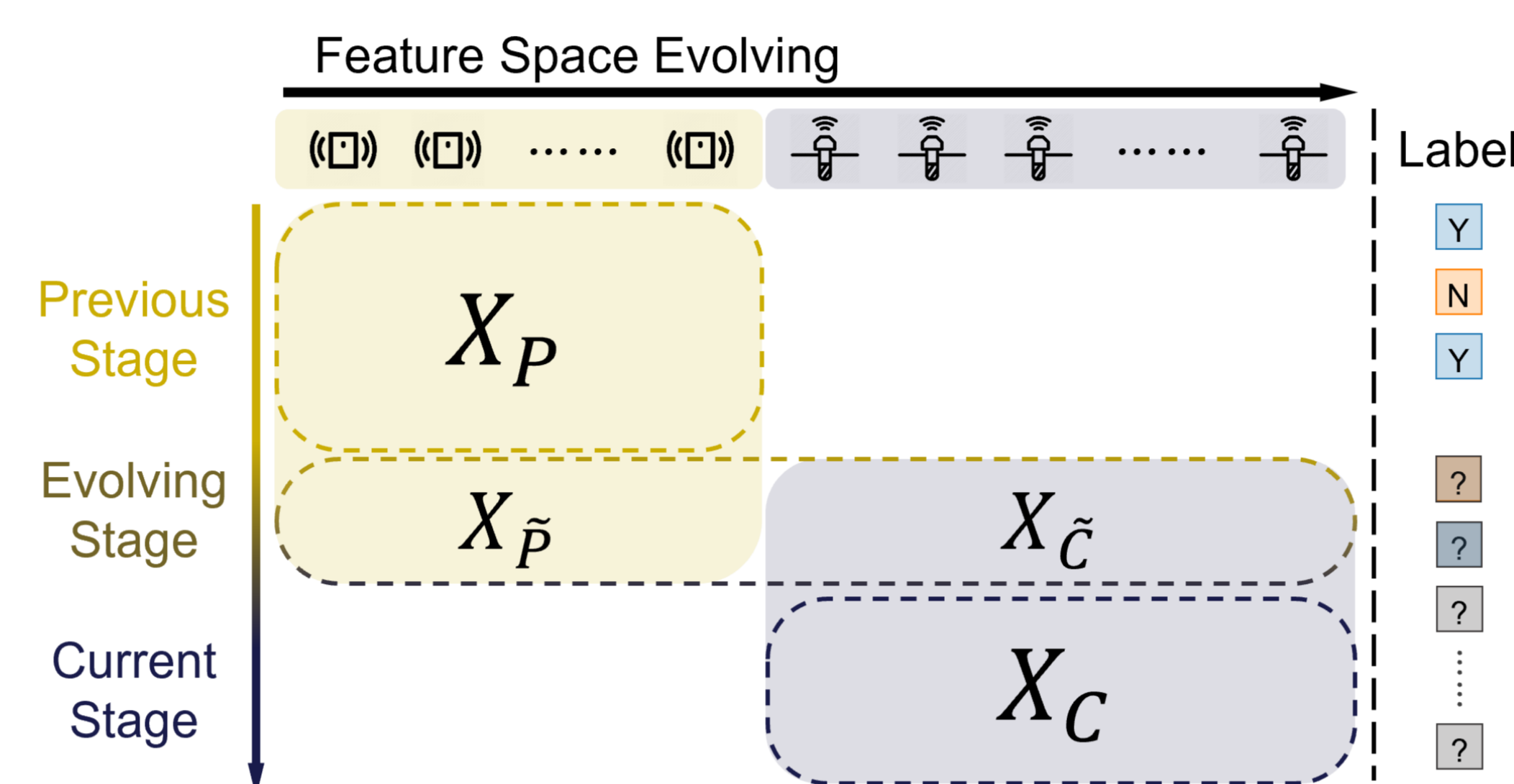


[NeurIPS'17] Hou, B.-J., Zhang, L., & Zhou, Z.-H. (2017). Learning with feature evolvable streams.
[MLJ'20] Zhao, P., Cai, L.-W., & Zhou, Z.-H. (2020). Handling concept drift via model reuse.

Formulation

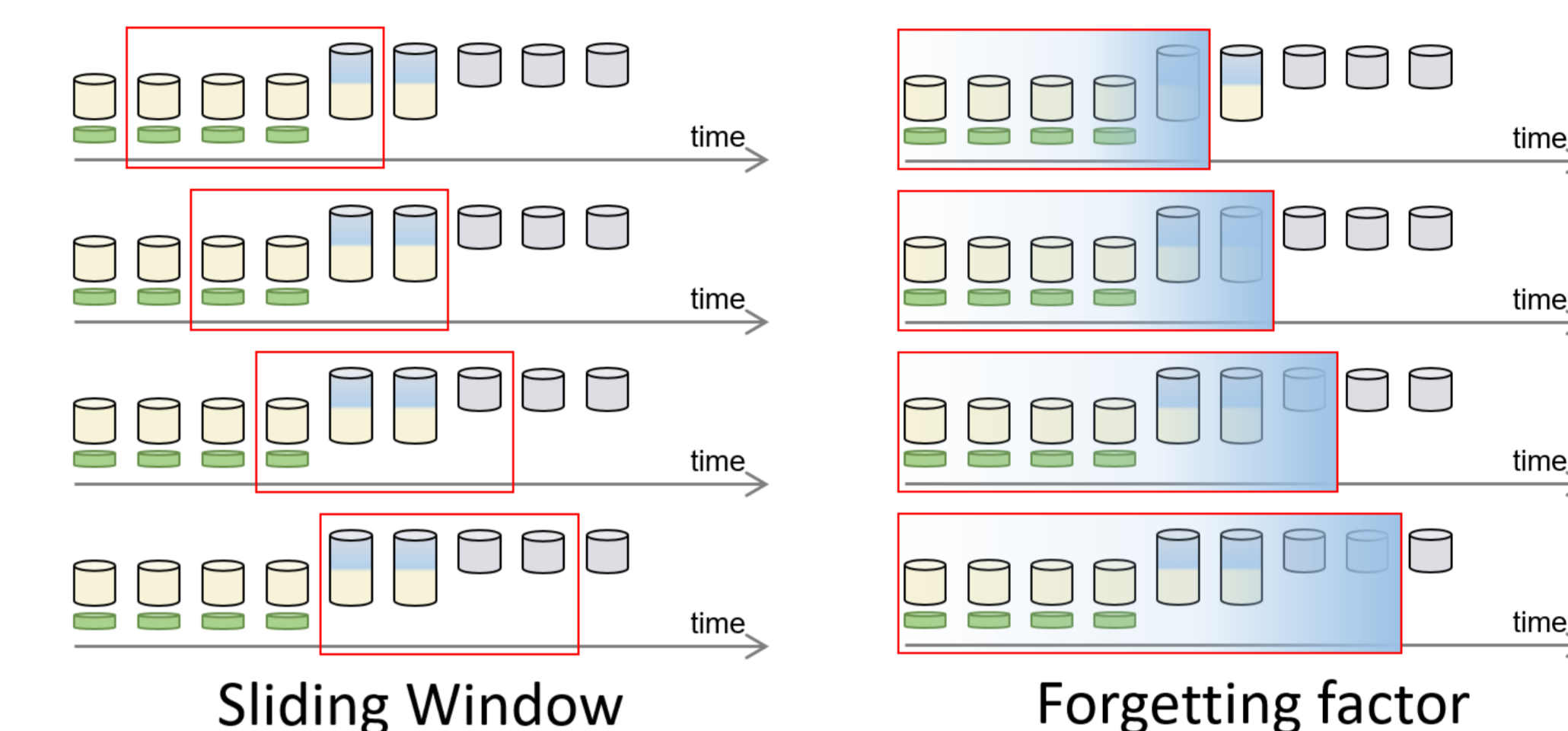
Feature and Distribution Evolving Stream Learning (FDESL)

- previous stage (labeled)
- evolving stage (feature space and distribution changing)
- current stage (unlabeled)



Challenge

Can we use Sliding Window or Forgetting Factor?



Drawbacks

- hard to handle distribution change
- hard to analyze generalization ability

Evolving Discrepancy & Generalization Bound

Idea: Measure Discrepancy of data from different feature spaces

Bridge the gap via the evolving stage

- data in the evolving stage share the same labels
- admissible loss aligns the hypotheses via the evolving stage

$$disc_E''(S_P, S_C) = \sup_{g \in \mathcal{G}, h \in \mathcal{H}} [\hat{R}_{S_P}(g, y_P) - \hat{R}_{S_{\bar{P}}}(g, y_{\bar{P}})] + [\hat{R}_{S_{\bar{C}}}(h, y_{\bar{C}}) - \hat{R}_{S_C}(h, y_C)] + \sigma d_1(g, h)$$

Previous Stage to Evolving Stage Evolving Stage to Current Stage Hypotheses Alignment

Generalization bound

- The expected risk on the current data batch is upper bounded by **empirical risk** & **evolving discrepancy**

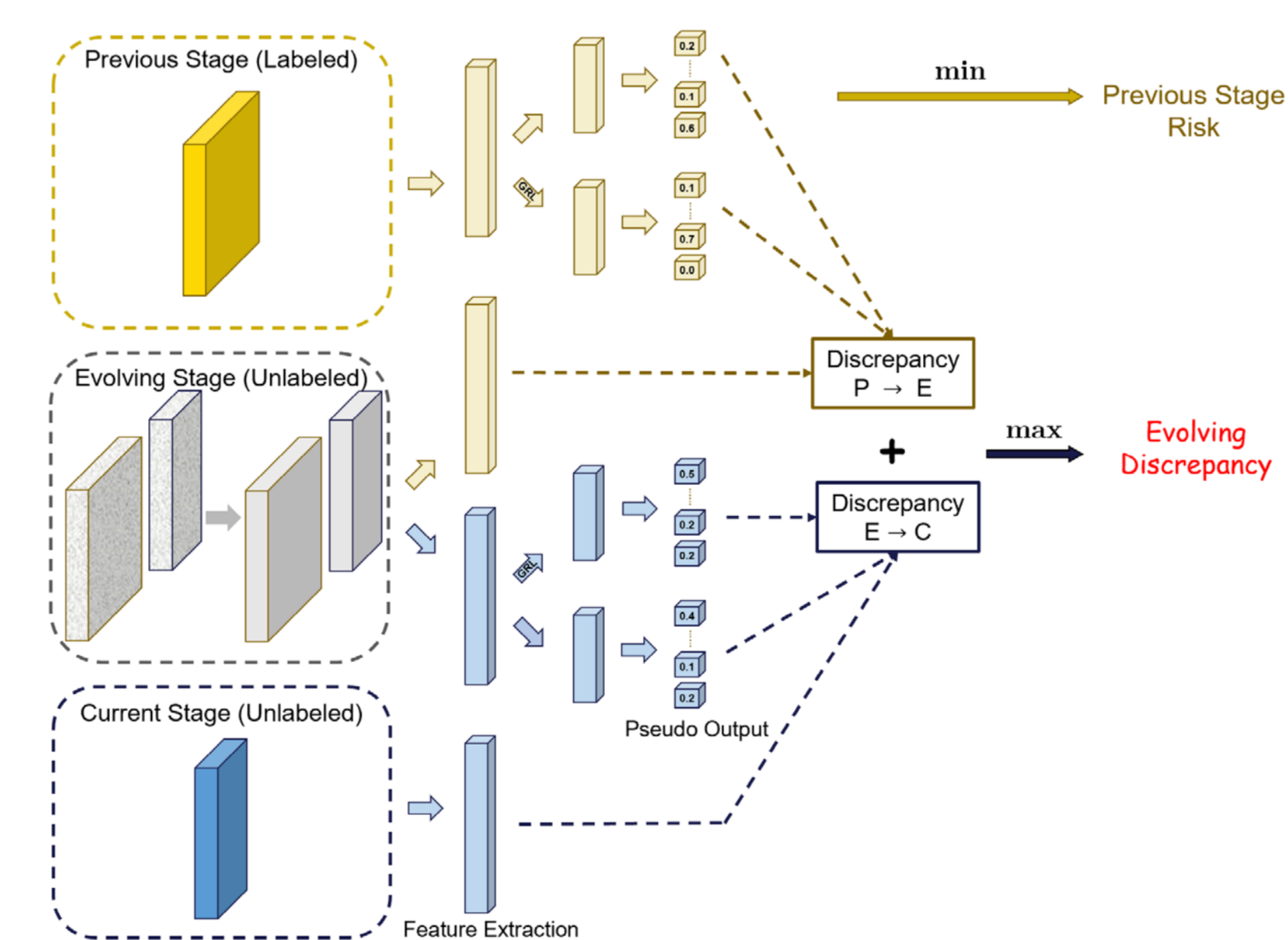
$$R_{D_C}(h, f_C) \leq \hat{R}_{S_{P_{\alpha}}}(g, y_P) + disc_E(S_P, S_C) + 2L\mathfrak{R}_n(\mathcal{H}) + M_C \sqrt{\frac{\log(1/\delta)}{2n}}$$

Remarks

- Evolving discrepancy measures the discrepancy between two consecutive batches (with different feature space & distribution) via the evolving stage
- So we can analyze the generalization ability for the FDESL problem

Deep Neural Network Implementation

- estimate weights $\alpha \in \mathbb{R}^m, \beta \in \mathbb{R}^n$ [TCS'14]
- solve the minimax optimization



Adversarial network [JMLR'16] based EDM Framework

[TCS'14] Cortes, C., & Mohri, M. (2014). Domain adaptation and sample bias correction theory and algorithm for regression.
[JMLR'16] Ganin, Yaroslav, et al. (2016). Domain-adversarial training of neural networks.

Experiments

Synthetic data

- the evolving discrepancy reflects the relation

Real-world applications

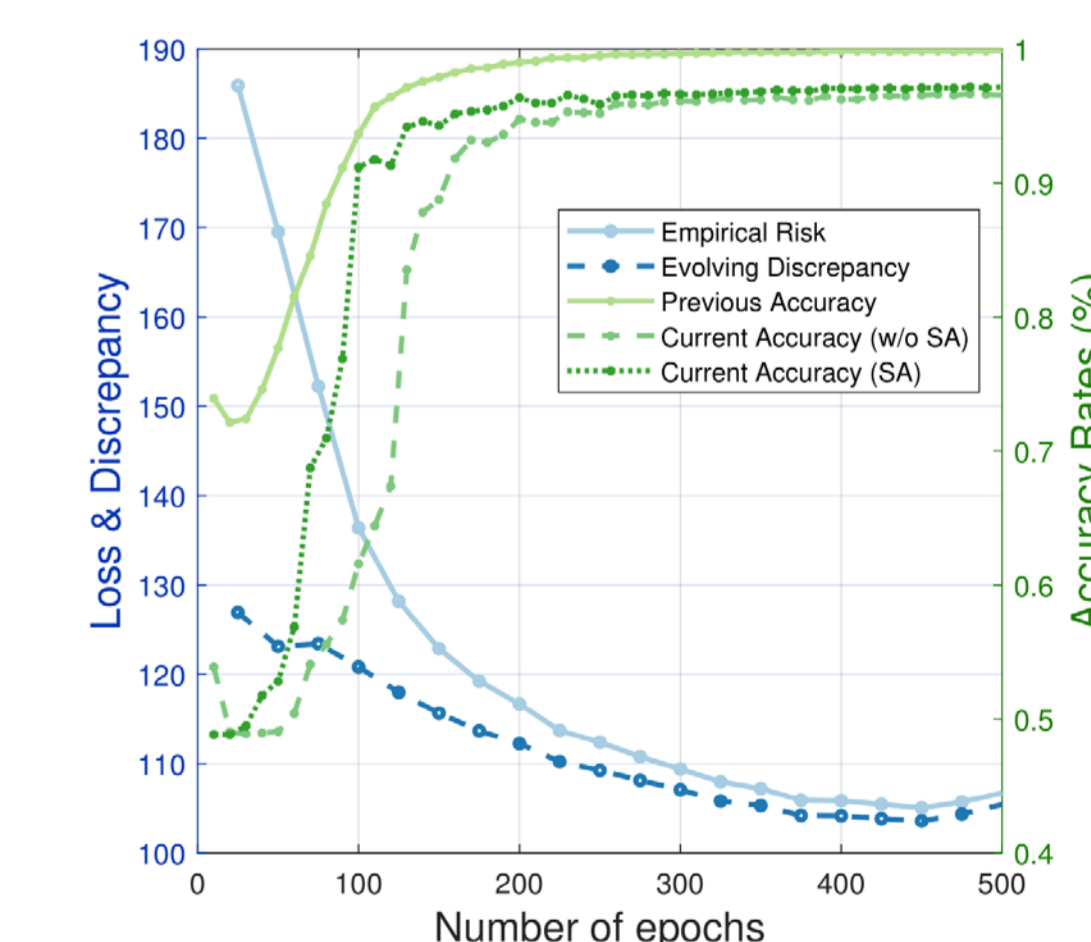
- the EDM algorithm solves the FDESL problem

Evolving discrepancy verification

- minimizing the evolving discrepancy improves the average accuracy

Methods	RFID	A.Books	A.Movies	A.CDs
FESL	77.39 ± 2.5	70.53 ± 4.7	67.30 ± 3.6	61.79 ± 3.4
TSIW	91.34 ± 1.1	73.83 ± 2.1	72.61 ± 2.0	63.93 ± 0.7
EDM	93.32 ± 1.2	77.97 ± 5.2	76.16 ± 1.8	69.47 ± 2.5

Methods	EN-FR	FR-SP	GR-IT	IT-GR
FESL	78.51 ± 1.9	73.64 ± 2.6	75.12 ± 1.4	77.96 ± 0.9
TSIW	84.42 ± 1.8	79.43 ± 2.3	81.92 ± 4.4	82.30 ± 2.7
EDM	86.74 ± 0.7	80.72 ± 1.4	85.40 ± 3.9	84.84 ± 2.7



Experiments on real-world applications

Evolving discrepancy verification

Conclusion

- ♠ We formulate the Feature and Distribution Evolving Stream Learning (FDESL) problem, which accommodates a variety of real-world applications
- ♠ We characterize the FDESL problem by evolving discrepancy and derive the generalization ability analysis
- ♠ We propose the Evolving Discrepancy Minimization (EDM) algorithm and validates the effectiveness on synthetic and real-world data