

Lecture 8: Knowledge 2

Previously...

```
function HYBRID-WUMPUS-AGENT(percept) returns an action
  inputs: percept, a list, [stench,breeze,glitter,bump,scream]
  persistent: KB, a knowledge base, initially the atemporal “wumpus physics”
               t, a counter, initially 0, indicating time
               plan, an action sequence, initially empty

  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  TELL the KB the temporal “physics” sentences for time t
  safe  $\leftarrow$   $\{[x, y] : \text{ASK}(\text{KB}, \text{OK}_{x,y}^t) = \text{true}\}$ 
  if  $\text{ASK}(\text{KB}, \text{Glitter}^t) = \text{true}$  then
    plan  $\leftarrow$  [Grab] + PLAN-ROUTE(current,  $\{[1,1]\}$ , safe) + [Climb]
  if plan is empty then
    unvisited  $\leftarrow$   $\{[x, y] : \text{ASK}(\text{KB}, L_{x,y}^{t'}) = \text{false for all } t' \leq t\}$ 
    plan  $\leftarrow$  PLAN-ROUTE(current, unvisited  $\cap$  safe, safe)
  if plan is empty and  $\text{ASK}(\text{KB}, \text{HaveArrow}^t) = \text{true}$  then
    possible_wumpus  $\leftarrow$   $\{[x, y] : \text{ASK}(\text{KB}, \neg W_{x,y}) = \text{false}\}$ 
    plan  $\leftarrow$  PLAN-SHOT(current, possible_wumpus, safe)
  if plan is empty then // no choice but to take a risk
    not_unsafe  $\leftarrow$   $\{[x, y] : \text{ASK}(\text{KB}, \neg \text{OK}_{x,y}^t) = \text{false}\}$ 
    plan  $\leftarrow$  PLAN-ROUTE(current, unvisited  $\cap$  not_unsafe, safe)
  if plan is empty then
    plan  $\leftarrow$  PLAN-ROUTE(current,  $\{[1, 1]\}$ , safe) + [Climb]
  action  $\leftarrow$  POP(plan)
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow$  t + 1
  return action
```

```
function PLAN-ROUTE(current,goals,allowed) returns an action sequence
  inputs: current, the agent’s current position
           goals, a set of squares; try to plan a route to one of them
           allowed, a set of squares that can form part of the route

  problem  $\leftarrow$  ROUTE-PROBLEM(current, goals, allowed)
  return A*-GRAPH-SEARCH(problem)
```

Pros and cons of propositional logic



- 😊 Propositional logic is **declarative**: pieces of syntax correspond to facts
- 😊 Propositional logic allows partial/disjunctive/negated information (unlike most data structures and databases)
- 😊 Propositional logic is **compositional**:
meaning of $B_{1,1} \wedge P_{1,2}$ is derived from meaning of $B_{1,1}$ and of $P_{1,2}$
- 😊 Meaning in propositional logic is **context-independent** (unlike natural language, where meaning depends on context)
- 😞 Propositional logic has very limited expressive power (unlike natural language)
E.g., cannot say “pits cause breezes in adjacent squares”
except by writing one sentence for each square

First-order logic



Whereas propositional logic assumes world contains **facts**, first-order logic (like natural language) assumes the world contains

- **Objects**: people, houses, numbers, theories, Ronald McDonald, colors, baseball games, wars, centuries . . .
- **Relations**: red, round, bogus, prime, multistoried . . ., brother of, bigger than, inside, part of, has color, occurred after, owns, comes between, . . .
- **Functions**: father of, best friend, third inning of, one more than, end of . . .

Logics in general

Language	Ontological Commitment	Epistemological Commitment
Propositional logic	facts	true/false/unknown
First-order logic	facts, objects, relations	true/false/unknown
Temporal logic	facts, objects, relations, times	true/false/unknown
Probability theory	facts	degree of belief
Fuzzy logic	facts + degree of truth	known interval value

Syntax of FOL: Basic elements



Constants	<i>KingJohn, 2, UCB, ...</i>
Predicates	<i>Brother, >, ...</i>
Functions	<i>Sqrt, LeftLegOf, ...</i>
Variables	<i>x, y, a, b, ...</i>
Connectives	$\wedge \vee \neg \Rightarrow \Leftrightarrow$
Equality	$=$
Quantifiers	$\forall \exists$

Atomic sentences

Atomic sentence = *predicate*(*term*₁, ..., *term*_{*n*})
or *term*₁ = *term*₂

Term = *function*(*term*₁, ..., *term*_{*n*})
or *constant* or *variable*

E.g., *Brother*(*KingJohn*, *RichardTheLionheart*)
> (*Length*(*LeftLegOf*(*Richard*)), *Length*(*LeftLegOf*(*KingJohn*)))

Complex sentences

Complex sentences are made from atomic sentences using connectives

$$\neg S, \quad S_1 \wedge S_2, \quad S_1 \vee S_2, \quad S_1 \Rightarrow S_2, \quad S_1 \Leftrightarrow S_2$$

E.g. $Sibling(KingJohn, Richard) \Rightarrow Sibling(Richard, KingJohn)$

$$>(1, 2) \vee \leq(1, 2)$$

$$>(1, 2) \wedge \neg >(1, 2)$$

Truth in first-order logic



Sentences are true with respect to a **model** and an **interpretation**

Model contains ≥ 1 objects (**domain elements**) and relations among them

Interpretation specifies referents for

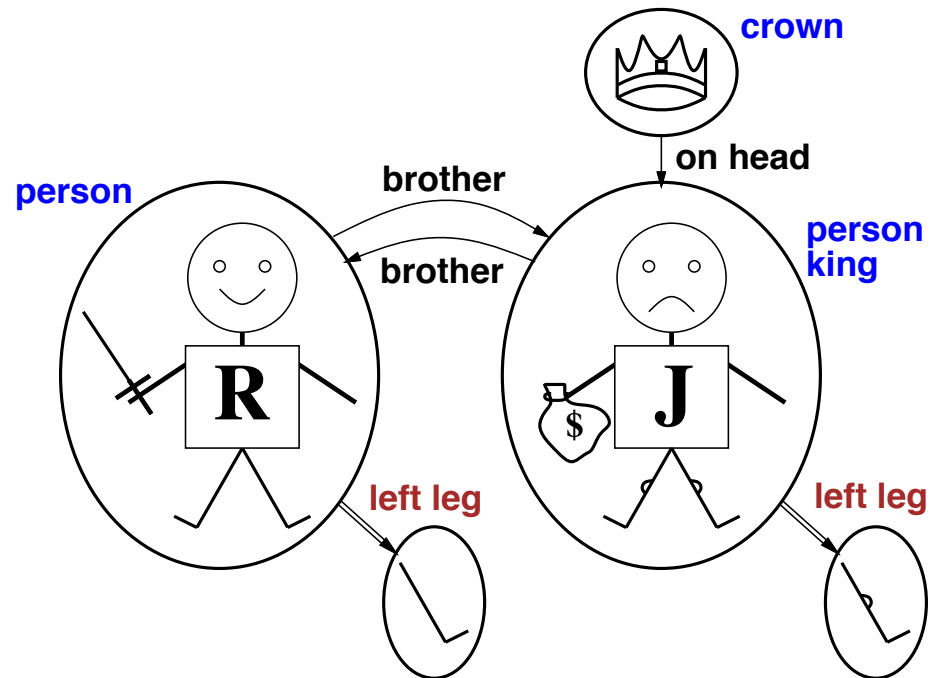
constant symbols \rightarrow **objects**

predicate symbols \rightarrow **relations**

function symbols \rightarrow **functional relations**

An atomic sentence *predicate*(*term*₁, ..., *term*_{*n*}) is true
iff the **objects** referred to by *term*₁, ..., *term*_{*n*}
are in the **relation** referred to by *predicate*

Models for FOL: Example



Consider the interpretation in which
Richard → Richard the Lionheart
John → the evil King John
Brother → the brotherhood relation

Under this interpretation, $Brother(Richard, John)$ is true just in case Richard the Lionheart and the evil King John are in the brotherhood relation in the model

Models for FOL: Lots!



Entailment in propositional logic can be computed by enumerating models

We **can** enumerate the FOL models for a given KB vocabulary:

For each number of domain elements n from 1 to ∞

For each k -ary predicate P_k in the vocabulary

For each possible k -ary relation on n objects

For each constant symbol C in the vocabulary

For each choice of referent for C from n objects ...

Computing entailment by enumerating FOL models is not easy!

Universal quantification



$\forall \langle \text{variables} \rangle \langle \text{sentence} \rangle$

Everyone at Berkeley is smart:

$\forall x \text{ At}(x, \text{Berkeley}) \Rightarrow \text{Smart}(x)$

$\forall x P$ is true in a model m iff P is true with x being **each** possible object in the model

Roughly speaking, equivalent to the conjunction of instantiations of P

$(\text{At}(\text{KingJohn}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{KingJohn}))$
 $\wedge (\text{At}(\text{Richard}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{Richard}))$
 $\wedge (\text{At}(\text{Berkeley}, \text{Berkeley}) \Rightarrow \text{Smart}(\text{Berkeley}))$
 $\wedge \dots$

A common mistake to avoid

Typically, \Rightarrow is the main connective with \forall

Common mistake: using \wedge as the main connective with \forall :

$$\forall x \text{ } At(x, Berkeley) \wedge Smart(x)$$

means “Everyone is at Berkeley and everyone is smart”

Existential quantification

$\exists \langle \text{variables} \rangle \langle \text{sentence} \rangle$

Someone at Stanford is smart:

$\exists x \text{ At}(x, \text{Stanford}) \wedge \text{Smart}(x)$

$\exists x P$ is true in a model m iff P is true with x being **some** possible object in the model

Roughly speaking, equivalent to the disjunction of instantiations of P

$(\text{At}(\text{KingJohn}, \text{Stanford}) \wedge \text{Smart}(\text{KingJohn}))$
 $\vee (\text{At}(\text{Richard}, \text{Stanford}) \wedge \text{Smart}(\text{Richard}))$
 $\vee (\text{At}(\text{Stanford}, \text{Stanford}) \wedge \text{Smart}(\text{Stanford}))$
 $\vee \dots$

Another common mistake to avoid



Typically, \wedge is the main connective with \exists

Common mistake: using \Rightarrow as the main connective with \exists :

$$\exists x \text{ At}(x, \text{Stanford}) \Rightarrow \text{Smart}(x)$$

is true if there is anyone who is not at Stanford!

Properties of quantifiers



$\forall x \forall y$ is the same as $\forall y \forall x$ (why??)

$\exists x \exists y$ is the same as $\exists y \exists x$ (why??)

$\exists x \forall y$ is **not** the same as $\forall y \exists x$

$\exists x \forall y \text{ Loves}(x, y)$

“There is a person who loves everyone in the world”

$\forall y \exists x \text{ Loves}(x, y)$

“Everyone in the world is loved by at least one person”

Quantifier duality: each can be expressed using the other

$\forall x \text{ Likes}(x, \text{IceCream}) \quad \neg \exists x \neg \text{Likes}(x, \text{IceCream})$

$\exists x \text{ Likes}(x, \text{Broccoli}) \quad \neg \forall x \neg \text{Likes}(x, \text{Broccoli})$

Fun with sentences



Brothers are siblings

$$\forall x, y \text{ Brother}(x, y) \Rightarrow \text{Sibling}(x, y).$$

“Sibling” is symmetric

$$\forall x, y \text{ Sibling}(x, y) \Leftrightarrow \text{Sibling}(y, x).$$

One’s mother is one’s female parent

$$\forall x, y \text{ Mother}(x, y) \Leftrightarrow (\text{Female}(x) \wedge \text{Parent}(x, y)).$$

A first cousin is a child of a parent’s sibling

$$\forall x, y \text{ FirstCousin}(x, y) \Leftrightarrow \exists p, ps \text{ Parent}(p, x) \wedge \text{Sibling}(ps, p) \wedge \text{Parent}(ps, y)$$

Equality

$term_1 = term_2$ is true under a given interpretation
if and only if $term_1$ and $term_2$ refer to the same object

E.g., $1 = 2$ and $\forall x \times(Sqrt(x), Sqrt(x)) = x$ are satisfiable
 $2 = 2$ is valid

E.g., definition of (full) *Sibling* in terms of *Parent*:

$$\forall x, y \text{ Sibling}(x, y) \Leftrightarrow [\neg(x = y) \wedge \exists m, f \neg(m = f) \wedge \\ \text{Parent}(m, x) \wedge \text{Parent}(f, x) \wedge \text{Parent}(m, y) \wedge \text{Parent}(f, y)]$$

Interacting with FOL KBs

Suppose a wumpus-world agent is using an FOL KB and perceives a smell and a breeze (but no glitter) at $t = 5$:

$Tell(KB, Percept([Smell, Breeze, None], 5))$

$Ask(KB, \exists a \text{ Action}(a, 5))$

I.e., does KB entail any particular actions at $t = 5$?

Answer: $Yes, \{a/Shoot\}$ ← substitution (binding list)

Given a sentence S and a substitution σ ,

$S\sigma$ denotes the result of plugging σ into S ; e.g.,

$S = Smarter(x, y)$

$\sigma = \{x/Hillary, y/Bill\}$

$S\sigma = Smarter(Hillary, Bill)$

$Ask(KB, S)$ returns some/all σ such that $KB \models S\sigma$

Knowledge base for the wumpus world



“Perception”

$\forall b, g, t \text{ Percept}([Smell, b, g], t) \Rightarrow Smelt(t)$

$\forall s, b, t \text{ Percept}([s, b, Glitter], t) \Rightarrow AtGold(t)$

Reflex: $\forall t \text{ AtGold}(t) \Rightarrow \text{Action}(Grab, t)$

Reflex with internal state: do we have the gold already?

$\forall t \text{ AtGold}(t) \wedge \neg Holding(Gold, t) \Rightarrow \text{Action}(Grab, t)$

$Holding(Gold, t)$ cannot be observed

\Rightarrow keeping track of change is essential

Deducing hidden properties



Properties of locations:

$$\forall x, t \text{ At}(\text{Agent}, x, t) \wedge \text{Smelt}(t) \Rightarrow \text{Smelly}(x)$$

$$\forall x, t \text{ At}(\text{Agent}, x, t) \wedge \text{Breeze}(t) \Rightarrow \text{Breezy}(x)$$

Squares are breezy near a pit:

Diagnostic rule—infer cause from effect

$$\forall y \text{ Breezy}(y) \Rightarrow \exists x \text{ Pit}(x) \wedge \text{Adjacent}(x, y)$$

Causal rule—infer effect from cause

$$\forall x, y \text{ Pit}(x) \wedge \text{Adjacent}(x, y) \Rightarrow \text{Breezy}(y)$$

Neither of these is complete—e.g., the causal rule doesn't say whether squares far away from pits can be breezy

Definition for the *Breezy* predicate:

$$\forall y \text{ Breezy}(y) \Leftrightarrow [\exists x \text{ Pit}(x) \wedge \text{Adjacent}(x, y)]$$

Keeping track of change

Facts hold in **situations**, rather than eternally

E.g., *Holding(Gold, Now)* rather than just *Holding(Gold)*

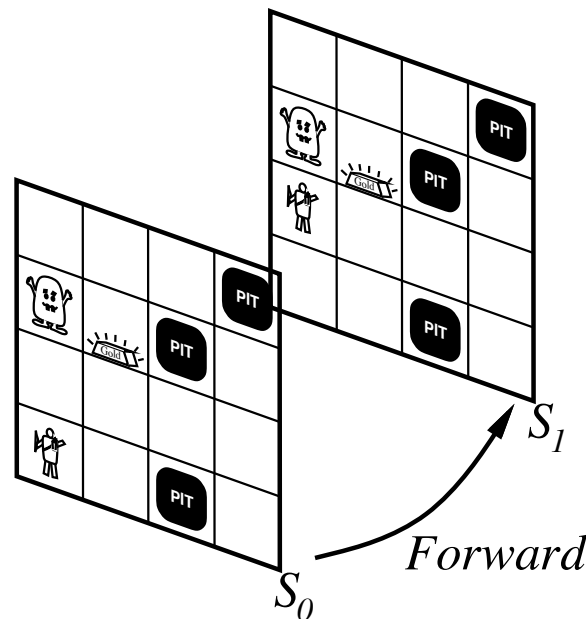
Situation calculus is one way to represent change in FOL:

Adds a situation argument to each non-eternal predicate

E.g., *Now* in *Holding(Gold, Now)* denotes a situation

Situations are connected by the *Result* function

Result(a, s) is the situation that results from doing *a* in *s*



Describing actions I

“Effect” axiom—describe changes due to action

$$\forall s \text{ AtGold}(s) \Rightarrow \text{Holding}(\text{Gold}, \text{Result}(\text{Grab}, s))$$

“Frame” axiom—describe **non-changes** due to action

$$\forall s \text{ HaveArrow}(s) \Rightarrow \text{HaveArrow}(\text{Result}(\text{Grab}, s))$$

Frame problem: find an elegant way to handle non-change

- (a) representation—avoid frame axioms
- (b) inference—avoid repeated “copy-overs” to keep track of state

Qualification problem: true descriptions of real actions require endless caveats—what if gold is slippery or nailed down or ...

Ramification problem: real actions have many secondary consequences—what about the dust on the gold, wear and tear on gloves, ...

Describing actions II



Successor-state axioms solve the representational frame problem

Each axiom is “about” a **predicate** (not an action per se):

$$\begin{aligned} P \text{ true afterwards} &\Leftrightarrow [\text{an action made } P \text{ true} \\ &\vee P \text{ true already and no action made } P \text{ false}] \end{aligned}$$

For holding the gold:

$$\begin{aligned} \forall a, s \text{ Holding}(\text{Gold}, \text{Result}(a, s)) &\Leftrightarrow \\ &[(a = \text{Grab} \wedge \text{AtGold}(s)) \\ &\vee (\text{Holding}(\text{Gold}, s) \wedge a \neq \text{Release})] \end{aligned}$$

Making plans



Initial condition in KB:

$At(Agent, [1, 1], S_0)$

$At(Gold, [1, 2], S_0)$

Query: $Ask(KB, \exists s \text{ Holding}(Gold, s))$

i.e., in what situation will I be holding the gold?

Answer: $\{s / Result(Grab, Result(Forward, S_0))\}$

i.e., go forward and then grab the gold

This assumes that the agent is interested in plans starting at S_0 and that S_0 is the only situation described in the KB

Making plans: A better way



Represent **plans** as action sequences $[a_1, a_2, \dots, a_n]$

$PlanResult(p, s)$ is the result of executing p in s

Then the query $Ask(KB, \exists p \text{ Holding}(Gold, PlanResult(p, S_0)))$
has the solution $\{p/[Forward, Grab]\}$

Definition of $PlanResult$ in terms of $Result$:

$$\forall s \text{ PlanResult}([], s) = s$$

$$\forall a, p, s \text{ PlanResult}([a|p], s) = \text{PlanResult}(p, \text{Result}(a, s))$$

Planning systems are special-purpose reasoners designed to do this type of inference more efficiently than a general-purpose reasoner

Summary



First-order logic:

- objects and relations are semantic primitives
- syntax: constants, functions, predicates, equality, quantifiers

Increased expressive power: sufficient to define wumpus world

Situation calculus:

- conventions for describing actions and change in FOL
- can formulate planning as inference on a situation calculus KB

A brief history of reasoning



450B.C.	Stoics	propositional logic, inference (maybe)
322B.C.	Aristotle	“syllogisms” (inference rules), quantifiers
1565	Cardano	probability theory (propositional logic + uncertainty)
1847	Boole	propositional logic (again)
1879	Frege	first-order logic
1922	Wittgenstein	proof by truth tables
1930	Gödel	\exists complete algorithm for FOL
1930	Herbrand	complete algorithm for FOL (reduce to propositional)
1931	Gödel	$\neg\exists$ complete algorithm for arithmetic
1960	Davis/Putnam	“practical” algorithm for propositional logic
1965	Robinson	“practical” algorithm for FOL—resolution

Universal instantiation (UI)



Every instantiation of a universally quantified sentence is entailed by it:

$$\frac{\forall v \alpha}{\text{SUBST}(\{v/g\}, \alpha)}$$

for any variable v and ground term g

E.g., $\forall x \text{ King}(x) \wedge \text{Greedy}(x) \Rightarrow \text{Evil}(x)$ yields

$$\text{King}(\text{John}) \wedge \text{Greedy}(\text{John}) \Rightarrow \text{Evil}(\text{John})$$

$$\text{King}(\text{Richard}) \wedge \text{Greedy}(\text{Richard}) \Rightarrow \text{Evil}(\text{Richard})$$

$$\text{King}(\text{Father}(\text{John})) \wedge \text{Greedy}(\text{Father}(\text{John})) \Rightarrow \text{Evil}(\text{Father}(\text{John}))$$

Existential instantiation (EI)

For any sentence α , variable v , and constant symbol k that does not appear elsewhere in the knowledge base:

$$\frac{\exists v \alpha}{\text{SUBST}(\{v/k\}, \alpha)}$$

E.g., $\exists x \text{Crown}(x) \wedge \text{OnHead}(x, \text{John})$ yields

$$\text{Crown}(C_1) \wedge \text{OnHead}(C_1, \text{John})$$

provided C_1 is a new constant symbol, called a Skolem constant

Another example: from $\exists x \text{d}(x^y)/\text{d}y = x^y$ we obtain

$$\text{d}(e^y)/\text{d}y = e^y$$

provided e is a new constant symbol

Instantiation



UI can be applied several times to **add** new sentences;
the new KB is logically equivalent to the old

EI can be applied once to **replace** the existential sentence;
the new KB is **not** equivalent to the old,
but is satisfiable iff the old KB was satisfiable

Reduction to propositional inference



Suppose the KB contains just the following:

$\forall x \text{ King}(x) \wedge \text{Greedy}(x) \Rightarrow \text{Evil}(x)$

$\text{King}(\text{John})$

$\text{Greedy}(\text{John})$

$\text{Brother}(\text{Richard}, \text{John})$

Instantiating the universal sentence in **all possible** ways, we have

$\text{King}(\text{John}) \wedge \text{Greedy}(\text{John}) \Rightarrow \text{Evil}(\text{John})$

$\text{King}(\text{Richard}) \wedge \text{Greedy}(\text{Richard}) \Rightarrow \text{Evil}(\text{Richard})$

$\text{King}(\text{John})$

$\text{Greedy}(\text{John})$

$\text{Brother}(\text{Richard}, \text{John})$

The new KB is **propositionalized**: proposition symbols are

$\text{King}(\text{John}), \text{Greedy}(\text{John}), \text{Evil}(\text{John}), \text{King}(\text{Richard})$ etc.

Reduction to propositional inference



Claim: a ground sentence* is entailed by new KB iff entailed by original KB

Claim: every FOL KB can be propositionalized so as to preserve entailment

Idea: propositionalize KB and query, apply resolution, return result

Problem: with function symbols, there are infinitely many ground terms,
e.g., *Father(Father(Father(John)))*

Theorem: Herbrand (1930). If a sentence α is entailed by an FOL KB,
it is entailed by a **finite** subset of the propositional KB

Idea: For $n = 0$ to ∞ do
 create a propositional KB by instantiating with depth- n terms
 see if α is entailed by this KB

Problem: works if α is entailed, loops if α is not entailed

Theorem: Turing (1936), Church (1936), entailment in FOL is **semidecidable**

Problems with propositionalization



Propositionalization seems to generate lots of irrelevant sentences.

E.g., from

$\forall x \text{ King}(x) \wedge \text{Greedy}(x) \Rightarrow \text{Evil}(x)$

$\text{King}(\text{John})$

$\forall y \text{ Greedy}(y)$

$\text{Brother}(\text{Richard}, \text{John})$

it seems obvious that $\text{Evil}(\text{John})$, but propositionalization produces lots of facts such as $\text{Greedy}(\text{Richard})$ that are irrelevant

With p k -ary predicates and n constants, there are $p \cdot n^k$ instantiations

With function symbols, it gets much much worse!

Unification



We can get the inference immediately if we can find a substitution θ such that $King(x)$ and $Greedy(x)$ match $King(John)$ and $Greedy(y)$

$\theta = \{x/John, y/John\}$ works

$UNIFY(\alpha, \beta) = \theta$ if $\alpha\theta = \beta\theta$

p	q	θ
$Knows(John, x)$	$Knows(John, Jane)$	$\{x/Jane\}$
$Knows(John, x)$	$Knows(y, OJ)$	$\{x/OJ, y/John\}$
$Knows(John, x)$	$Knows(y, Mother(y))$	$\{y/John, x/Mother(John)\}$
$Knows(John, x)$	$Knows(x, OJ)$	<i>fail</i>

Standardizing apart eliminates overlap of variables, e.g., $Knows(z_{17}, OJ)$

Generalized Modus Ponens (GMP)



(前件推理)

$$\frac{p_1', p_2', \dots, p_n', (p_1 \wedge p_2 \wedge \dots \wedge p_n \Rightarrow q)}{q\theta}$$

where $p_i'\theta = p_i\theta$ for all i

p_1' is *King(John)* p_1 is *King(x)*
 p_2' is *Greedy(y)* p_2 is *Greedy(x)*
 θ is $\{x/\text{John}, y/\text{John}\}$ q is *Evil(x)*
 $q\theta$ is *Evil(John)*

GMP used with KB of definite clauses (**exactly** one positive literal)

All variables assumed universally quantified

Soundness of GMP



Need to show that

$$p_1', \dots, p_n', (p_1 \wedge \dots \wedge p_n \Rightarrow q) \models q\theta$$

provided that $p_i'\theta = p_i\theta$ for all i

Lemma: For any definite clause p , we have $p \models p\theta$ by UI

1. $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \models (p_1 \wedge \dots \wedge p_n \Rightarrow q)\theta = (p_1\theta \wedge \dots \wedge p_n\theta \Rightarrow q\theta)$
2. $p_1', \dots, p_n' \models p_1' \wedge \dots \wedge p_n' \models p_1'\theta \wedge \dots \wedge p_n'\theta$
3. From 1 and 2, $q\theta$ follows by ordinary Modus Ponens

Example knowledge base



The law says that it is a crime for an American to sell weapons to hostile nations. The country Nono, an enemy of America, has some missiles, and all of its missiles were sold to it by Colonel West, who is American.

Prove that Col. West is a criminal

... it is a crime for an American to sell weapons to hostile nations:

$$\textit{American}(x) \wedge \textit{Weapon}(y) \wedge \textit{Sells}(x, y, z) \wedge \textit{Hostile}(z) \Rightarrow \textit{Criminal}(x)$$

Nono ... has some missiles, i.e., $\exists x \textit{Owns}(\textit{Nono}, x) \wedge \textit{Missile}(x)$:

$$\textit{Owns}(\textit{Nono}, M_1) \text{ and } \textit{Missile}(M_1)$$

... all of its missiles were sold to it by Colonel West

$$\forall x \textit{Missile}(x) \wedge \textit{Owns}(\textit{Nono}, x) \Rightarrow \textit{Sells}(\textit{West}, x, \textit{Nono})$$

Missiles are weapons:

$$\textit{Missile}(x) \Rightarrow \textit{Weapon}(x)$$

An enemy of America counts as "hostile":

$$\textit{Enemy}(x, \textit{America}) \Rightarrow \textit{Hostile}(x)$$

West, who is American ...

$$\textit{American}(\textit{West})$$

The country Nono, an enemy of America ...

$$\textit{Enemy}(\textit{Nono}, \textit{America})$$

Forward chaining algorithm

function FOL-FC-Ask(KB, α) **returns** a substitution or *false*

repeat until new is empty

$new \leftarrow \{ \}$

for each sentence r **in** KB **do**

$(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-APART}(r)$

for each θ such that $(p_1 \wedge \dots \wedge p_n)\theta = (p'_1 \wedge \dots \wedge p'_n)\theta$

for some p'_1, \dots, p'_n in KB

$q' \leftarrow \text{SUBST}(\theta, q)$

if q' is not a renaming of a sentence already in KB or new **then do**

add q' to new

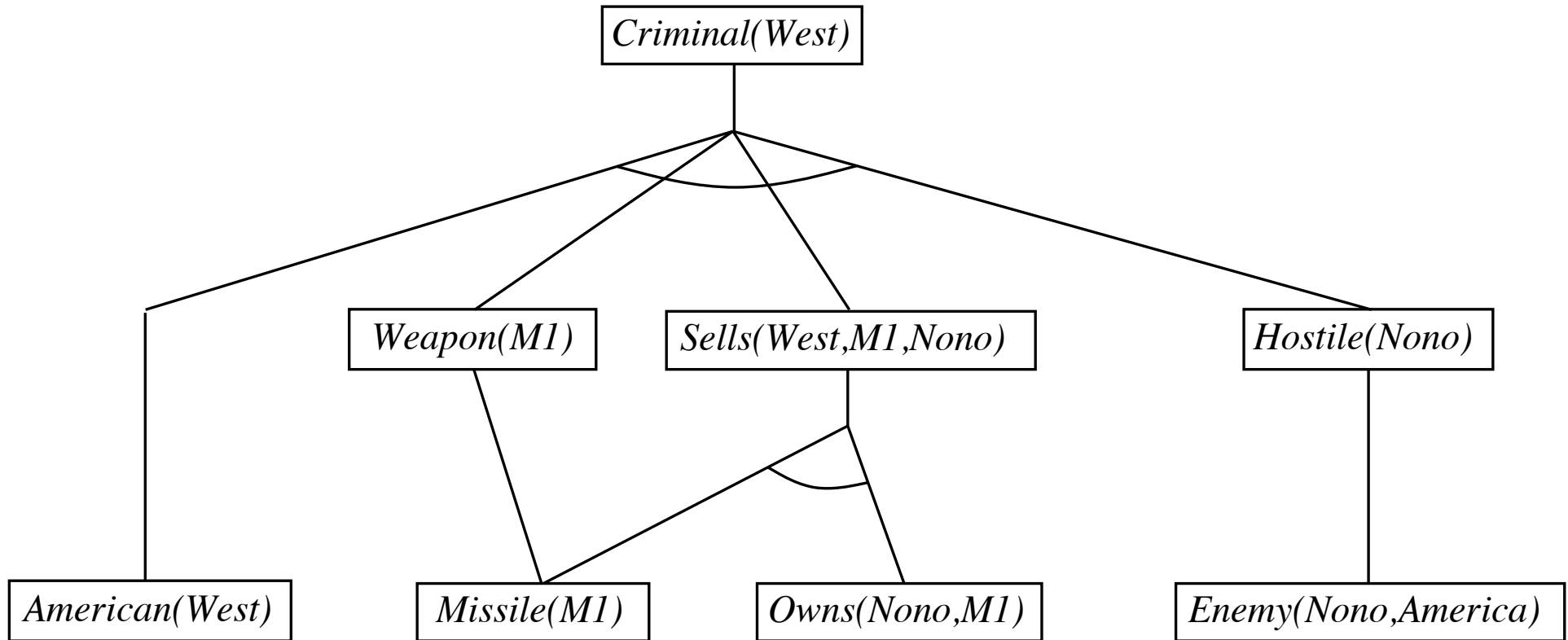
$\phi \leftarrow \text{UNIFY}(q', \alpha)$

if ϕ is not *fail* **then return** ϕ

add new to KB

return *false*

Forward chaining proof



Properties of forward chaining



Sound and complete for first-order definite clauses
(proof similar to propositional proof)

Datalog = first-order definite clauses + **no functions** (e.g., crime KB)
FC terminates for Datalog in poly iterations: at most $p \cdot n^k$ literals

May not terminate in general if α is not entailed

This is unavoidable: entailment with definite clauses is semidecidable

Efficiency of forward chaining



Simple observation: no need to match a rule on iteration k
if a premise wasn't added on iteration $k - 1$

\Rightarrow match each rule whose premise contains a newly added literal

Matching itself can be expensive

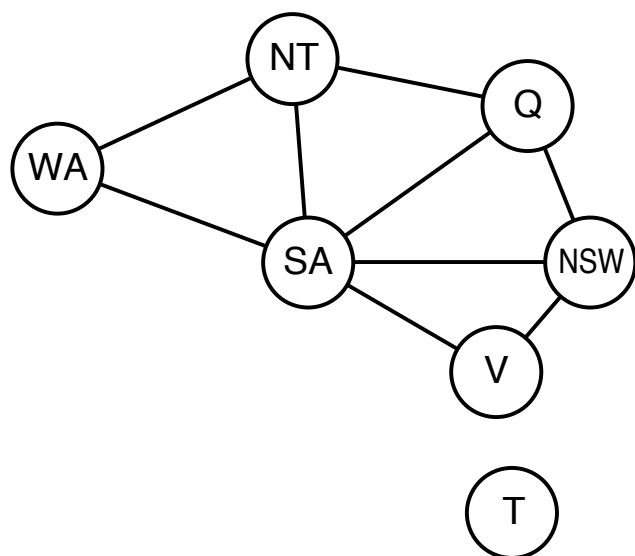
Database indexing allows $O(1)$ retrieval of known facts

e.g., query $Missile(x)$ retrieves $Missile(M_1)$

Matching conjunctive premises against known facts is NP-hard

Forward chaining is widely used in deductive databases

Hard matching example



$$\begin{aligned} & Diff(wa, nt) \wedge Diff(wa, sa) \wedge \\ & Diff(nt, q) Diff(nt, sa) \wedge \\ & Diff(q, nsw) \wedge Diff(q, sa) \wedge \\ & Diff(nsw, v) \wedge Diff(nsw, sa) \wedge \\ & Diff(v, sa) \Rightarrow Colorable() \end{aligned}$$

$$\begin{aligned} & Diff(Red, Blue) \quad Diff(Red, Green) \\ & Diff(Green, Red) \quad Diff(Green, Blue) \\ & Diff(Blue, Red) \quad Diff(Blue, Green) \end{aligned}$$

Colorable() is inferred iff the CSP has a solution

CSPs include 3SAT as a special case, hence matching is NP-hard

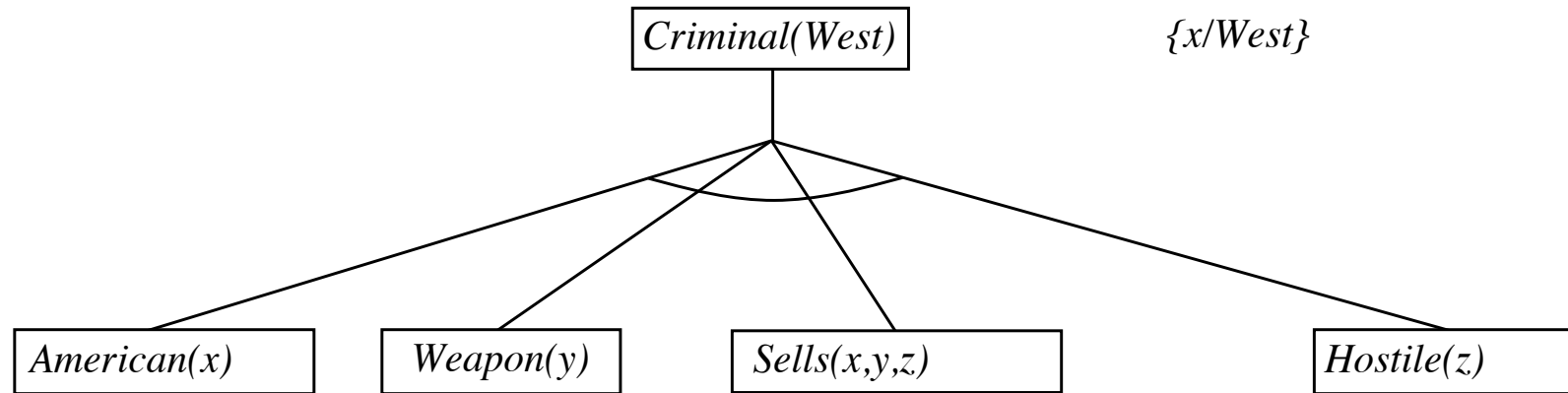
Backward chaining algorithm



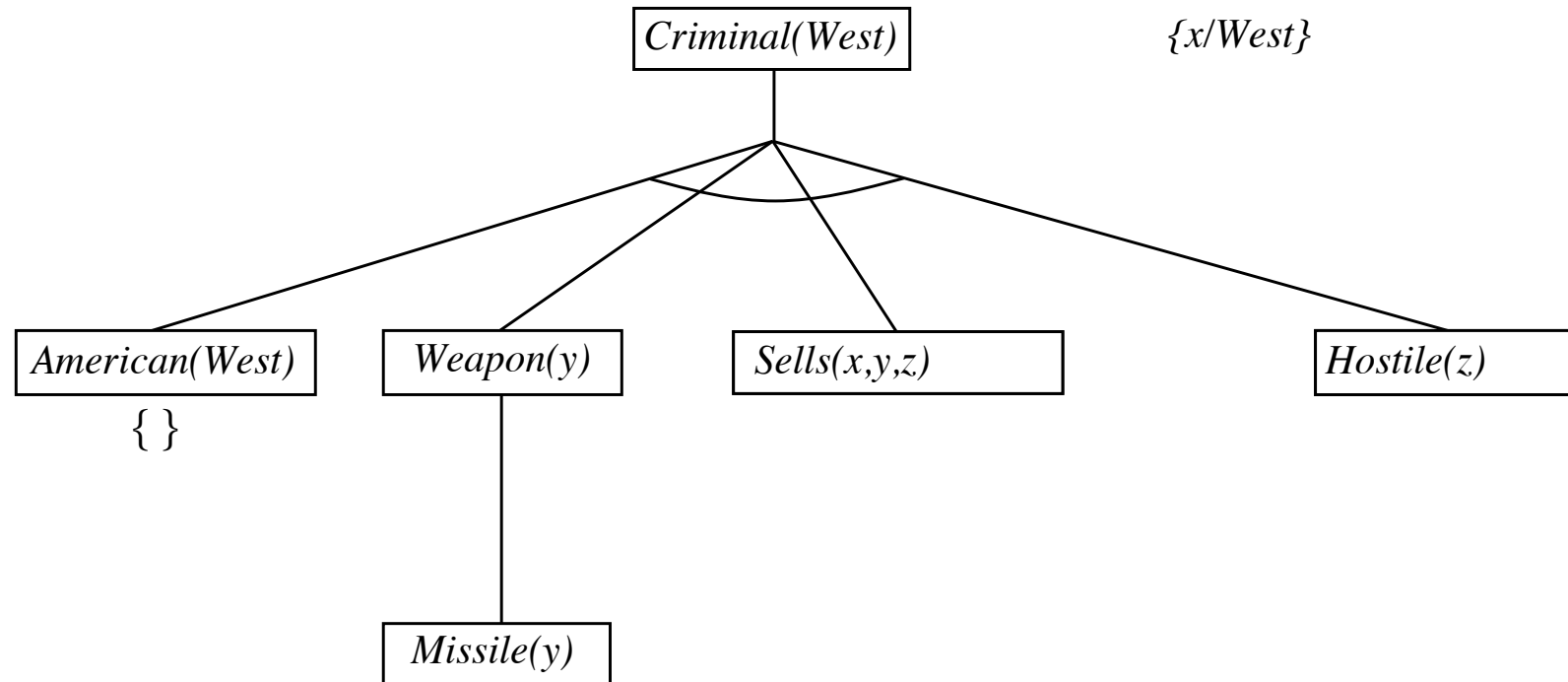
```
function FOL-BC-ASK(KB, goals,  $\theta$ ) returns a set of substitutions
  inputs: KB, a knowledge base
            goals, a list of conjuncts forming a query ( $\theta$  already applied)
             $\theta$ , the current substitution, initially the empty substitution  $\{ \}$ 
  local variables: answers, a set of substitutions, initially empty

  if goals is empty then return  $\{ \theta \}$ 
   $q' \leftarrow \text{SUBST}(\theta, \text{FIRST}(\textit{goals}))$ 
  for each sentence r in KB
    where  $\text{STANDARDIZE-APART}(r) = (p_1 \wedge \dots \wedge p_n \Rightarrow q)$ 
    and  $\theta' \leftarrow \text{UNIFY}(q, q')$  succeeds
     $\textit{new\_goals} \leftarrow [p_1, \dots, p_n | \text{REST}(\textit{goals})]$ 
     $\textit{answers} \leftarrow \text{FOL-BC-ASK}(\textit{KB}, \textit{new\_goals}, \text{COMPOSE}(\theta', \theta)) \cup \textit{answers}$ 
  return answers
```

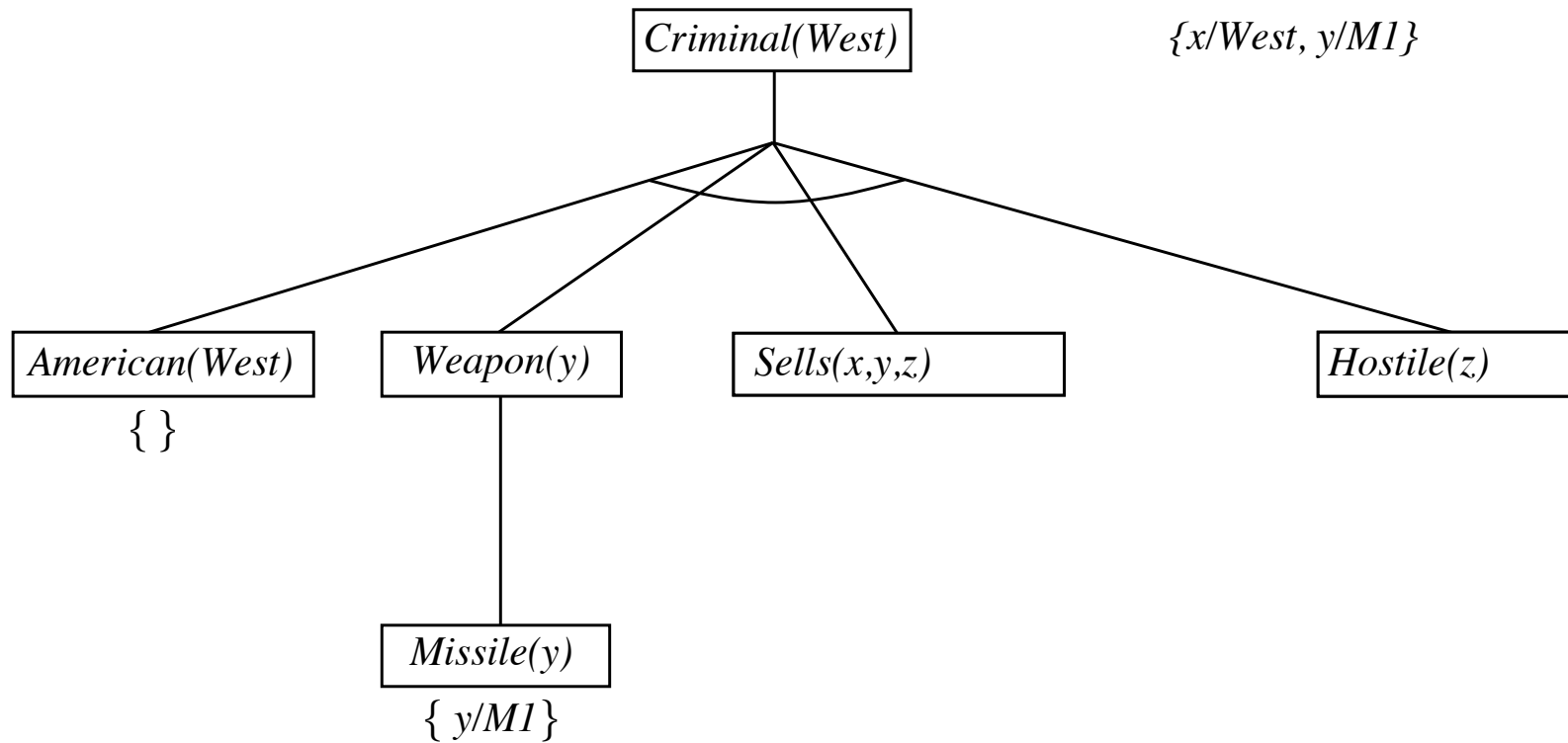
Backward chaining example



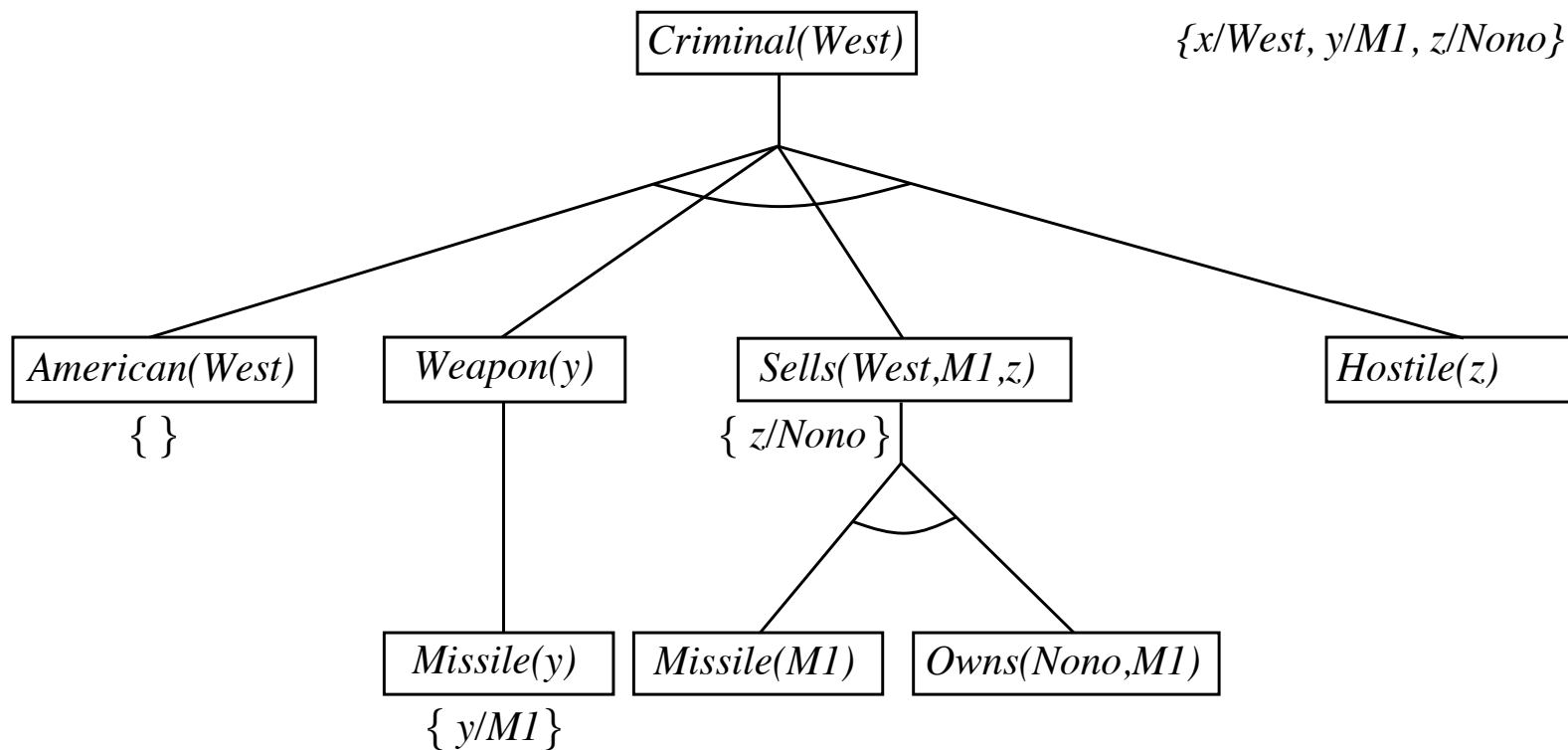
Backward chaining example



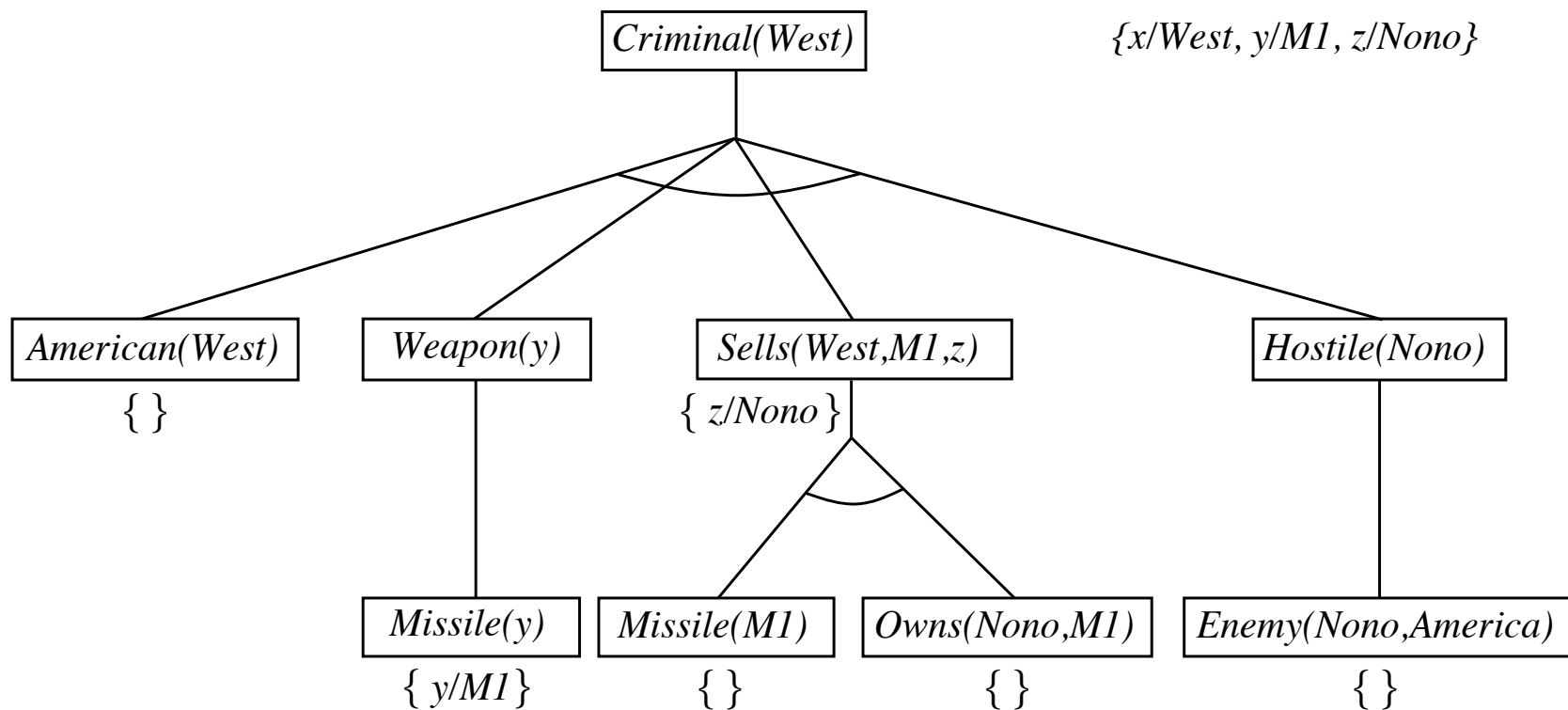
Backward chaining example



Backward chaining example



Backward chaining example



Properties of backward chaining



Depth-first recursive proof search: space is linear in size of proof

Incomplete due to infinite loops

⇒ fix by checking current goal against every goal on stack

Inefficient due to repeated subgoals (both success and failure)

⇒ fix using caching of previous results (extra space!)

Widely used (without improvements!) for **logic programming**

Logic programming



Sound bite: computation as inference on logical KBs

Logic programming

1. Identify problem
2. Assemble information
3. Tea break
4. Encode information in KB
5. Encode problem instance as facts
6. Ask queries
7. Find false facts

Ordinary programming

- Identify problem
- Assemble information
- Figure out solution
- Program solution
- Encode problem instance as data
- Apply program to data
- Debug procedural errors

Should be easier to debug *Capital(NewYork, US)* than $x := x + 2$!

Prolog systems



Basis: backward chaining with Horn clauses + bells & whistles
Widely used in Europe, Japan (basis of 5th Generation project)
Compilation techniques \Rightarrow approaching a billion LIPS

Program = set of clauses = head :- literal₁, ... literal_n.

`criminal(X) :- american(X), weapon(Y), sells(X,Y,Z), hostile(Z).`

Efficient unification by [open coding](#)

Efficient retrieval of matching clauses by direct linking

Depth-first, left-to-right backward chaining

Built-in predicates for arithmetic etc., e.g., `X is Y*Z+3`

Closed-world assumption (“negation as failure”)

e.g., given `alive(X) :- not dead(X).`

`alive(joe)` succeeds if `dead(joe)` fails

Prolog examples



Depth-first search from a start state X:

```
dfs(X) :- goal(X).  
dfs(X) :- successor(X,S), dfs(S).
```

No need to loop over S: successor succeeds for each

Appending two lists to produce a third:

```
append([], Y, Y).  
append([X|L], Y, [X|Z]) :- append(L, Y, Z).
```

query: append(A, B, [1, 2]) ?

answers: A=[] B=[1, 2]

A=[1] B=[2]

A=[1, 2] B=[]

Prolog example

Let's try

```
member(1,[1,2,3,4,5])
```

```
query: grandfather(X,yuqing)?
```

```
male(di).
```

```
male(jianbo).
```

```
female(xin).
```

```
female(yuan).
```

```
female(yuqing).
```

```
father(jianbo,di).
```

```
father(di,yuqing).
```

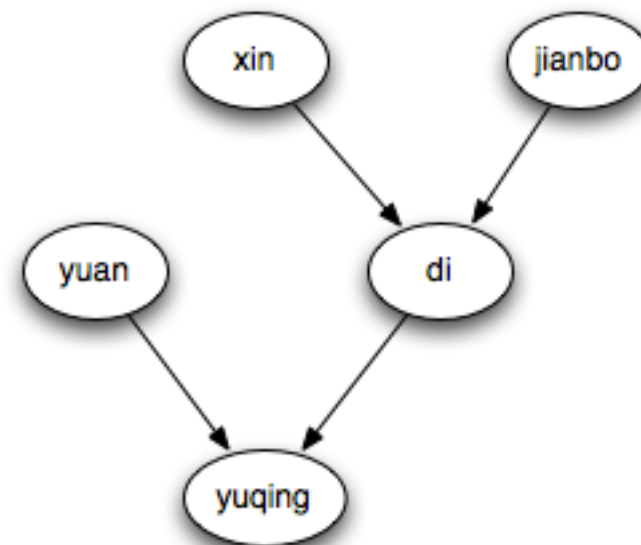
```
mother(xin,di).
```

```
mother(yuan,yuqing).
```

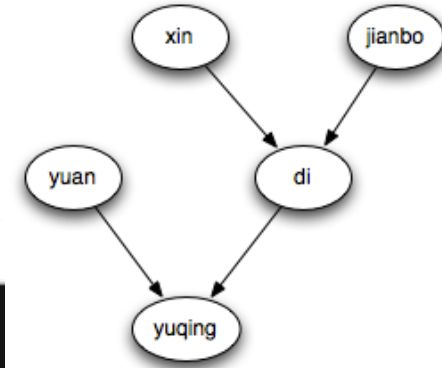
```
grandfather(X,Y):-father(X,Z),father(Z,Y).
```

```
grandmother(X,Y):-mother(X,Z),father(Z,Y).
```

```
daughter(X,Y):-father(X,Y),female(Y).
```



Prolog example



```
eyounxRMBP15:AI17 yuy$ █
```

Resolution: brief summary



Full first-order version:

$$\frac{\ell_1 \vee \cdots \vee \ell_k, \quad m_1 \vee \cdots \vee m_n}{(\ell_1 \vee \cdots \vee \ell_{i-1} \vee \ell_{i+1} \vee \cdots \vee \ell_k \vee m_1 \vee \cdots \vee m_{j-1} \vee m_{j+1} \vee \cdots \vee m_n)\theta}$$

where $\text{UNIFY}(\ell_i, \neg m_j) = \theta$.

For example,

$$\frac{\neg Rich(x) \vee Unhappy(x) \quad Rich(Ken)}{Unhappy(Ken)}$$

with $\theta = \{x/Ken\}$

Apply resolution steps to $CNF(KB \wedge \neg\alpha)$; complete for FOL

Conversion to CNF



Everyone who loves all animals is loved by someone:

$$\forall x [\forall y \text{ Animal}(y) \Rightarrow \text{Loves}(x, y)] \Rightarrow [\exists y \text{ Loves}(y, x)]$$

1. Eliminate biconditionals and implications

$$\forall x [\neg \forall y \neg \text{Animal}(y) \vee \text{Loves}(x, y)] \vee [\exists y \text{ Loves}(y, x)]$$

2. Move \neg inwards: $\neg \forall x, p \equiv \exists x \neg p$, $\neg \exists x, p \equiv \forall x \neg p$:

$$\forall x [\exists y \neg(\neg \text{Animal}(y) \vee \text{Loves}(x, y))] \vee [\exists y \text{ Loves}(y, x)]$$

$$\forall x [\exists y \neg \neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y)] \vee [\exists y \text{ Loves}(y, x)]$$

$$\forall x [\exists y \text{ Animal}(y) \wedge \neg \text{Loves}(x, y)] \vee [\exists y \text{ Loves}(y, x)]$$

Conversion to CNF



3. Standardize variables: each quantifier should use a different one

$$\forall x [\exists y \textit{Animal}(y) \wedge \neg \textit{Loves}(x, y)] \vee [\exists z \textit{Loves}(z, x)]$$

4. Skolemize: a more general form of existential instantiation.
Each existential variable is replaced by a **Skolem function** of the enclosing universally quantified variables:

$$\forall x [\textit{Animal}(F(x)) \wedge \neg \textit{Loves}(x, F(x))] \vee \textit{Loves}(G(x), x)$$

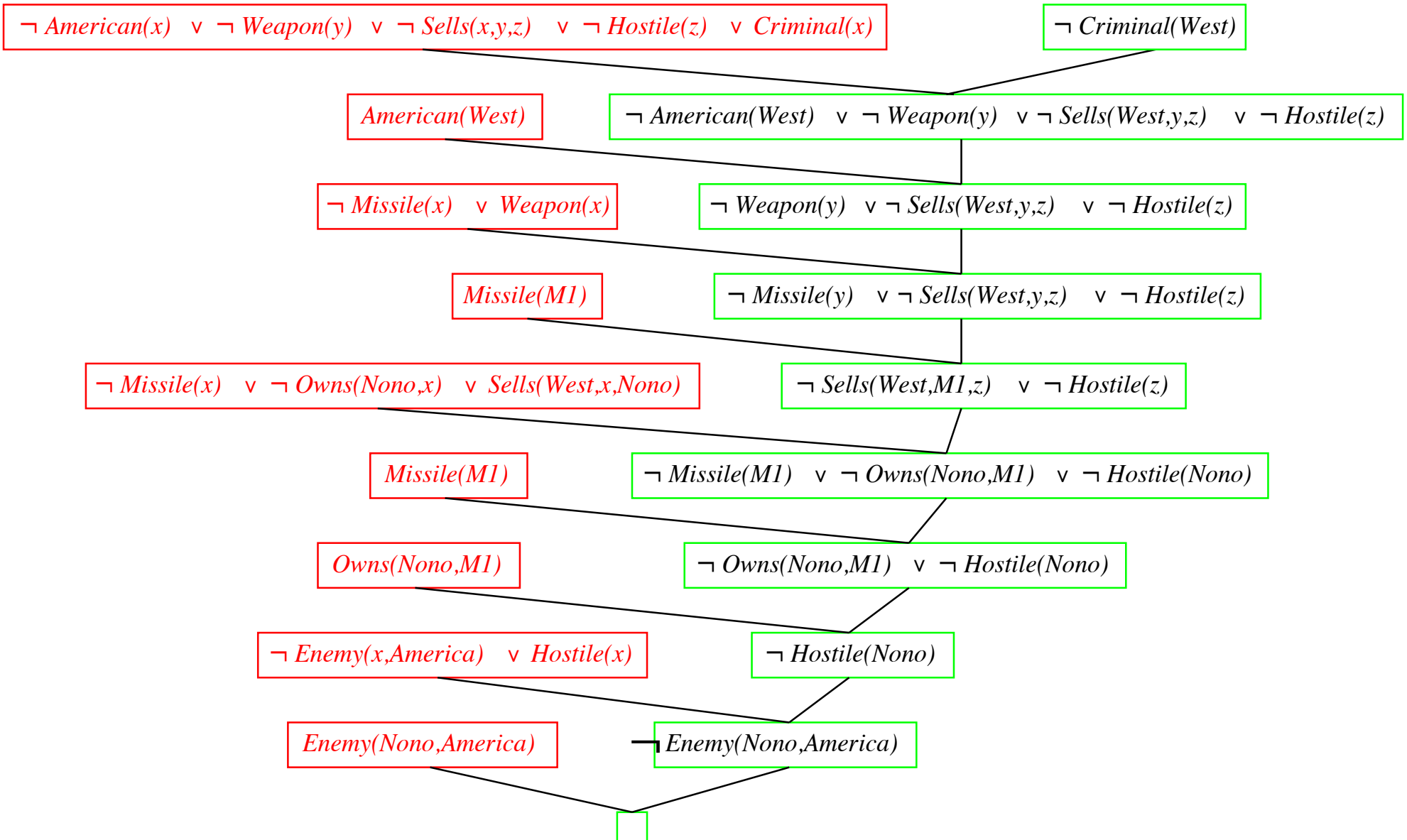
5. Drop universal quantifiers:

$$[\textit{Animal}(F(x)) \wedge \neg \textit{Loves}(x, F(x))] \vee \textit{Loves}(G(x), x)$$

6. Distribute \wedge over \vee :

$$[\textit{Animal}(F(x)) \vee \textit{Loves}(G(x), x)] \wedge [\neg \textit{Loves}(x, F(x)) \vee \textit{Loves}(G(x), x)]$$

Resolution proof: definite clauses



Previously...



Propositional Logic

PL-Forward chaining

PL-Backward chaining

PL-Resolution

First Order Logic (FOL)

Instantiation

FOL-Forward chaining

FOL-Backward chaining

FOL-Resolution

SAT problems



Propositional logic, CNF

literals: x_1, x_2, \dots, x_n

clauses: $(x_1 \vee x_2 \vee x_5) \quad (\neg x_2 \vee x_3 \vee \neg x_7) \quad \dots$

problem: find an assignment to literals so that the conjunction of the clauses is true, or prove unsatisfiable

$$(x_1 \vee x_2 \vee x_5) \wedge (\neg x_2 \vee x_3 \vee \neg x_7) \wedge \dots$$

2SAT: every clause has at most 2 literals

P-solvable

3SAT: every clause has at most 3 literals

NP-hard

SAT solvers



SAT problems have many important applications
many SAT solvers are ready for use

DPLL

WalkSAT

Davis–Putnam–Logemann–Loveland algorithm

function DPLL-SATISFIABLE?(*s*) **returns** *true* or *false*

inputs: *s*, a sentence in propositional logic

clauses \leftarrow the set of clauses in the CNF representation of *s*

symbols \leftarrow a list of the proposition symbols in *s*

return DPLL(*clauses*, *symbols*, { })

function DPLL(*clauses*, *symbols*, *model*) **returns** *true* or *false*

if every clause in *clauses* is true in *model* **then return** *true*

if some clause in *clauses* is false in *model* **then return** *false*

P, *value* \leftarrow FIND-PURE-SYMBOL(*symbols*, *clauses*, *model*)

if *P* is non-null **then return** DPLL(*clauses*, *symbols* – *P*, *model* \cup { *P*=*value* })

P, *value* \leftarrow FIND-UNIT-CLAUSE(*clauses*, *model*)

if *P* is non-null **then return** DPLL(*clauses*, *symbols* – *P*, *model* \cup { *P*=*value* })

P \leftarrow FIRST(*symbols*); *rest* \leftarrow REST(*symbols*)

return DPLL(*clauses*, *rest*, *model* \cup { *P*=*true* }) **or**

DPLL(*clauses*, *rest*, *model* \cup { *P*=*false* })

a deep-first search with heuristics

DPLL heuristics



Pure symbol heuristic: A **pure symbol** is a symbol that always appears with the same “sign” in all clauses.

$$(A \vee \neg B) \wedge (\neg B \vee \neg C) \wedge (C \vee A)$$

A and B is pure, but not C

Unit clause heuristic: A **unit clause** is a clause with just one literal.

$$(A \vee \neg B) \text{ with } A = \text{true}$$

is a unit clause

Other tricks



Component analysis : find disjoint subsets

Variable and value ordering : assign most frequent variable at first

Intelligent backtracking : remember conflicts

Random restart

Clever indexing

a local search hill-climbing or others.

```
function WALKSAT(clauses, p, max_flips) returns a satisfying model or failure  
inputs: clauses, a set of clauses in propositional logic  
         p, the probability of choosing to do a “random walk” move, typically around 0.5  
         max_flips, number of flips allowed before giving up  
  
model ← a random assignment of true/false to the symbols in clauses  
for i = 1 to max_flips do  
    if model satisfies clauses then return model  
    clause ← a randomly selected clause from clauses that is false in model  
    with probability p flip the value in model of a randomly selected symbol from clause  
    else flip whichever symbol in clause maximizes the number of satisfied clauses  
return failure
```

failure ≠ unsatisfiable

The landscape of random SAT problems



Not all SAT instances are hard
under-constraint: a few clauses => easy to enumerate
over-constraint: too many clauses => unsatisfiable

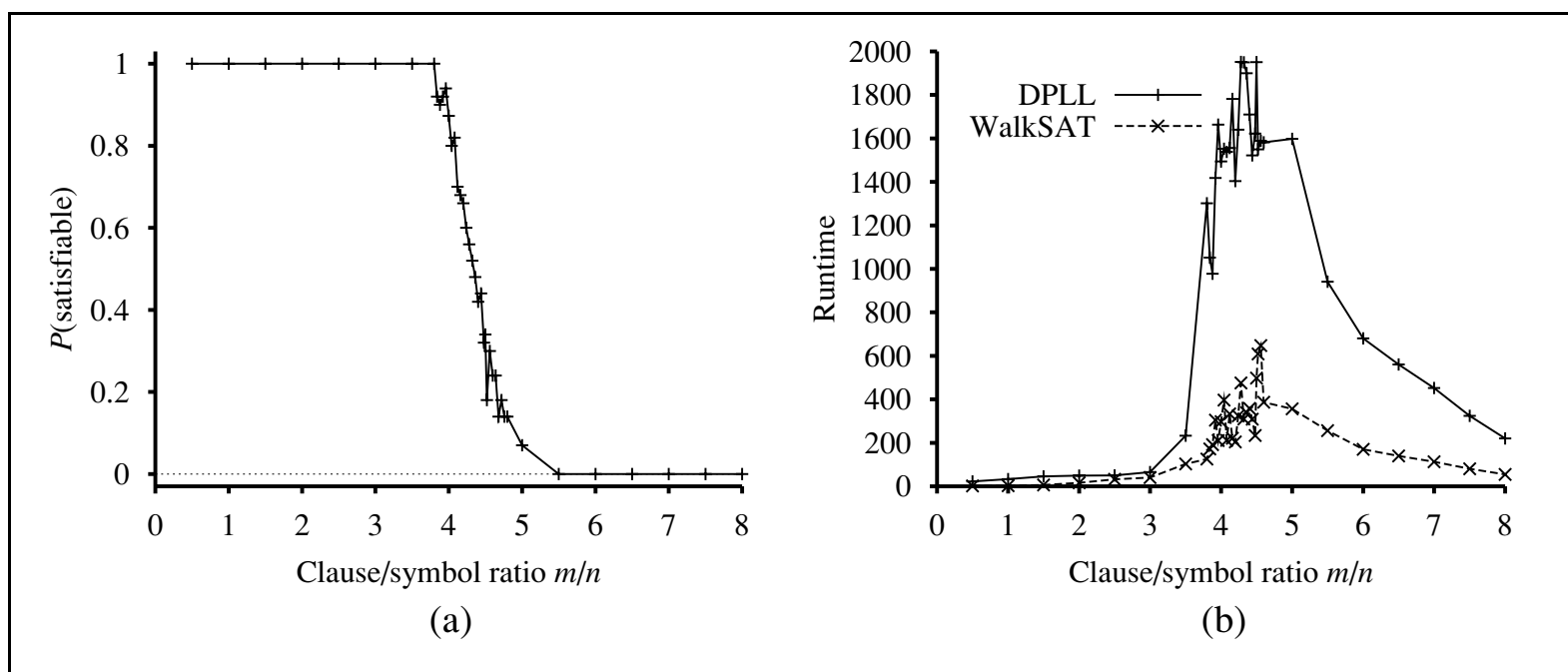


Figure 7.19 (a) Graph showing the probability that a random 3-CNF sentence with $n = 50$ symbols is satisfiable, as a function of the clause/symbol ratio m/n . (b) Graph of the median run time (measured in number of recursive calls to DPLL, a good proxy) on random 3-CNF sentences. The most difficult problems have a clause/symbol ratio of about 4.3.

Planning

There are many languages description the world
Planning Domain Definition Language
1.2, 2.1, 2.2, 3.0, 3.1

state s

Action(s)

Result(s, a)

Action(Fly($p, from, to$),

PRECOND: $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT: $\neg At(p, from) \wedge At(p, to)$

Action(Fly(P_1, SFO, JFK),

PRECOND: $At(P_1, SFO) \wedge Plane(P_1) \wedge Airport(SFO) \wedge Airport(JFK)$

EFFECT: $\neg At(P_1, SFO) \wedge At(P_1, JFK)$

Precondition



action **a** is **applicable** in state **s** if the preconditions are satisfied by **s**

$$(a \in \text{ACTIONS}(s)) \Leftrightarrow s \models \text{PRECOND}(a)$$

$$\forall p, from, to \ (Fly(p, from, to) \in \text{ACTIONS}(s)) \Leftrightarrow \\ s \models (At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to))$$

Result



removing the fluents that appear as negative literals in the action's effects (what we call the **delete list** or $\text{DEL}(\mathbf{a})$), and adding the fluents that are positive literals in the action's effects (what we call the **add list** or $\text{ADD}(\mathbf{a})$)

$$\text{RESULT}(s, a) = (s - \text{DEL}(a)) \cup \text{ADD}(a) .$$

Action(*Fly*(P_1 , *SFO*, *JFK*),

PRECOND: $At(P_1, SFO) \wedge Plane(P_1) \wedge Airport(SFO) \wedge Airport(JFK)$

EFFECT: $\neg At(P_1, SFO) \wedge At(P_1, JFK)$)

Example

$Init(On(A, Table) \wedge On(B, Table) \wedge On(C, A)$
 $\wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(B) \wedge Clear(C))$
 $Goal(On(A, B) \wedge On(B, C))$
 $Action(Move(b, x, y),$
 PRECOND: $On(b, x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge Block(y) \wedge$
 $(b \neq x) \wedge (b \neq y) \wedge (x \neq y),$
 EFFECT: $On(b, y) \wedge Clear(x) \wedge \neg On(b, x) \wedge \neg Clear(y))$
 $Action(MoveToTable(b, x),$
 PRECOND: $On(b, x) \wedge Clear(b) \wedge Block(b) \wedge (b \neq x),$
 EFFECT: $On(b, Table) \wedge Clear(x) \wedge \neg On(b, x))$

Figure 10.3 A planning problem in the blocks world: building a three-block tower. One solution is the sequence $[MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)]$.

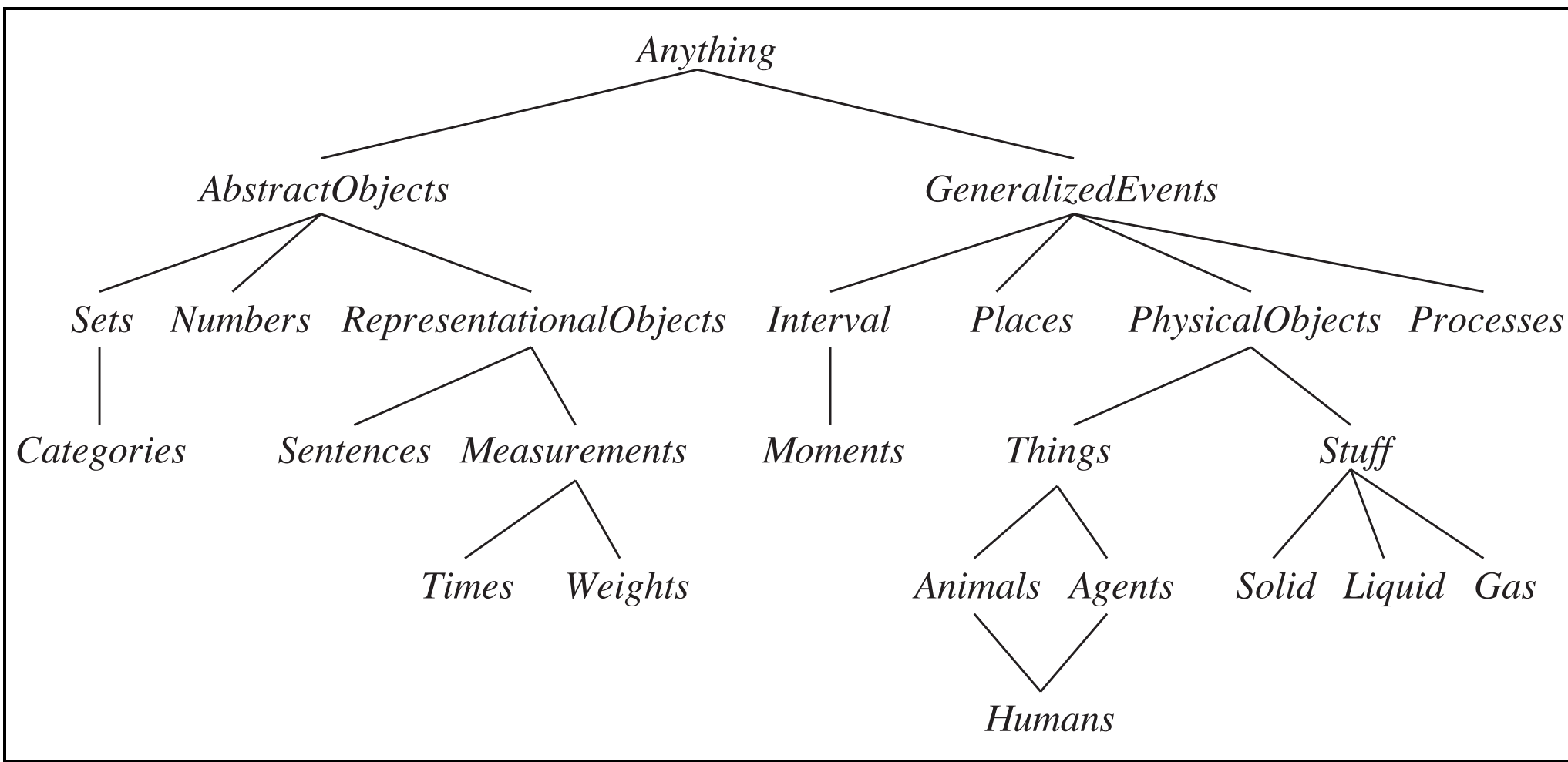


Figure 10.4 Diagram of the blocks-world problem in Figure 10.3.

Ontology and Semantic Web



Up ontology



Domain ontology

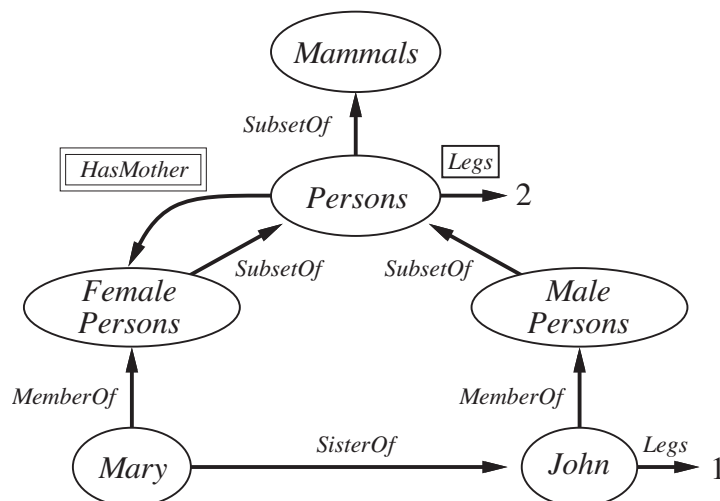


Figure 12.5 A semantic network with four objects (John, Mary, 1, and 2) and four categories. Relations are denoted by labeled links.

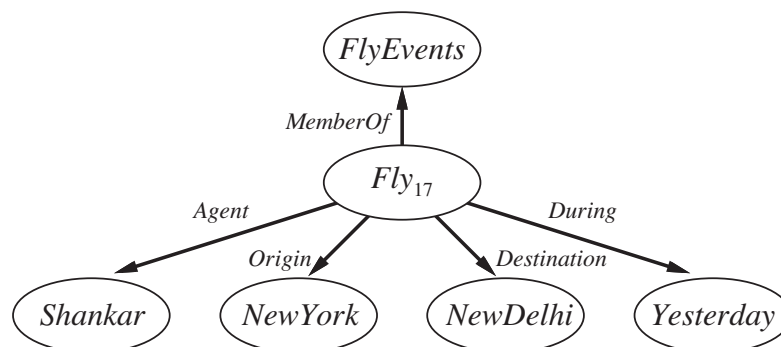


Figure 12.6 A fragment of a semantic network showing the representation of the logical assertion $Fly(Shankar, NewYork, NewDelhi, Yesterday)$.

Example: Wordnet



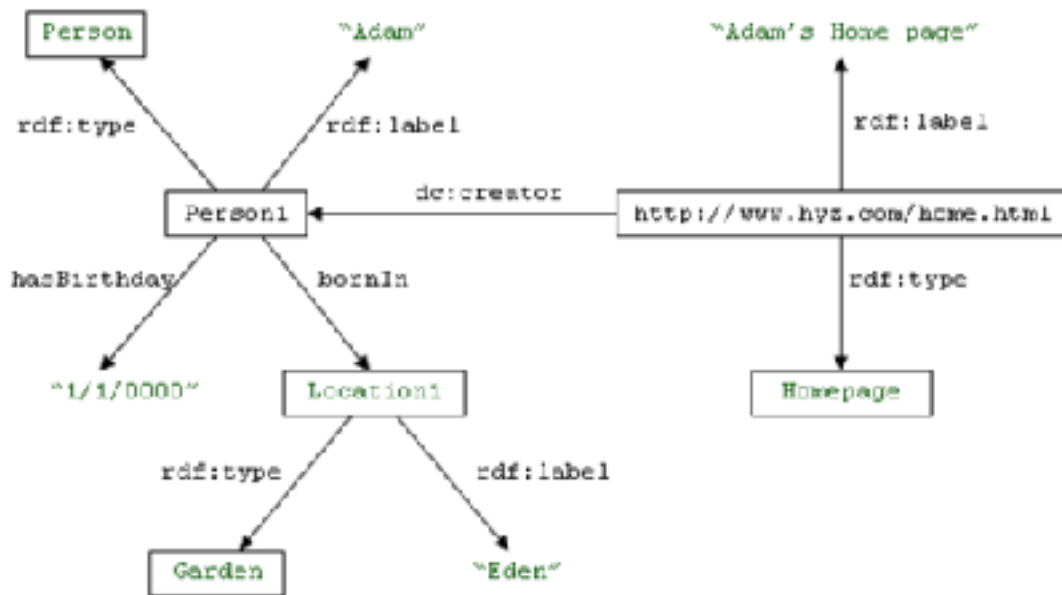
Hamburger

- Hamburger (an inhabitant of Hamburg)
 - direct hypernym:
 - German (a person of German nationality)
 - sister term
 - German (a person of German nationality)
 - East German (a native/inhabitant of the former GDR)
 - Bavarian (a native/inhabitant of Bavaria)
- derivationally related form
 - Hamburg (a port city in northern Germany on the Elbe River that was founded by Chalemagne in the...)

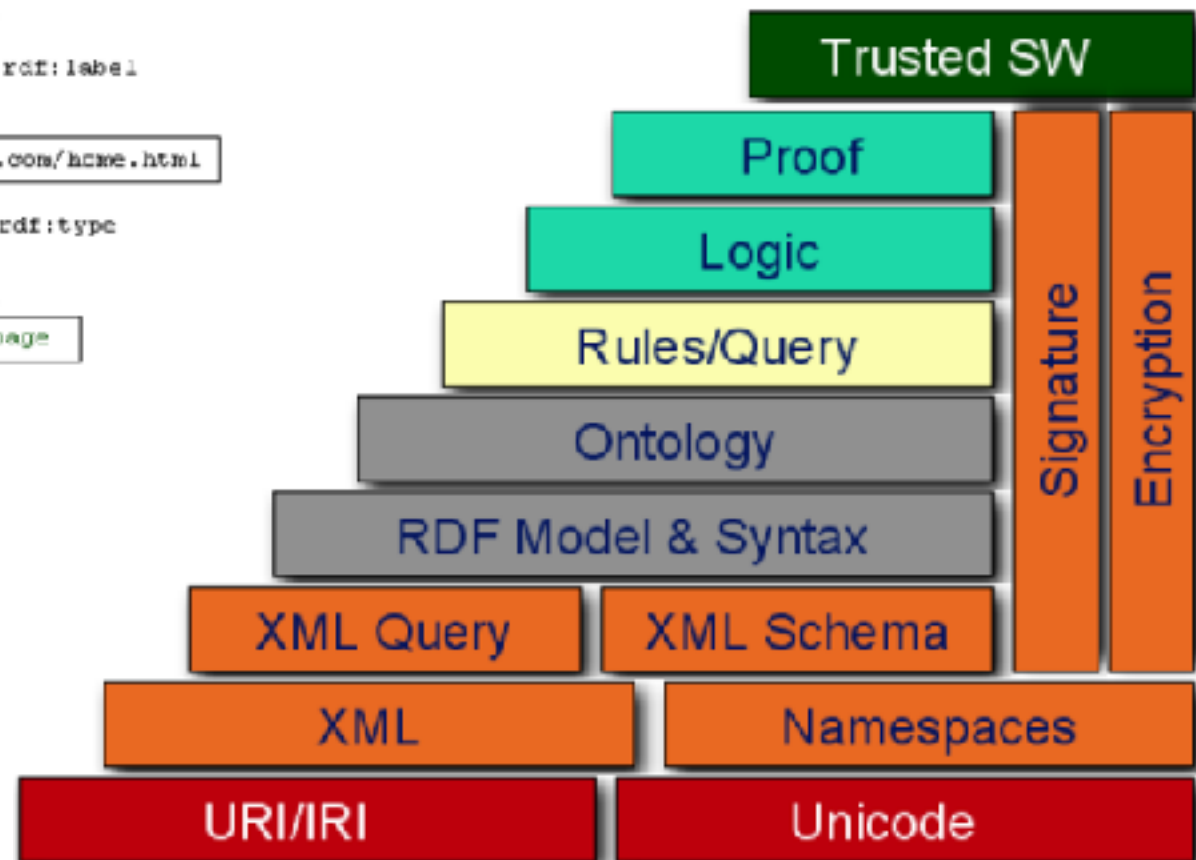
[from wikipedia]

Semantic web

- handling complex and heterogeneous information resources
- retrieving documents based on a set of relationships that are external to these documents
- providing multiple search options for richer investigation
- targeting and sifting results more efficiently
- using authoritative information resources more effectively as guides to searching



An RDF graph



Hey there! Are you maybe looking for [Freebase instead?](#)

Data Dumps

- Search
- Search Overview
- Search Cookbook
- Search Output
- Search Metaschema
- Search Widget

Data Dumps

⚠ The Freebase API will be completely shut-down on Aug 31, 2016. This page provides access to the last available data dump. [Read more](#)

Data Dumps are a downloadable version of the data in Freebase. They constitute a snapshot of the data stored in Freebase and the Schema that structures it, and are provided under the same CC-BY license. The Freebase/Wikidata mappings are provided under the CC0 license.

- 目录
- Freebase Triples
- Freebase Deleted Triples
- Freebase/Wikidata Mappings
- License
- Ching

Freebase Triples

This dataset contains every fact currently in Freebase.

Total triples: 1.9 billion

23 GB gzipped

[DOWNLOAD](#)

Updated: Weekly

Data Format: N-Triples

License: CC-BY

The RDF data is serialized using the N-Triples format, encoded as UTF-8.

RDF

```
<http://rdf.freebase.com/ns/g.11vjc1ym> <http://rdf.freebase.com/ns/g.11vjc1ym> <http://rdf.freebase.com/ns/g.11vjc1ym> <http://rdf.freebase.com/ns/g.11vjc1ym> <http://rdf.freebase.com/ns/g.11vjc1ym> <http://rdf.freebase.com/ns/g.11vjc1ym> <http://www.w
```

★ If you're writing your own code to parse the RDF dumps it's often more efficient to extract the data first and then processing the uncompressed data.

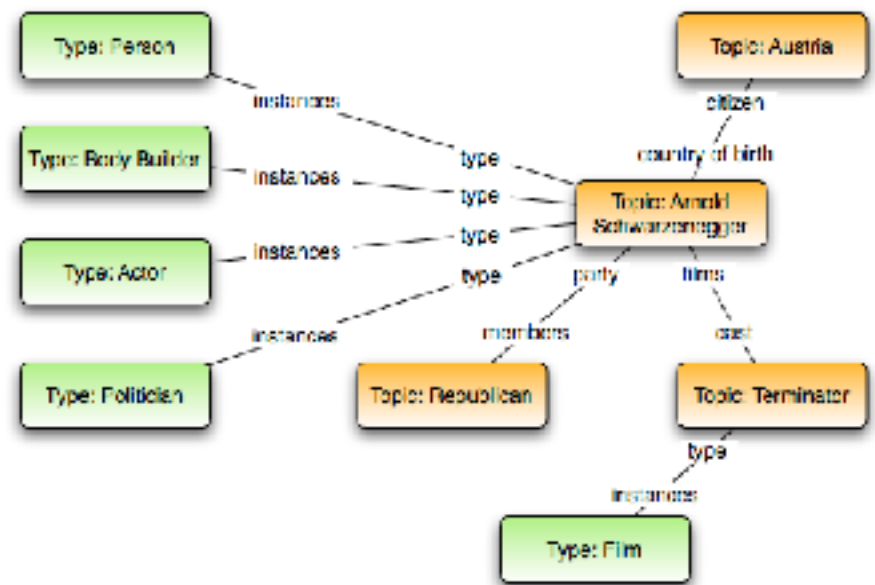
<subject> <predicate> <object> .

Note: In Freebase, objects have MIDs that look like /m/312rkp. In Freebase schema like /common/topic are written as common.topic

The subject is the ID of a Freebase object. It can be a Freebase MID readable ID (ex. /common.topic) for schema.

The predicate is always a human-readable ID for a Freebase property. [RDFS](#). Freebase foreign key namespaces are also used as predicates to make it easier to look up keys by namespace.

The object field may contain a Freebase MID for an object or a human-readable ID for schema from Freebase or other RDF vocabularies. It may also include literal values like strings, booleans and numeric values.



WikiData



- Main page
- Community portal
- Project news
- Create a new item
- Recent changes
- Random item
- Query Service
- Identify
- Help
- Donate
- Print/export
- Create a book
- Download as PDF
- Printable version

Welcome!

Wikidata is a free and open knowledge base that can be read and edited by both humans and machines.

Wikidata acts as central storage for the structured data of its Wikimedia sister projects including Wikipedia, Wikivoyage, Wikisource, and others.

Wikidata also provides support to many other sites and services beyond just Wikimedia projects! The content of Wikidata is available under a free license, exported using standard formats, and can be interlinked to other open data sets on the linked data web.

Learn about data

New to the wonderful world of data? Develop and improve your data literacy through content designed to get you up to speed and feeling comfortable with the fundamentals in no time.

Item: Earth (Q1)
Property: highest point (P31)
Restrict value: Mount Everest (Q234)

- Get involved**
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- What is Wikidata? Read the **Wikidata introduction**.
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 - Individuals and organisations can also **donate data**.
- Meet the Wikidata community**
- Visit the **community portal** or attend a **Wikidata event**.
 - Create a **user account**.

- Popular items**
- 2018 Toronto van attack (Q4142274)
 - 2018 Giro dell'Aspenino (Q51602019)
 - Liège-Bastogne-Liège for Women 2018 (Q4211955)
 - Saleh Al al-Sammad (Q1942978)
 - Marguerite HOURMÈRE (Q11294594)
 - Karen Karapetyan (Q1879623) (pictured)
 - Semirani Hotel bombing (Q2086153)
-

Discover

label — Douglas Adams (Q42)

description — English writer and humorist
Douglas Noel Adams | Douglas Noel Adams
► In more languages

property — **educated at**

rank —

statement group —

St John's College	end time	1974
	academic major	English literature
	academic degree	Bachelor of Arts
	start time	1971

▼ 2 references

stated in	Encyclopædia Britannica Online
reference URL	http://www.nndb.com/people/731/000023662
original language of work	English
retrieved	7 December 2013
publisher	HNDB
title	Douglas Adams (English)

+ add reference

Brentwood School	end time	1970
	start time	1959

► 0 references

+ add (statement)

identifier

analysis

value

qualifiers

opened references

collapsed reference

Example application

百度为您找到相关结果约3,060,000个

张飞_百度百科



职业：武将
 主要成就：当阳挡曹军、取西川、宕渠大胜
 简介：**张飞**（？ - 221年），字益德，幽州涿郡（今河北省保定市涿州市）人氏，三国时期蜀汉名将。刘备长坂坡败退，**张飞**仅...
[人物生平](#) [历史评价](#) [后世追位](#) [艺术造诣](#) [轶事典故](#) [更多>>](#)
[查看“张飞”全部14个含义>>](#)
[baike.baidu.com/2014-10-12](#)

张飞_百度图片 - 举报图片

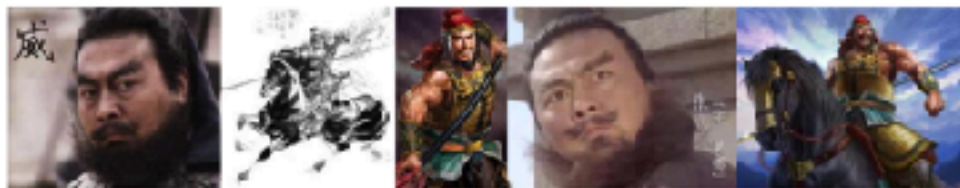


image.baidu.com - 查看全部263,345张图片

历史上张飞是个什么样的人_百度知道

9个回答 - 提问时间：2012年04月21日
 最佳答案：在历史上**张飞**、黄忠、魏延是蜀国最优秀的武将,其他人全都靠边站。在容貌上,三国演义颠覆**张飞**形象,其实**张飞**是一个白面俊生,长的非常好看,赤壁之战前...
[zhidao.baidu.com/link?...](#) - 80%好评

- [张飞的真正死因](#) 10个回答 2013-07-17
 - [许褚和张飞谁猛?](#) 5个回答 2009-04-11
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张飞吧_百度贴吧

月活跃用户：3224人 累计发帖：10万

<三国演义> 主要人物

展开



赵云

三国时期蜀汉名将



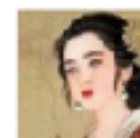
关羽

五虎上将之一



吕布

三国第一猛将



魏延

舍魏延年华得美名千秋

相关人物

展开



刘备

三国时期蜀汉开国皇帝



荀彧

东汉末年著名政治家



水镜八奇

八奇中的最强者



诸葛亮

三国时期蜀魏猛将

其他人还搜

展开



丈八蛇矛

张飞所用兵器



曹操

可爱的纤维跑得快?



八虎骑

曹操帐下八位武将



崔慧恩

诸葛亮的女儿之名

南京大学

实体

100

描述

- “中国最顶尖的大学”
- “源远流长的高等学府”
- “中国‘净源头’的雅集地”
- “中国改革开放以后最早实施的素质教育国际合作长期项目”
- “声誉卓著的百年名校”
- “东方教育的中心”

属性

人工智能学院院长	周志华	前身	三江师范学堂
原党委书记	洪银兴	校长	陈骏
成立	人工智能学院	教授	毕飞宇
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国际关系研究院院长	朱锋	商学院院长	赵曙明

标签

- 高校
- 大学
- 院校
- 学校
- 机构
- 单位
- 名校
- 学府
- 科研机构
- 研究机构
- 重点大学
- 高等院校
- 教授
- 科研院所
- 综合性大学

近义项

- Nanjing University
- NJU
- 国立东南大学
- 国立东南大学

南京大学学报

实体

99

标签

- 刊物
- 期刊
- 报刊
- 学术刊物
- 杂志

南京大学教授

集合

展开内容

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南京大学长江产业经济研究院、光明智库、光明网联合主办 《2019中国进口...
http://about.gmw.cn/2019-11/13/content_33315363.htm

2019年11月13日 - 光明日报打造服务型媒体, 为知识界提供全方位学术服务, 并与专家学者携手合作、紧跟机遇, 为中国经济快车持续运行贡献“媒体+智库”的独特智慧。南京大学长江产业经济研究院特聘研究员、北京师范大学国家进口研究中心主任魏浩 (摄影: 光明网记者潘浩)

南京大学报考人数近3万, 多数专业推免生占比超50%, 报考需谨慎! 统考
https://www.sohu.com/a/353240253_100123142

2019年11月12日 - 原标题: 南京大学报考人数近3万, 多数专业推免生占比超50%, 报考需谨慎! 今天我们来说说考研热门院校南京大学。南京大学坐落于钟灵毓秀、虎踞龙盘的金陵古都, 是一所历史悠久、声誉卓著的百年名校。国家211工程、985工程首批重点建设高校。

主要学习来源

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www.sohu.com · 2019年10月9日

历史最悠久的九所大学 最古老均具有千年传承! 历史悠久千年传承...
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南京大学_百度百科
baike.baidu.com · 2019年3月1日

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zhidao.baidu.com · 2018年12月3日

南京大学新闻网-2019自然指数年度榜单: 南京大学位列全球高校...
news.nju.edu.cn · 2019年8月5日

哲学考研该怎么选学校? 25所名校学科排名, 北大、复旦首当其冲...
www.sohu.com · 2019年10月30日

南大简介
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用英语说中国名校: 南京大学 (双选) - 听力课堂
www.ingclass.net · 2018年3月17日