



# Efficient Rectification of **Neuro-Symbolic** Reasoning Inconsistencies by **Abductive Reflection**

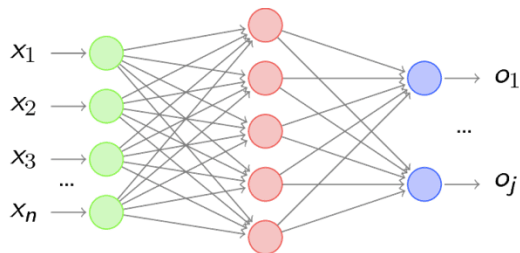
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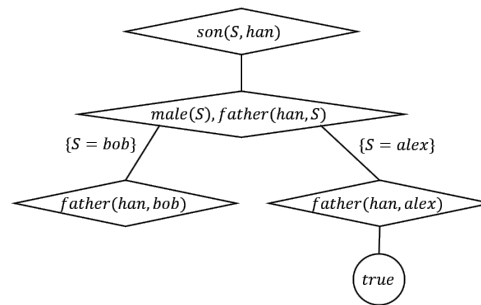
This paper has won the **Outstanding Paper Award** of AAAI 2025



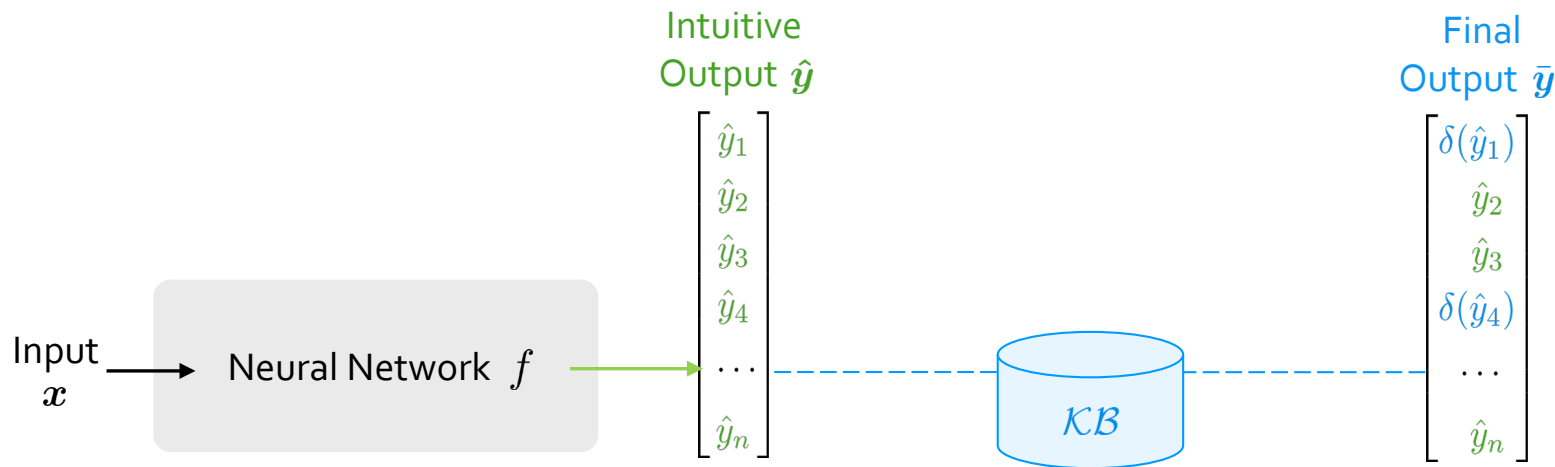
Effectively combining neural network and logical reasoning is the "**holy grail**" of AI.



**Neural network** is adept at using **data**



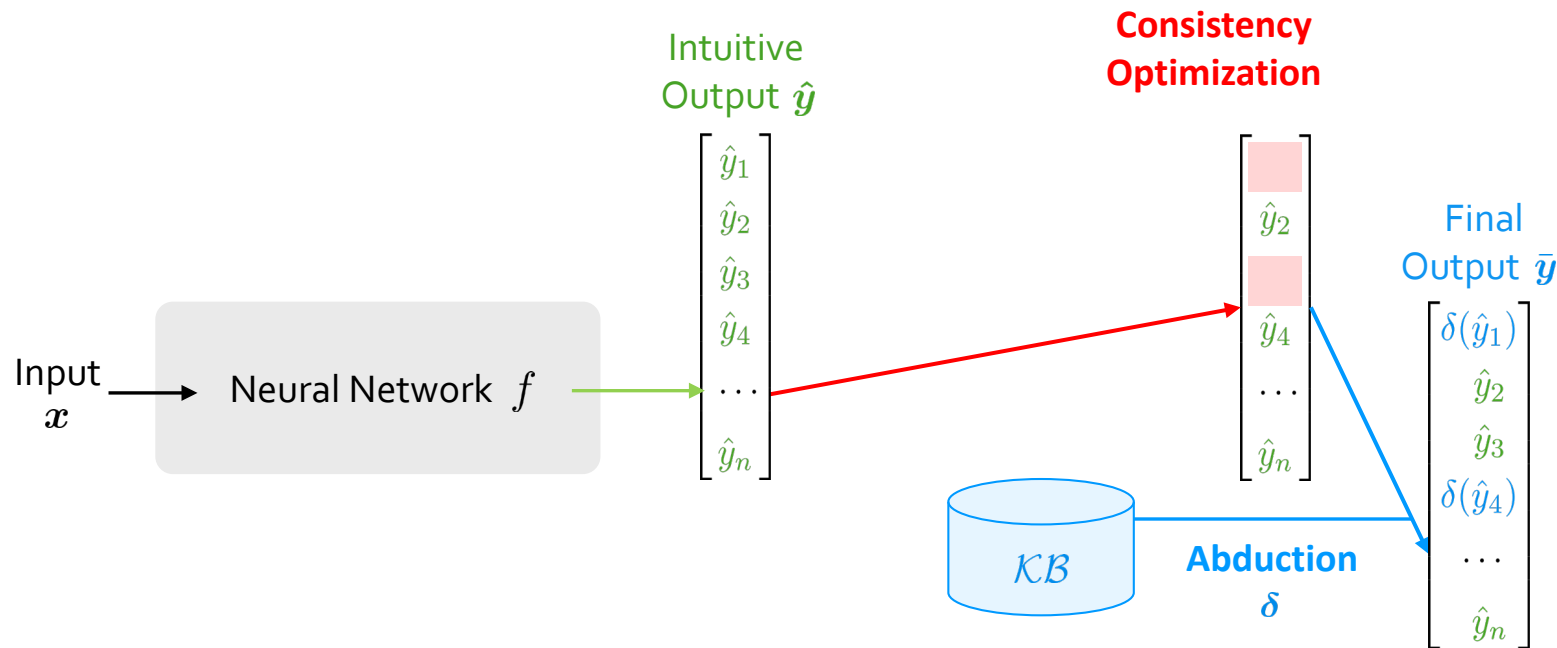
**Logical reasoning** is adept at using **knowledge**



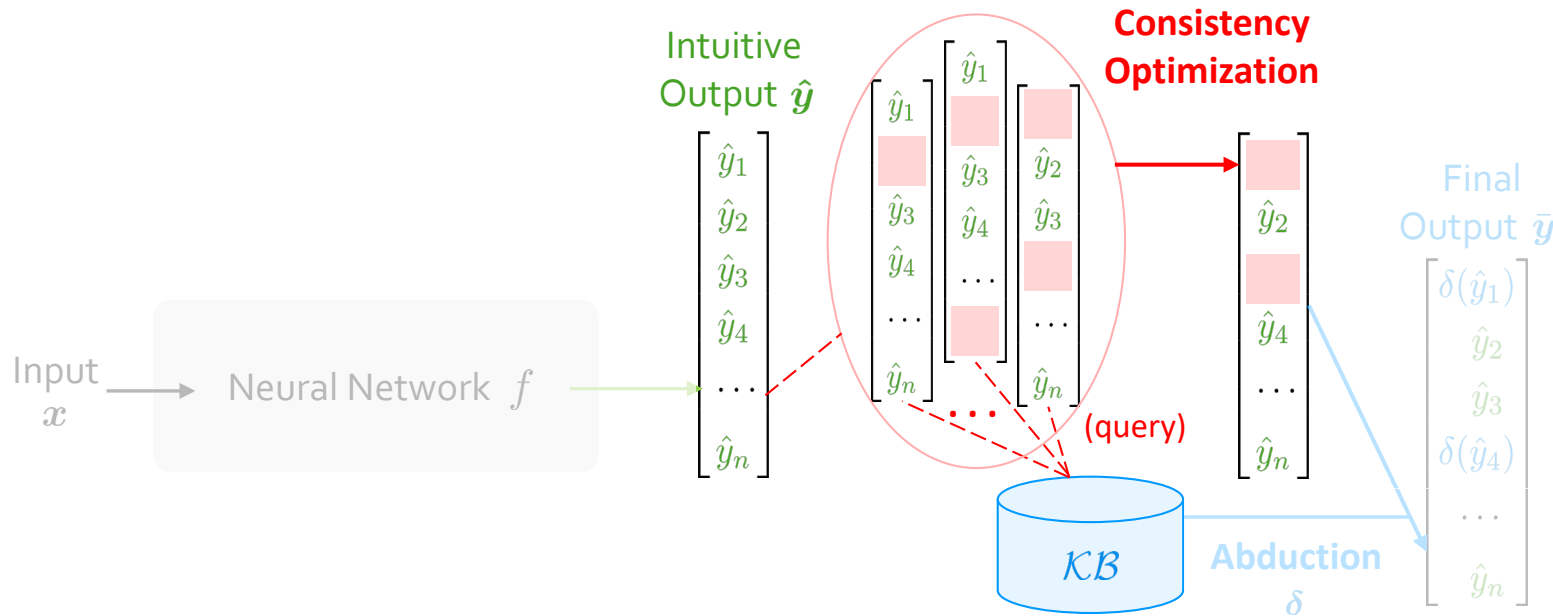
Neural network  $f$  maps input  $x$  into  $\hat{y} = [\hat{y}_1, \hat{y}_2, \dots, \hat{y}_n]$ .

Knowledge base  $\mathcal{KB}$  holds constraints on  $y$ , and can perform reasoning.

Zhou, Z.-H. 2019. Abductive learning: towards bridging machine learning and logical reasoning. Science China Information Sciences, 62: 1–3.

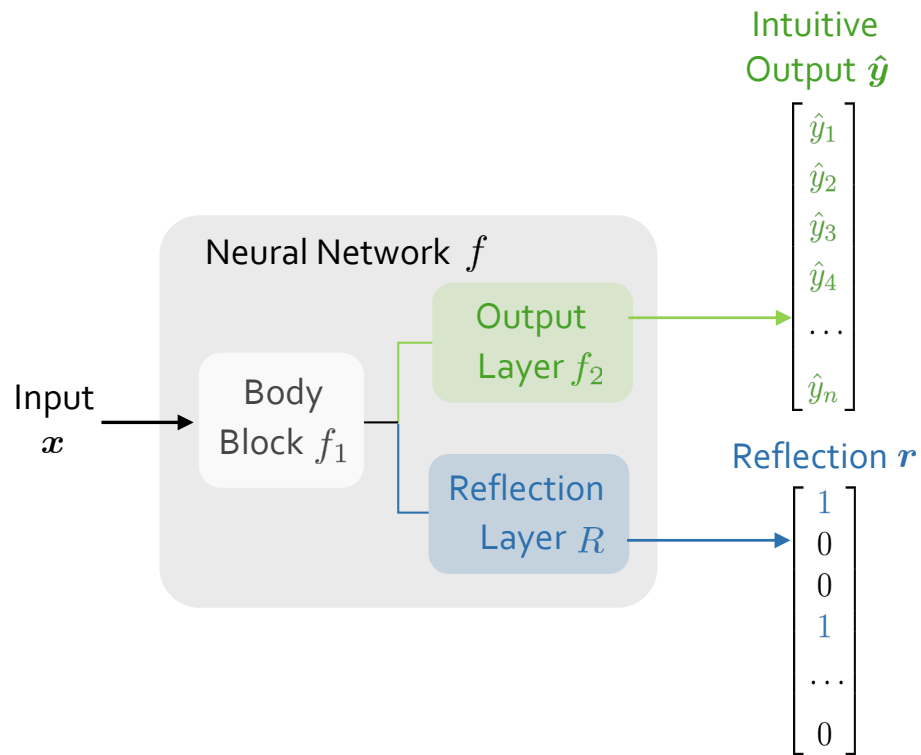


# Consistency Optimization an Efficiency Bottleneck of ABL

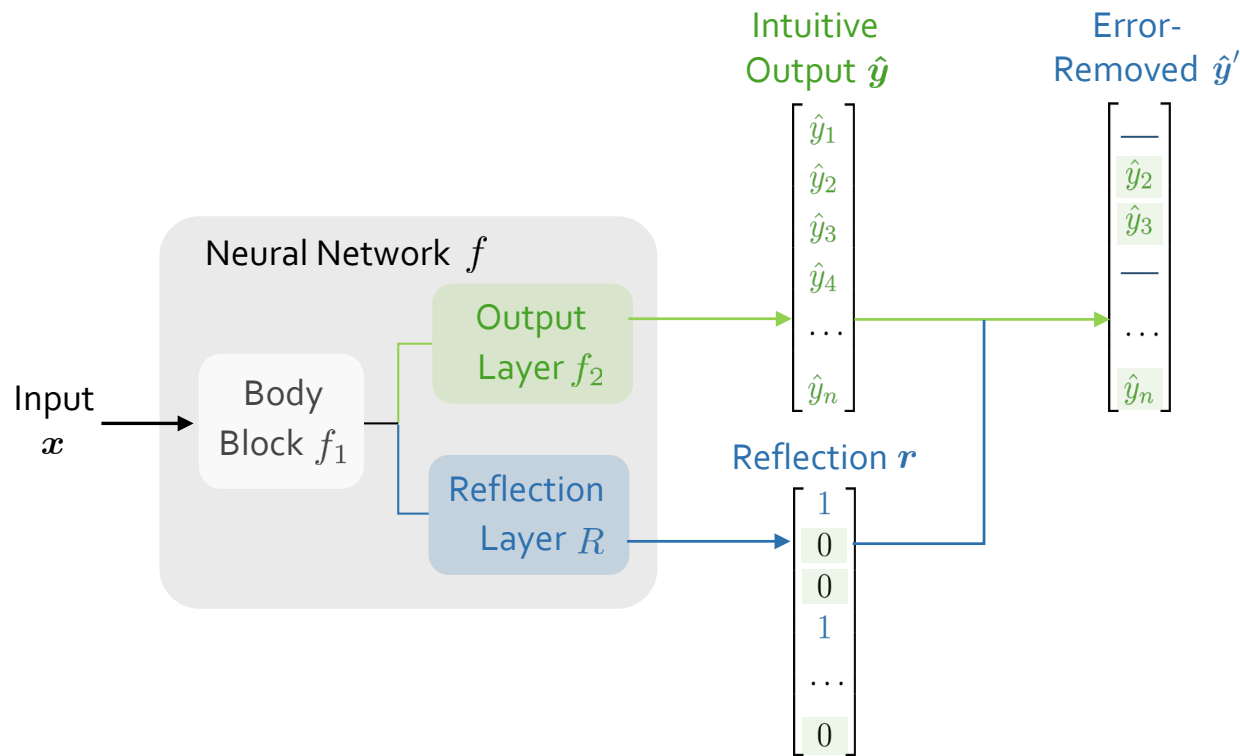


Too many possible solutions to query, too much time spent on consistency evaluation

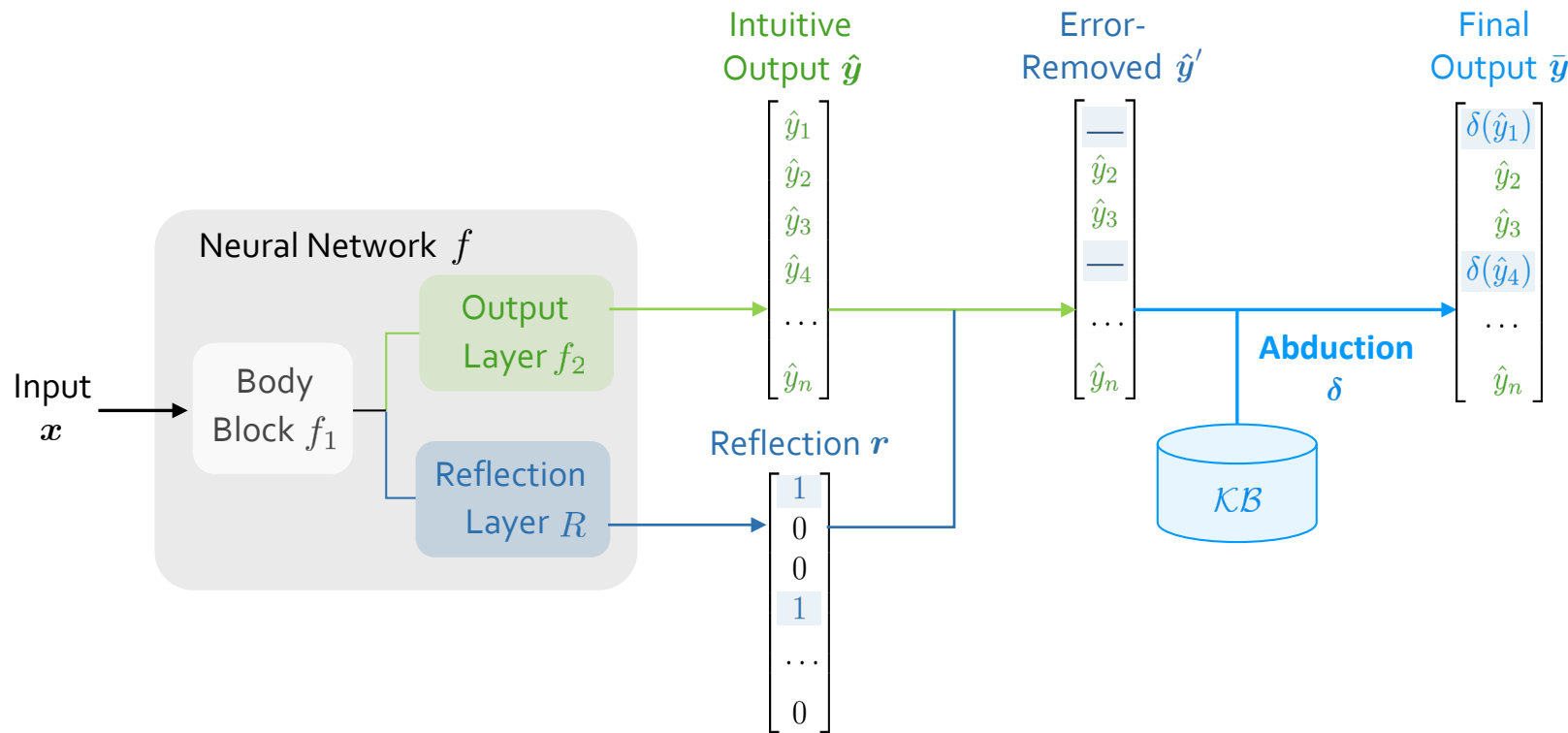
# Our Method: **Abductive Learning with Reflection**



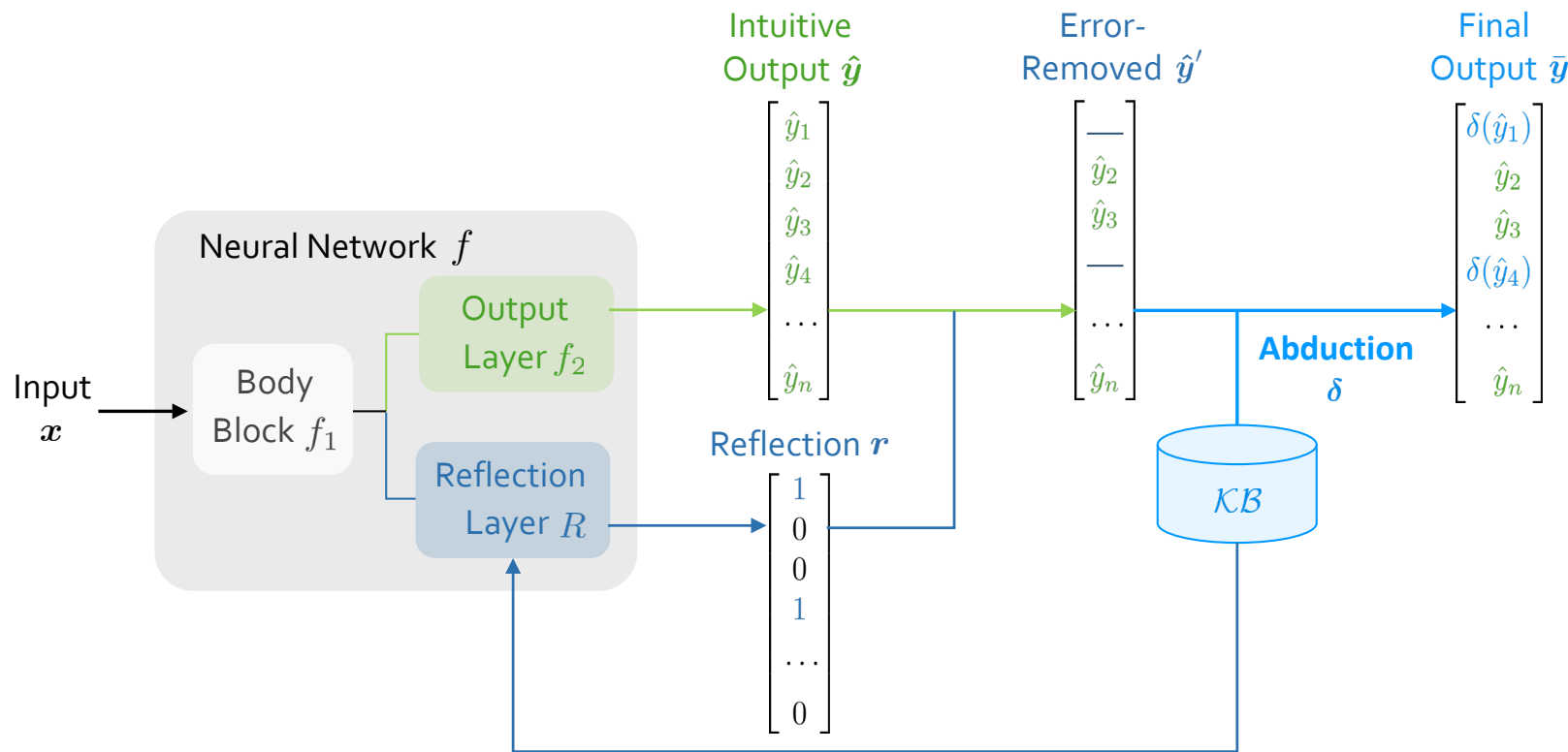
## Our Method: **Abductive Learning with Reflection** (cont.)

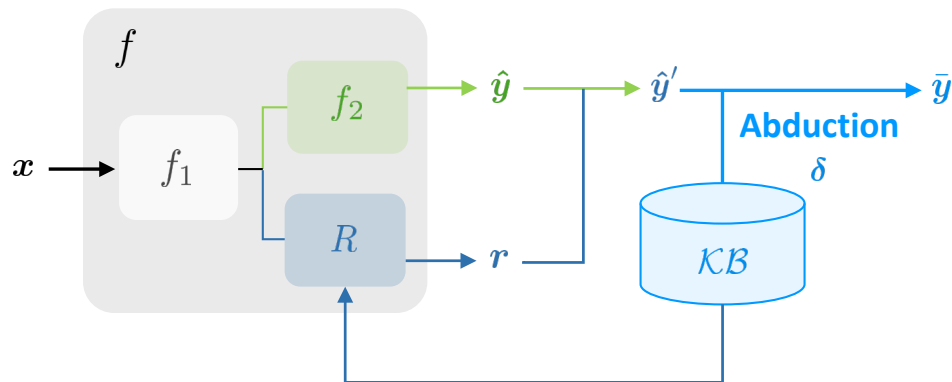


# Our Method: **Abductive Learning with Reflection** (cont.)



# Our Method: **Abductive Learning with Reflection** (cont.)





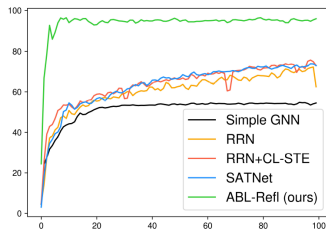
**Neural network** provides a fast, overall approximate solution, and

**Reflection** promptly directs the focus for **Symbolic reasoning** on a much reduced space.

- Reflection vector is generated **simultaneously** with intuitive output;
- During each inference,  $\mathcal{KB}$  is only invoked **once**, regardless of data scale;
- Reflection is trained using information **directly from**  $\mathcal{KB}$ .

# Experiments

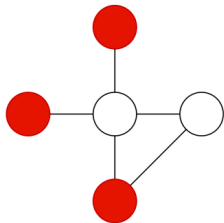
| Method          | Training Time (min)              | Inference Time (s) | Inference Accuracy             |
|-----------------|----------------------------------|--------------------|--------------------------------|
| RRN             | 114.8 $\pm$ 7.8                  | 0.19 $\pm$ 0.01    | 73.1 $\pm$ 1.2                 |
| CL-STE          | 173.6 $\pm$ 9.9                  | 0.19 $\pm$ 0.02    | 76.5 $\pm$ 1.8                 |
| SATNet          | 140.3 $\pm$ 6.8                  | 0.11 $\pm$ 0.01    | 74.1 $\pm$ 0.4                 |
| <b>ABL-Refl</b> | <b>109.8<math>\pm</math>10.8</b> | 0.22 $\pm$ 0.02    | <b>97.4<math>\pm</math>0.3</b> |



| Solver              | Method          | Inference Time (s) |                                   |                                   |
|---------------------|-----------------|--------------------|-----------------------------------|-----------------------------------|
|                     |                 | NN Time            | Abduction Time                    | Overall Time                      |
| MiniSAT             | Solver only     | -                  | 0.227 $\pm$ 0.024                 | 0.227 $\pm$ 0.024                 |
|                     | <b>ABL-Refl</b> | 0.021 $\pm$ 0.004  | <b>0.196<math>\pm</math>0.015</b> | <b>0.217<math>\pm</math>0.019</b> |
| Prolog with CLP(FD) | Solver only     | -                  | 105.81 $\pm$ 5.62                 | 105.81 $\pm$ 5.62                 |
|                     | <b>ABL-Refl</b> | 0.021 $\pm$ 0.004  | <b>31.86<math>\pm</math>1.88</b>  | <b>31.88<math>\pm</math>1.89</b>  |

Achieves far better **accuracy** in only a **few epochs (<10)**.

Enhances the **efficiency** of symbolic solvers.



| Method          | Dataset (Graph nums./Avg. nodes per graph/Avg. edges per graph) |                                   |                                   |                                   |
|-----------------|-----------------------------------------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
|                 | ENZYMES (600/33/62)                                             | PROTEINS (1113/39/73)             | IMDB-Binary (1000/19/97)          | COLLAB (5000/74/2457)             |
| Erdos           | 0.883 $\pm$ 0.156                                               | 0.905 $\pm$ 0.133                 | 0.936 $\pm$ 0.175                 | 0.852 $\pm$ 0.212                 |
| Neural SFE      | 0.933 $\pm$ 0.148                                               | 0.926 $\pm$ 0.165                 | 0.961 $\pm$ 0.143                 | 0.781 $\pm$ 0.316                 |
| <b>ABL-Refl</b> | <b>0.991<math>\pm</math>0.017</b>                               | <b>0.985<math>\pm</math>0.020</b> | <b>0.979<math>\pm</math>0.029</b> | <b>0.982<math>\pm</math>0.015</b> |

Capable of handling **scalable** data scenarios, and a **wide range of** domain knowledge.



# Thanks!



Presented by **Wen-Chao Hu**

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