

## 1. Background: Learnware Paradigm

### Building high-quality models:

- Complex, time-consuming and expensive: data, computing resources, expertise...
  - A heavy burden for ordinary users.
- Difficult to reuse among different users: data privacy concerns, catastrophic forgetting.

### Learnware paradigm [Zhou, 2016; Zhou and Tan, 2022]

- Construct a **model market** that manages numerous well-performing models.
- Solve future tasks by leverage these models without having to build models from scratch.

### 1) Learnware components

$$\text{learnware} = \text{model} \boxplus \text{specification} \boxminus$$

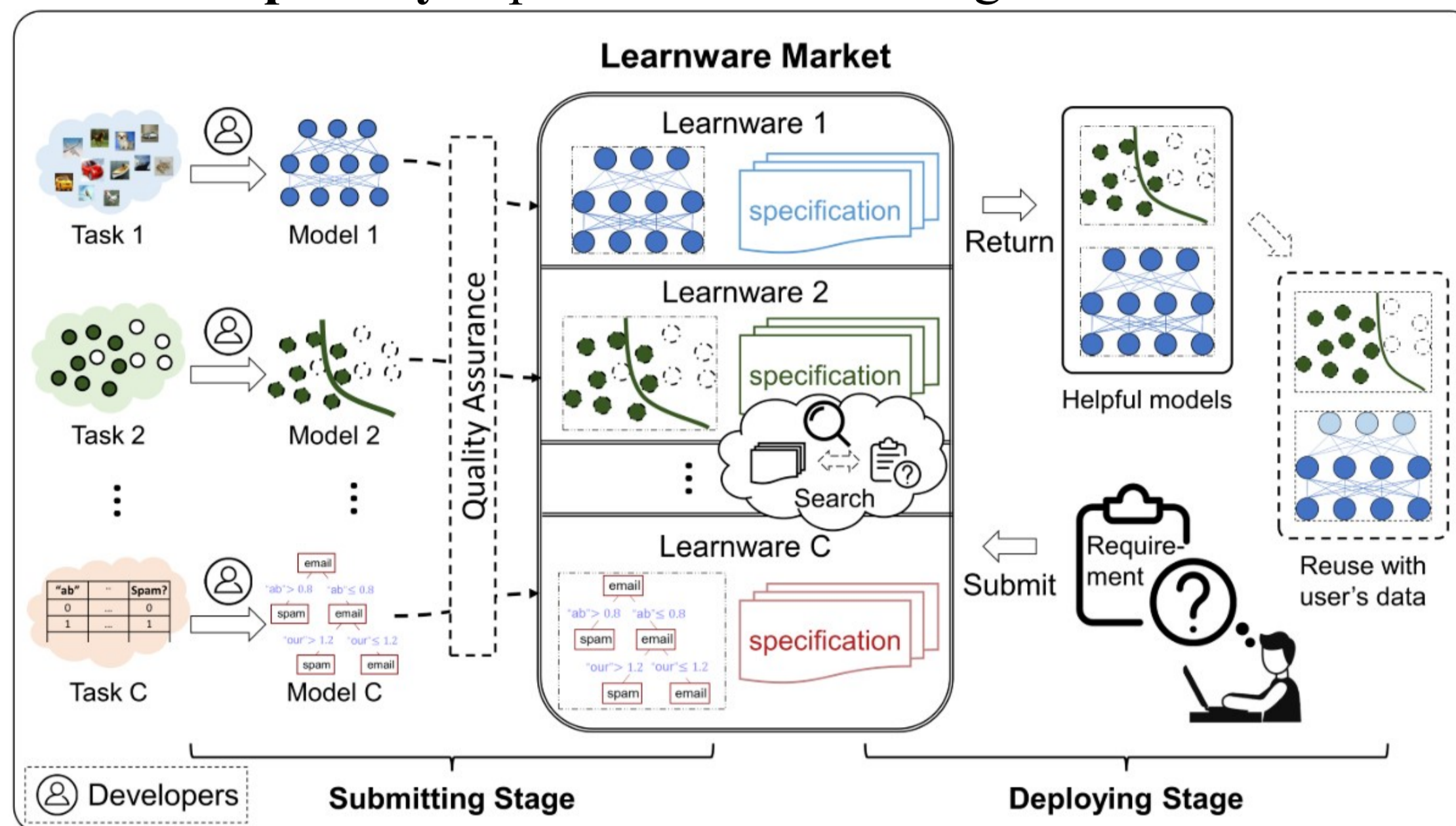
describe the functionality of the model

### 2) Procedure of learnware paradigm

**Submitting stage:** The learnware market assigns specifications to submitted models.

**Deploying stage:** The market helps the user identify & reuse helpful models according to the requirement.

**Data privacy** is preserved in both stages.



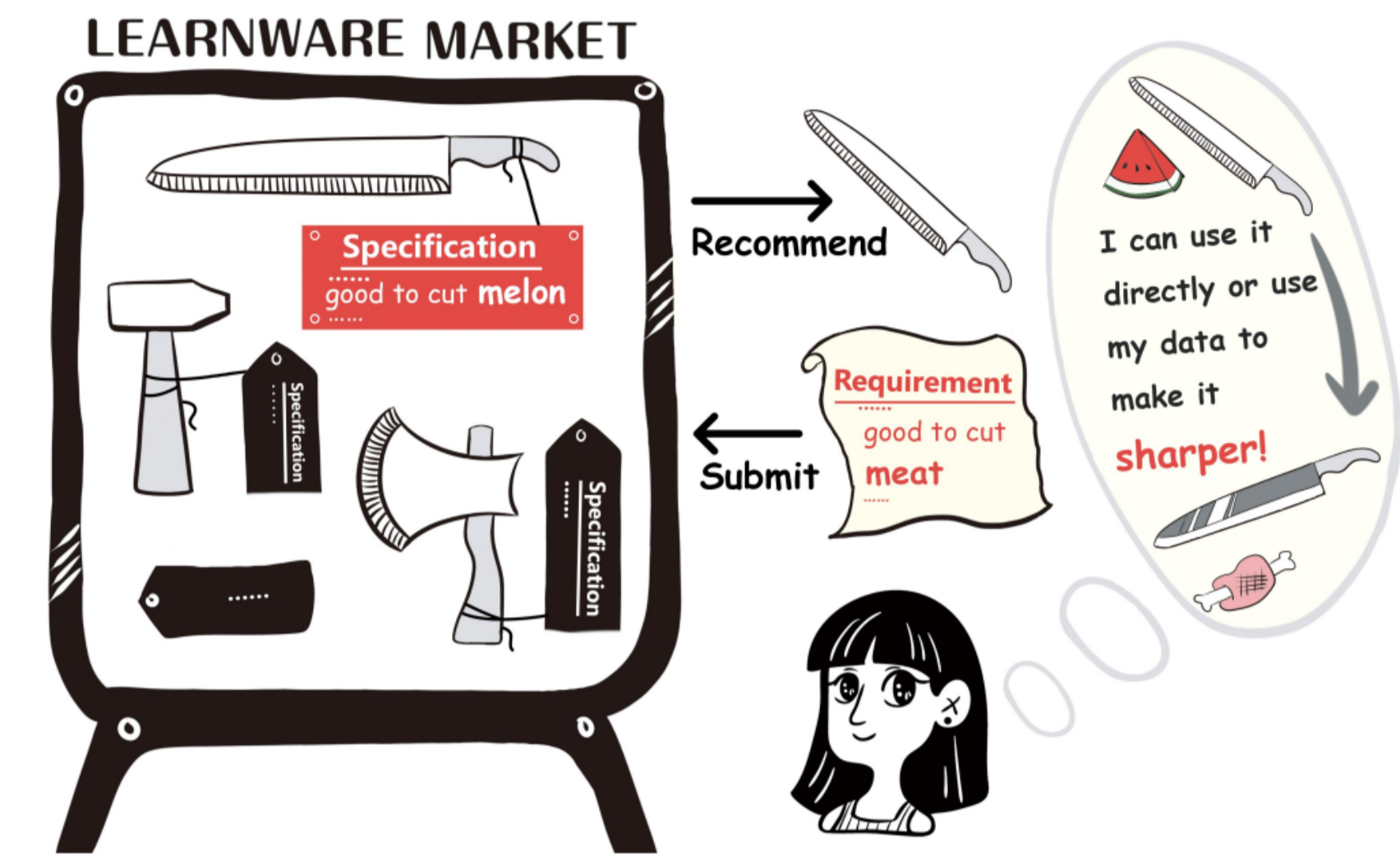
**Key challenge:** how to identify helpful models for a specific user task efficiently without leaking user data privacy?

### 3) Reduced Kernel Mean Embedding (RKME) specification [Zhou and Tan, 2022]

$$\min_{\beta, Z} \left\| \sum_{i=1}^n \frac{1}{n} k(x_i, \cdot) - \sum_{j=1}^m \beta_j k(z_j, \cdot) \right\|_{\mathcal{H}}^2$$

KME of original data      RKME specification

- Sketch the dataset via **weighted samples** in RKHS.
- Capture **major distribution information** while **protecting data privacy**.
- Assumption: each learnware is a well-performing model on its on training data.
  - Identifying a suitable model for user task can be approached by identifying a model whose training distribution is close to the distribution of user task.



## 2. Motivation

**Previous algorithms** based on RKME specification [Wu et al., 2023][Zhang et al., 2021][Tan et al., 2022][Tan et al., 2023]

- Require **examining all learnwares** in the market:
  - Computationally unaffordable in large markets.
- Impose strict **restrictions** on the market:
  - E.g., all learnwares share the same ground-truth labeling function.

**This paper:** a more **efficient** and **flexible** method

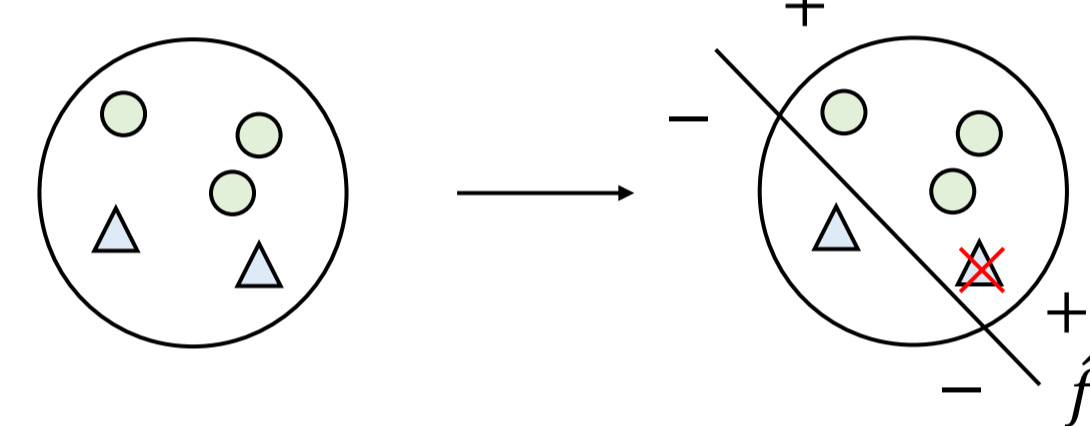
- A learnware scoring criterion with fewer restrictions.
- An anchor-based framework only examining only a small portion of the market.

## 3. Whether a learnware is helpful?

**Question 1:** How to judge whether a learnware is potentially helpful based on the limited labeled data of the user?

**Case 1:** There exists one learnware that can solve user's task.

**Solution:** Calculate losses on user's data, and choose the learnware with the smallest loss.



**Case 2:** No single learnware can tackle the user task as a whole, but multiple learnwares can each tackle a part of user's task separately.

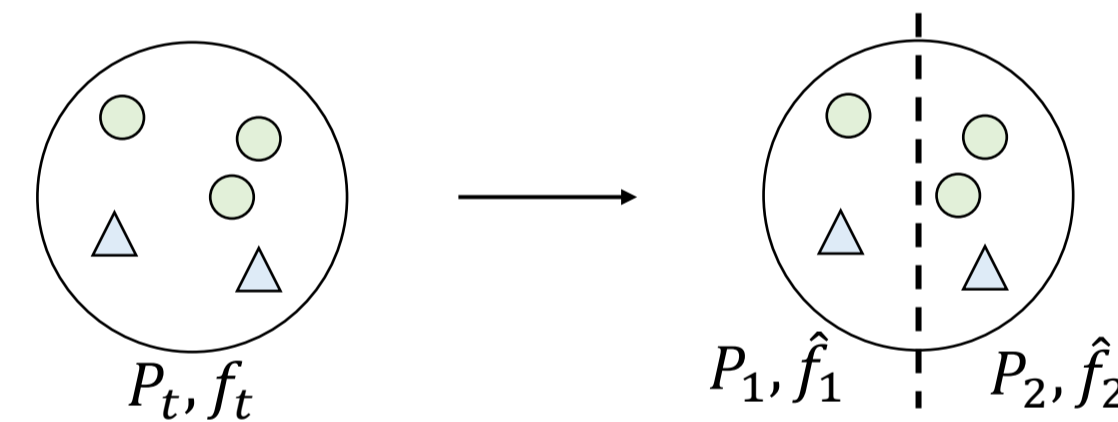
### Instance-recurrent Assumptions

- The user's distribution is a mixture of multiple key learnwares' distributions

$$P_t = \sum_i w_i P_i$$

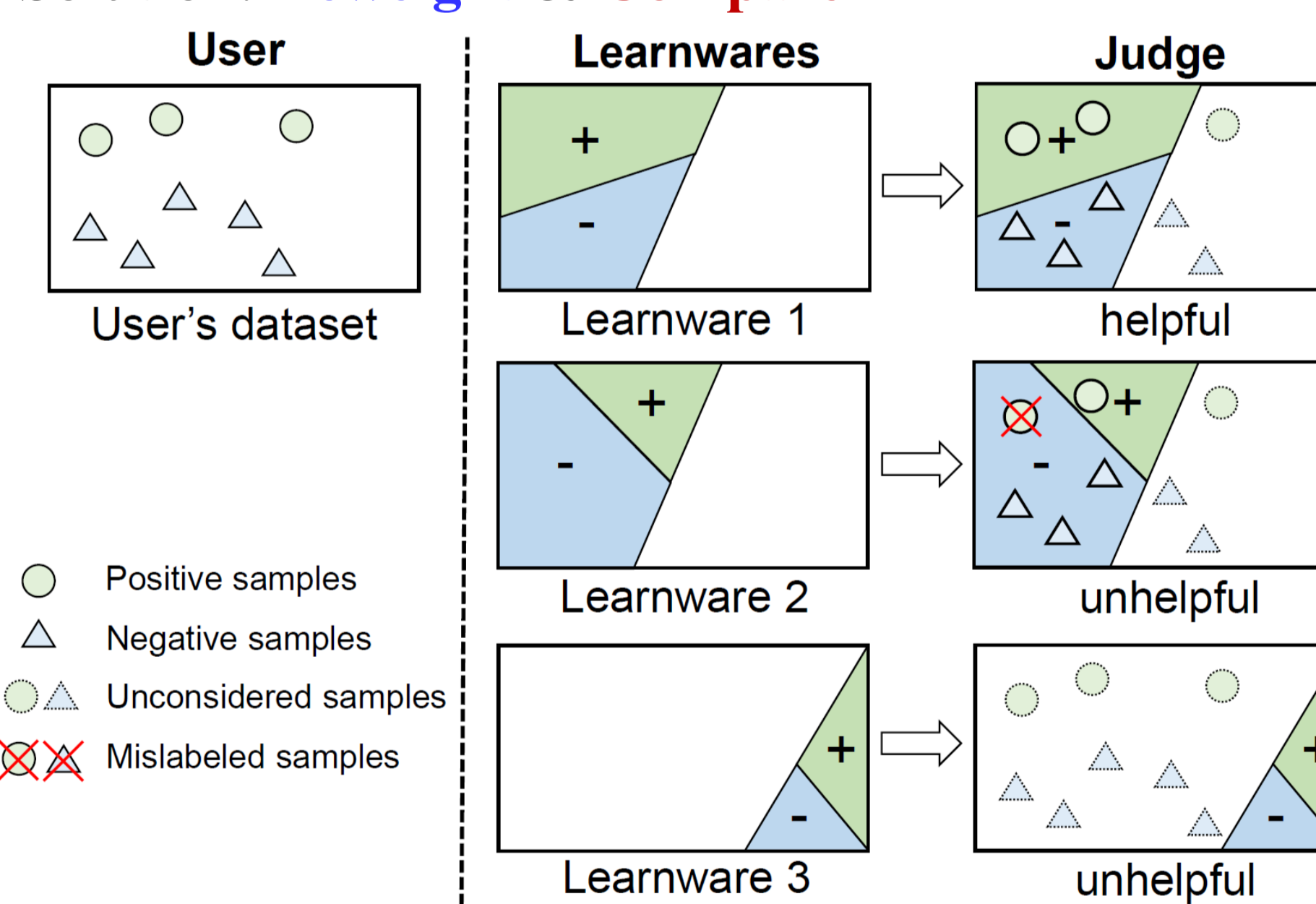
- Each key learnware  $i$  performs well in the corresponding mixture component

$$\mathcal{L}(P_i, \hat{f}_i, f_t) \leq \epsilon$$



Key learnwares:  
 $0.4P_1 + 0.6P_2 = P_t$   
 $\mathcal{L}(P_1, \hat{f}_1, f_t) \leq \epsilon$   
 $\mathcal{L}(P_2, \hat{f}_2, f_t) \leq \epsilon$   
 Other learnwares:  
 $w_i = 0$

### Solution: Reweight & Compare



**Our method:** For learnware  $(\tilde{\mu}_i, \hat{f}_i)$ , corresponds to user's data  $\{\mathbf{x}_{tn}, \mathbf{y}_{tn}\}_{n=1}^{N_t}$

### Reweight:

- Reweight the user's samples to simulate learnware's distribution in RKHS
- Get a weighted dataset  $\{\eta_{in}, (\mathbf{x}_{tn}, \mathbf{y}_{tn})\}_{n=1}^{N_t}$  with RKME defined as  $\tilde{\mu}_{t \rightarrow i}$

### Compare:

- on this reweighted dataset, 
$$h_i = U \|\tilde{\mu}_i - \tilde{\mu}_{t \rightarrow i}\|_{\mathcal{H}} + \sum_{n=1}^{N_t} \eta_{in} L(\hat{f}_i(\mathbf{x}_{tn}), \mathbf{y}_{tn})$$
- Judge:  $h_i \leq \theta$ : helpful;  $h_i > \theta$ : unhelpful

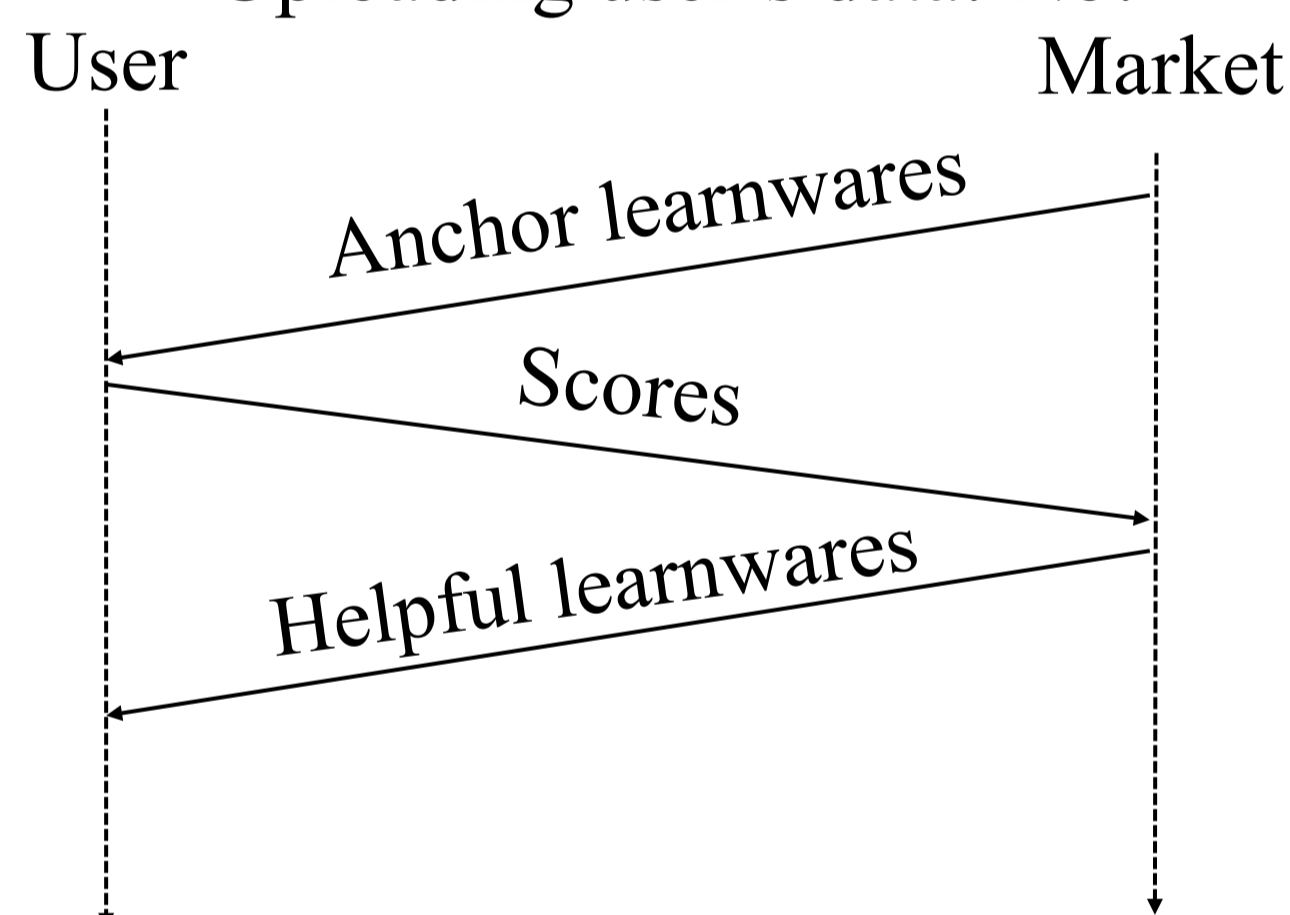
**Analyses:** There exists a good  $\theta$ , with a high probability,

- All key learnwares are considered helpful;
- And all learnwares considered helpful can solve one part of user's task.

## 4. Anchor-based Learnware Identification Framework

**Question 2:** how to identify helpful learnwares efficiently?

- Examining the whole market: No!
- Uploading user's data: No!



### Anchor Learnwares!

- Market sends anchor learnwares to user;
- User tests anchor learnwares and returns scores to market;
- Market identifies helpful learnwares based on scores.

### Submitting stage: Cluster of learnwares

- A helpful anchor + a good cluster  $\leftrightarrow$  The whole cluster may be helpful
- Define a dissimilarity

$$d_{ij} = U \cdot d(P_i, P_j) + \min\{\mathcal{L}(P_i, \hat{f}_i, \hat{f}_j), \mathcal{L}(P_j, \hat{f}_j, \hat{f}_i)\}$$

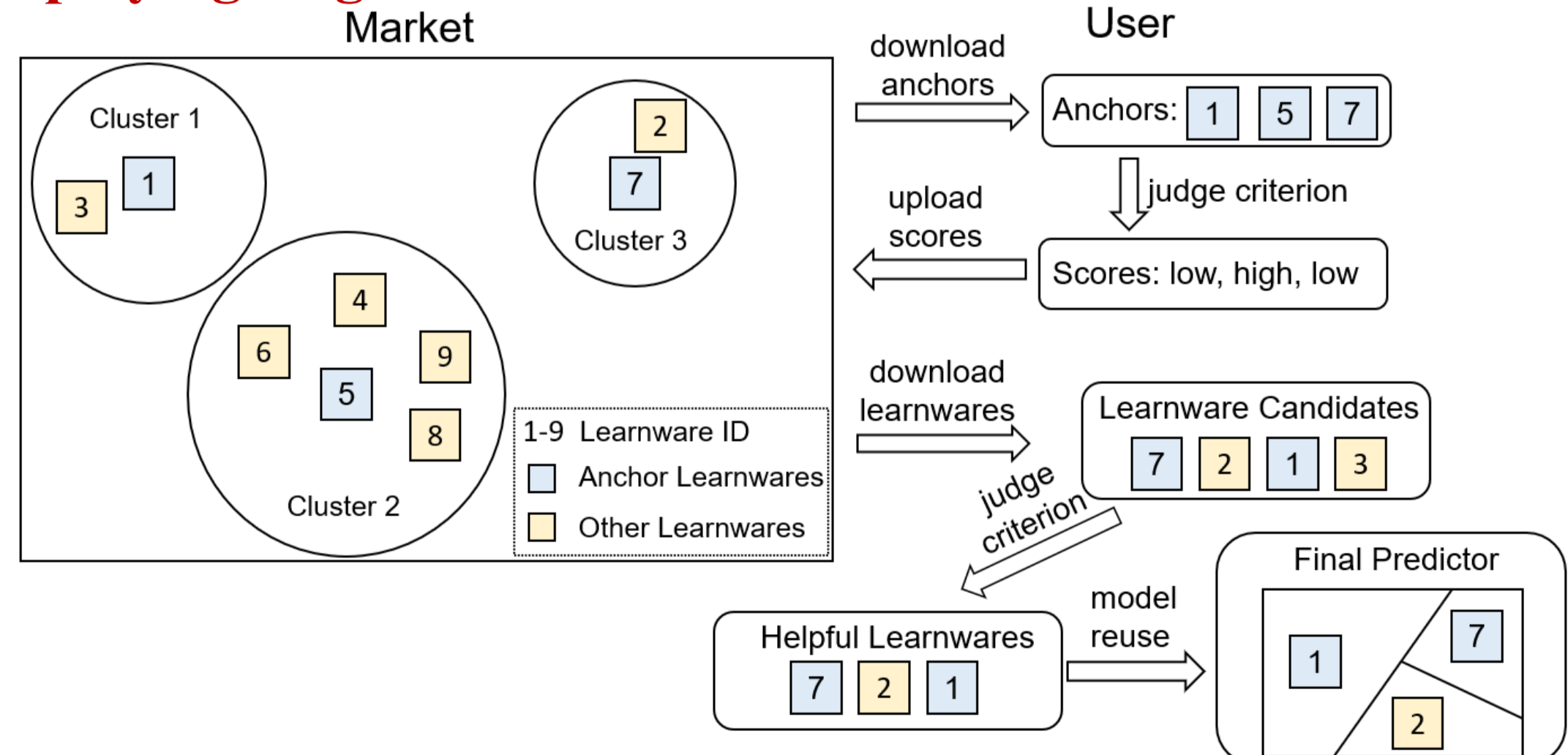
and then transform to the RKME version.

- Cluster algorithm:
  - PAM: a k-medoids algorithm, medoids as anchors.
  - Multi-level clustering is available for very large markets.

### Analyses: helpfulness on user's task:

Informally, for any user's task,  $|\text{help}(\text{learnware}) - \text{help}(\text{anchor})| \leq \text{radius}$ .

### Deploying stage:



## 5. Conclusion

- Propose a novel learnware scoring criterion based on the RKME specification to assess the potential helpfulness of a learnware;
- Design an anchor-based framework to achieve efficient learnware identification by examining only a small portion of learnwares in the market;
- Theoretical guarantees + Experimental verification.

## 5. Experiments

### Market construction:

- 4 real-world datasets that can be naturally divided into several parts;
- Train 15 models on each part: different linear models, LightGBM, and neural networks.

Dataset	Task	#Instance	Split Criterion	#Models	#Users
M5	Regression	46M	Department	1050	10
PFS	Regression	9M	Shop	795	17
PPG-DaLiA	Regression	517K	Activity	675	22
Covtype	Classification	581K	Soil	450	10

### Results:

- Our learnware scoring criterion (Ours-traversal) achieve the best performance;
- Our anchor method (Ours-anchor) greatly improves efficiency (examine 11.8%, 14.9%, 21.42%, 19.91% learnwares) with very little performance degradation.

	M5			PFS			PPG-DaLiA			Covtype		
	RMSE	Imp.	Time	RMSE	Imp.	Time	MSE	Imp.	Time	Error	Imp.	Time
From-scratch	4.142	1.85%	-	3.081	13.79%	-	19.83	45.43%	-	0.334	50.60%	-
Random	4.085	0.00%	-	3.297	0.00%	-	36.62	0.00%	-	0.683	0.00%	-
RKME-task	3.389	18.27%	7.77	2.798	25.42%	2.35	24.53	33.64%	<b>0.73</b>	0.380	44.05%	<b>0.30</b>
RKME-instance	3.586	13.72%	137.57	2.931	14.56%	277.10	22.40	38.51%	201.42	0.240	65.00%	21.33
Validate	3.266	21.12%	4.09	2.671	29.46%	3.34	14.70	59.87%	10.07	0.245	64.01%	2.43
Ours-traversal	3.154	23.80%	10.61	<b>2.609</b>	<b>32.48%</b>	8.27	<b>13.29</b>	<b>63.71%</b>	11.35	<b>0.222</b>	<b>67.67%</b>	4.94
Ours-anchor	<b>3.148</b>	<b>23.80%</b>	<b>1.13</b>	2.616	32.07%	<b>1.37</b>	14.03	61.71%	2.57	0.244	64.45%	1.12