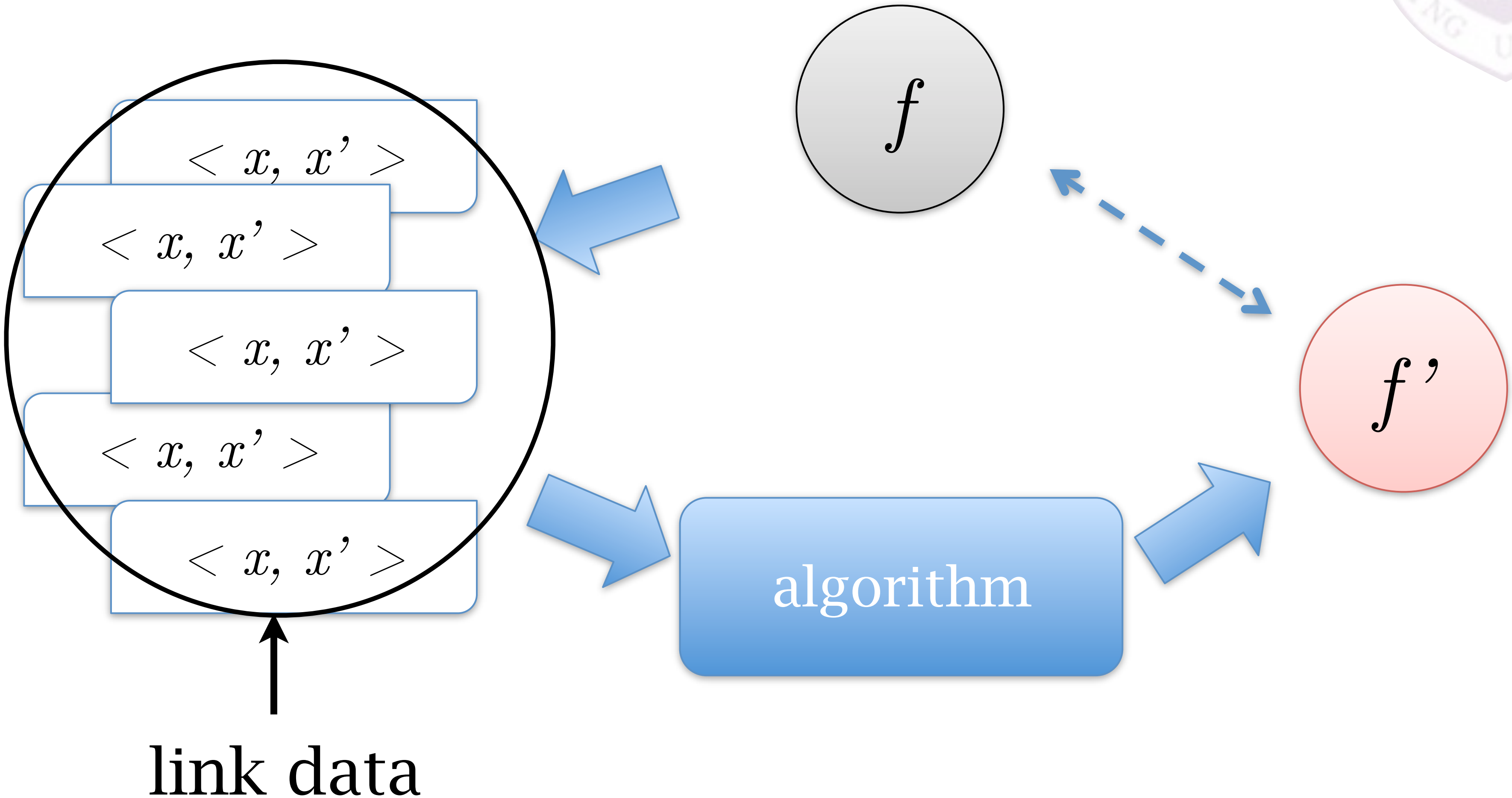
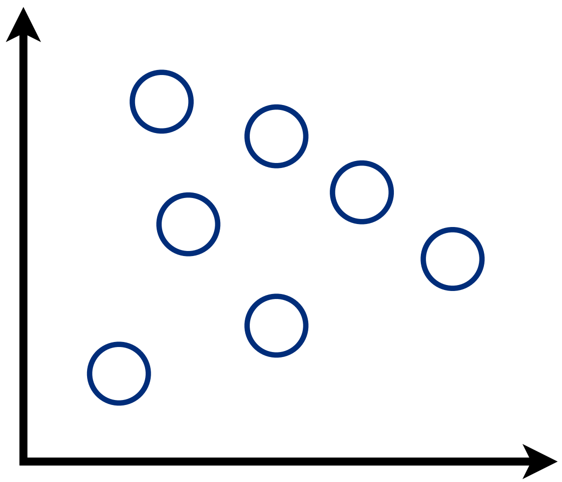
Lecture 11: Mining Link Data

http://cs.nju.edu.cn/yuy/course_dm12.ashx

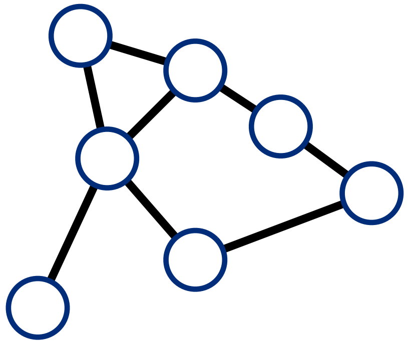
Position



What is link data



vector data



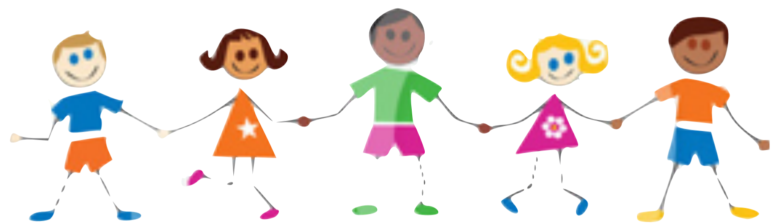
link data
= graph

chain
tree
acyclic graph
graph
multi-graph
...
directed
undirected

nodes may have features, but we focus on the information of the edges at the moment

Why care links

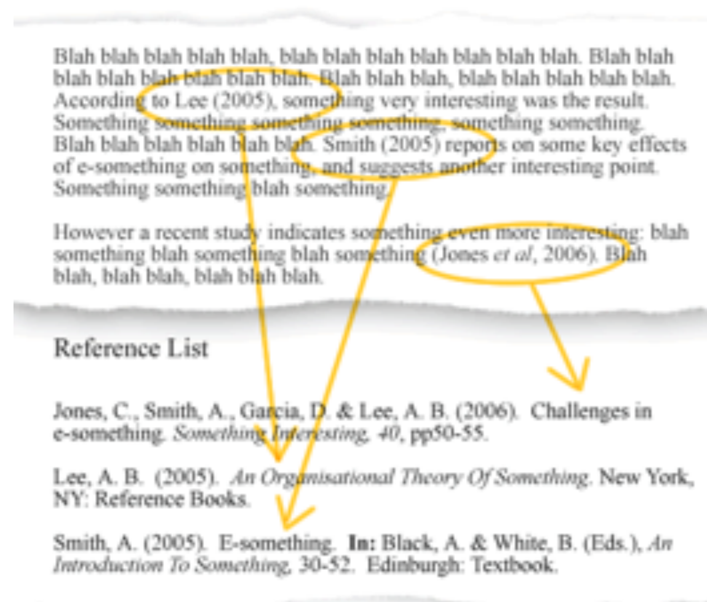
pervasive and easy to obtain



friendship

hyperlink

any relationship...



Blah blah blah blah blah, blah blah blah blah blah blah blah. Blah blah blah blah blah blah blah blah. Blah blah blah, blah blah blah blah blah. According to Lee (2005), something very interesting was the result. Something something something something, something something. Blah blah blah blah blah blah. Smith (2005) reports on some key effects of e-something on something, and suggests another interesting point. Something something blah something.

However a recent study indicates something even more interesting: blah something blah something blah something (Jones *et al*, 2006). Blah blah, blah blah, blah blah blah.

Reference List

Jones, C., Smith, A., Garcia, D. & Lee, A. B. (2006). Challenges in e-something. *Something Interesting, 40*, pp50-55.

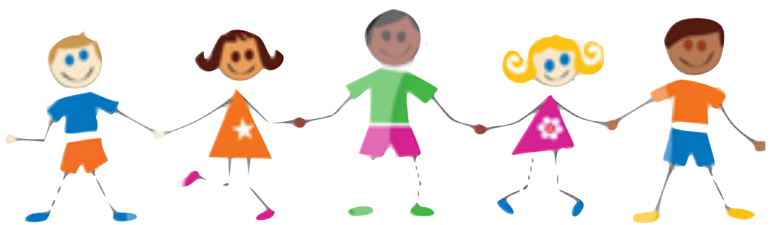
Lee, A. B. (2005). *An Organisational Theory Of Something.* New York, NY: Reference Books.

Smith, A. (2005). E-something. **In:** Black, A. & White, B. (Eds.), *An Introduction To Something*, 30-52. Edinburgh: Textbook.

citation

Why care links

more explicit semantic



friendship

(city, job, age, salary)

are they friends?

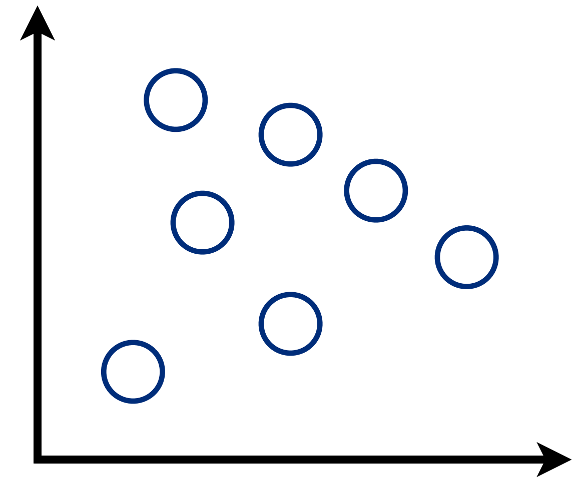
sometimes feature vectors are used to obtain links

e.g. find neighbor instances

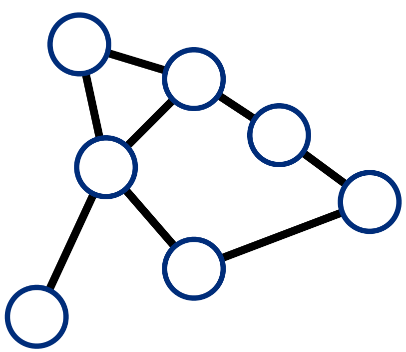
Why care links

relax i.i.d. assumption

in supervised learning, we commonly assume objects are i.i.d. drawn from a fixed distribution



link data explicitly expresses the relationship among objects



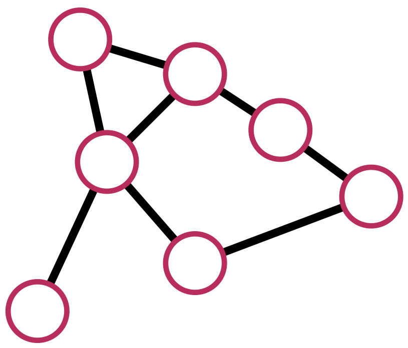
Goals in mining link data

many tasks could be performed with link data

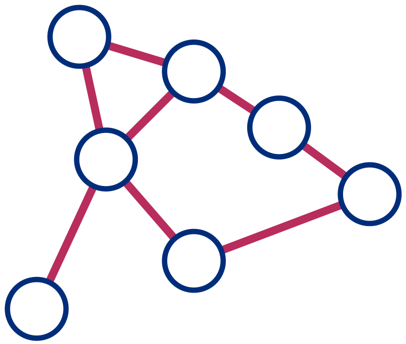
object ranking

object classification

object clustering

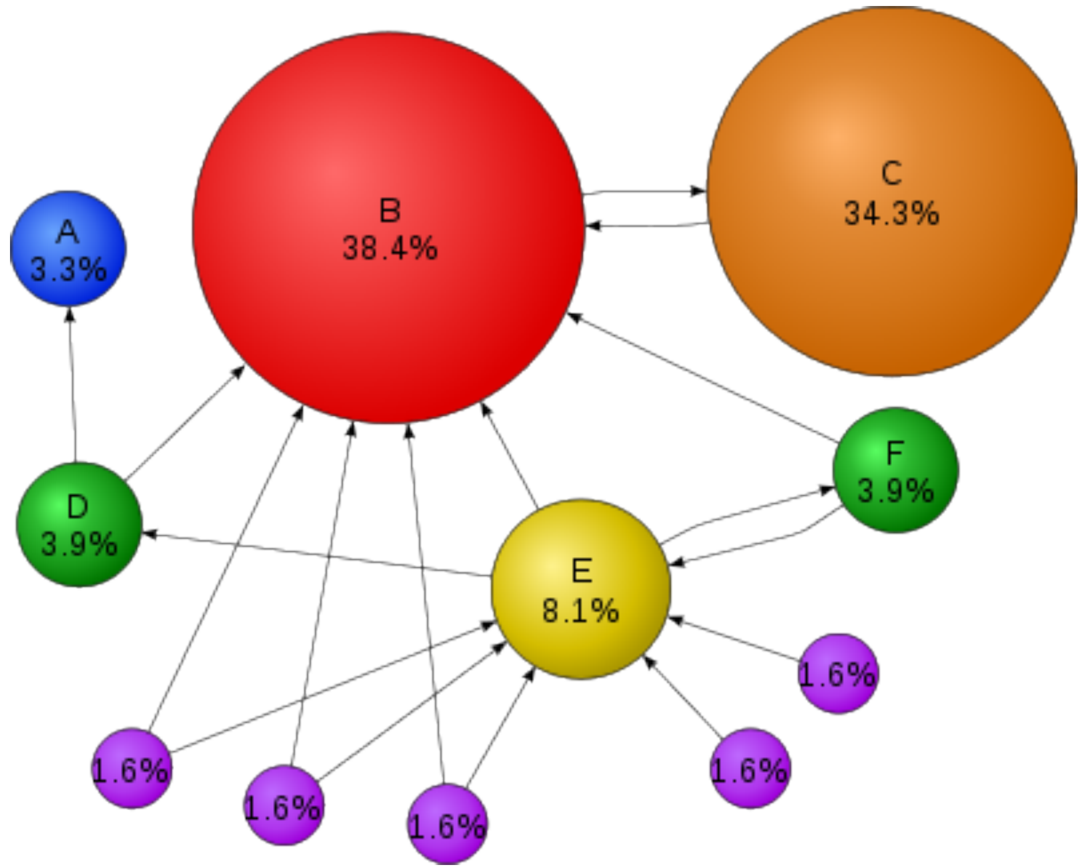


link prediction



Object ranking

ranking the importance of nodes in a directed graph

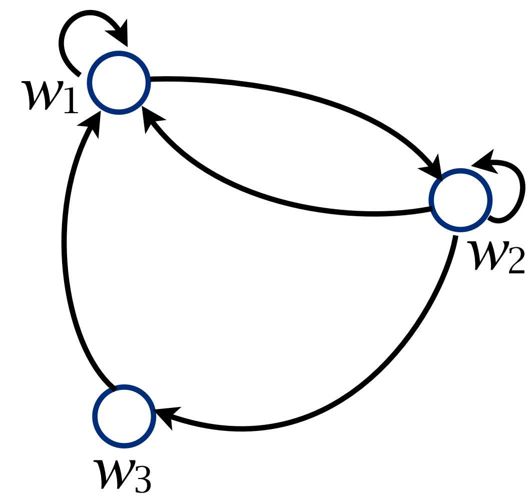


Object ranking

PageRank [PagePage, et al., 1998]

Randomly surf in the web

The importance of a web be the fraction of time staying in the web after infinite surfing time



transition matrix M

	w_1	w_2	w_3
w_1	0.5	0.5	0
w_2	0.33	0.33	0.33
w_3	1	0	0

current state w_1, next state: $(1,0,0)*M=(0.5,0.5,0)$
next state: $(0.5,0.5,0)*M = (1,0,0)*M*M = (0.416,0.416,0.167)$
next state: $(1,0,0)*M^3 = (0.514, 0.347, 0.139)$
after 10 steps: (0,5, 0.375, 0.125) stationary distribution

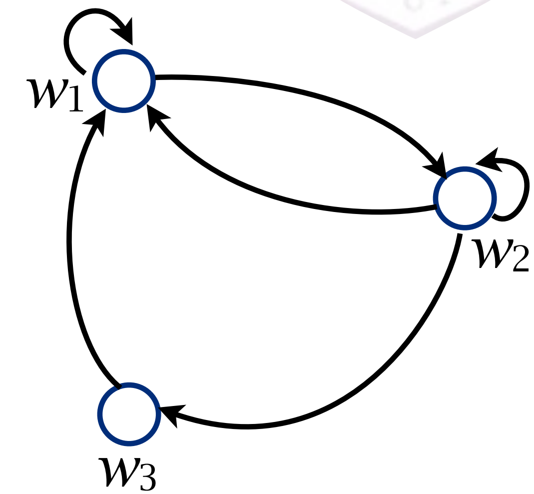
Object ranking

PageRank [Page, et al., 1998]

Let $\boldsymbol{r}$ be the stationary distribution:

$$\boldsymbol{r} = M^\top \boldsymbol{r}$$

$\boldsymbol{r}$ is the eigenvector of M^{T} with the eigenvalue 1



transition matrix M

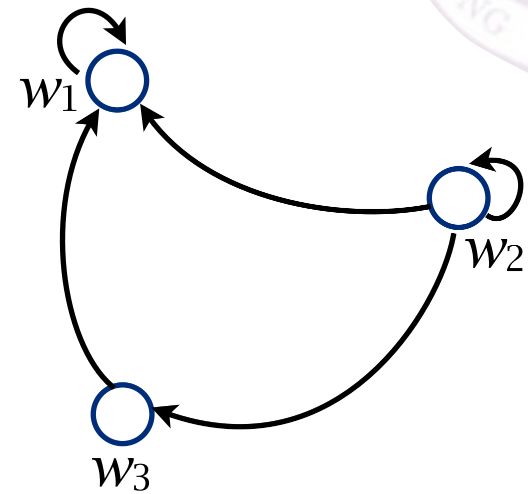
	w_1	w_2	w_3
w_1	0.5	0.5	0
w_2	0.33	0.33	0.33
w_3	1	0	0

A PageRank voting view:

$$\boldsymbol{r}(x_i) = \boldsymbol{r}(x_1)P(x_i|x_1) + \ldots + \boldsymbol{r}(x_n)P(x_i|x_n)$$

Object ranking

PageRank [Page, et al., 1998]



The problem with absorbing states

PageRank:

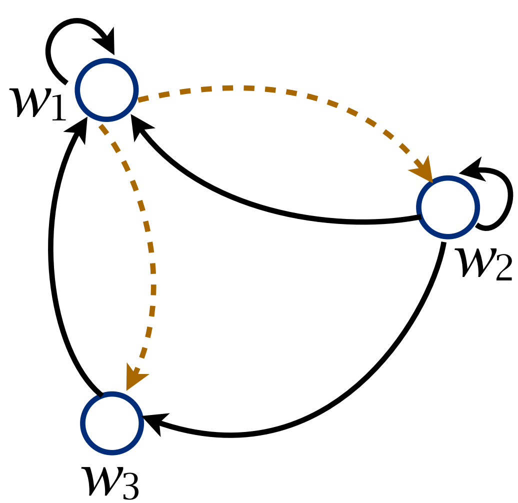
$$w_1 = 1,\ w_2 = w_3 = 0$$

transition matrix M

	w_1	w_2	w_3
w_1	1	0	0
w_2	0.33	0.33	0.33
w_3	1	0	0

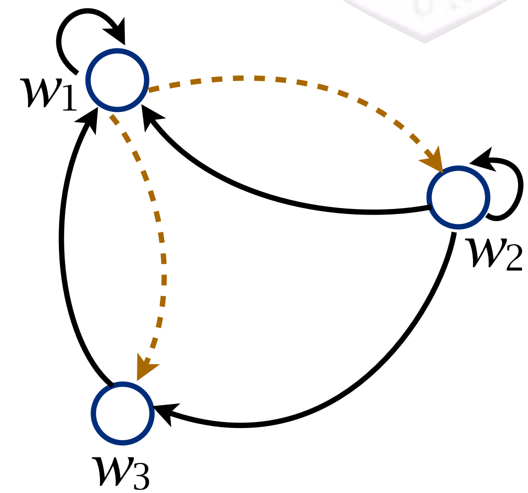
Add a full graph:

jump to a random state with a small probability (restart)



Object ranking

PageRank [Page, et al., 1998]



Damping factor: the surfing process restarts with probability 1-*d* (d=0.85)

A PageRank voting view:

$$\boldsymbol{r}(x_i) = (1-d)\frac{1}{n} + d(\boldsymbol{r}(x_1)P(x_i|x_1) + \ldots + \boldsymbol{r}(x_n)P(x_i|x_n))$$

Matrix form:

$$\boldsymbol{r} = \frac{1-d}{n}\mathbf{1} + dM^\top \boldsymbol{r}$$

transition matrix M

	w_1	w_2	w_3
w_1	0.5	0.5	0
w_2	0.33	0.33	0.33
w_3	1	0	0

$\boldsymbol{r}$ solution: $\boldsymbol{r} = (I - dM^\top)^{-1}\frac{1-d}{n}\mathbf{1}$

recursive solution: $\boldsymbol{r}_{t+1} = \frac{1-d}{n}\mathbf{1} + dM^\top \boldsymbol{r}_t$

Object ranking

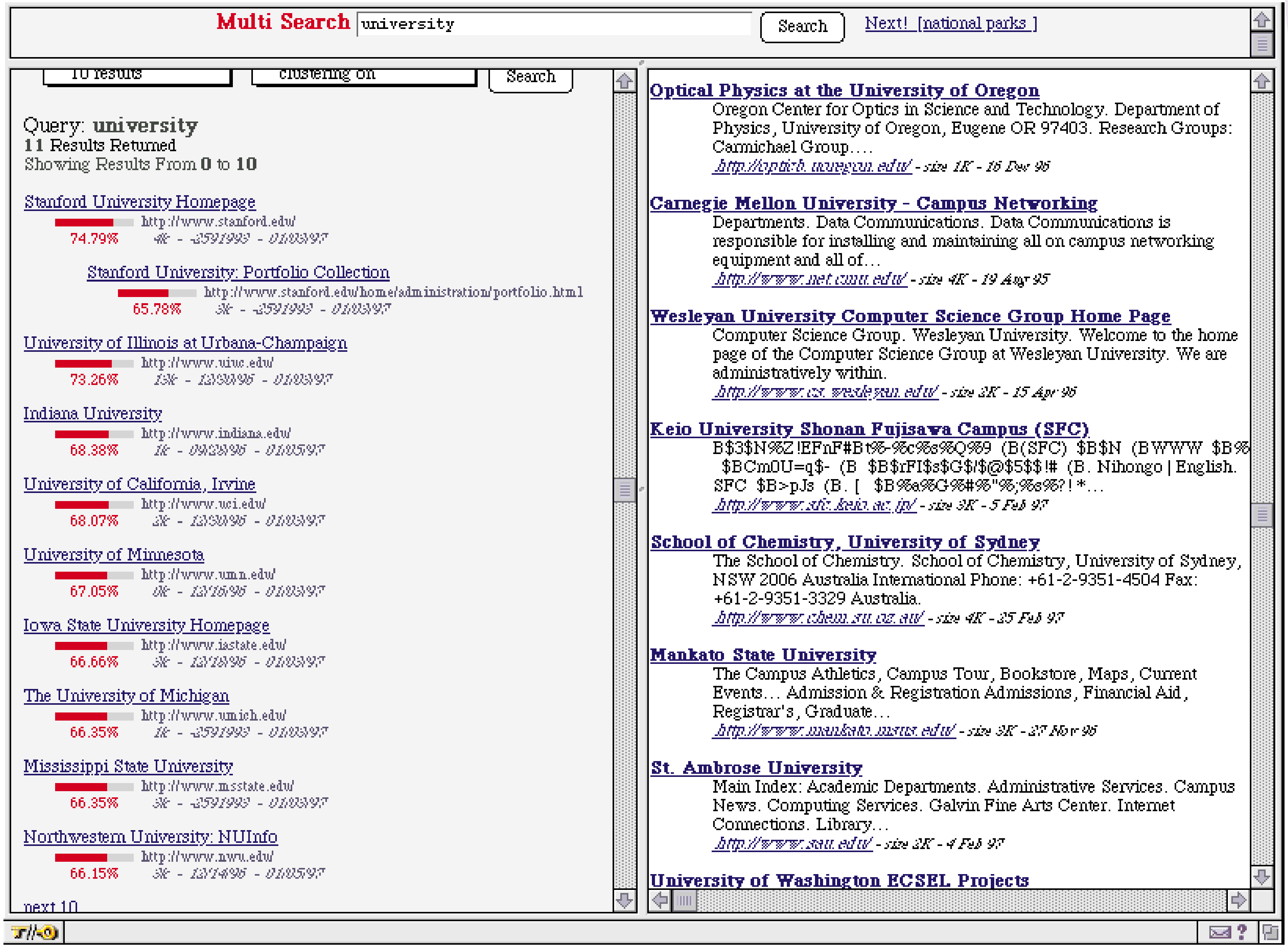


Figure 6: Comparison of Query for "University"

[Page, et al., 1998]

Object ranking

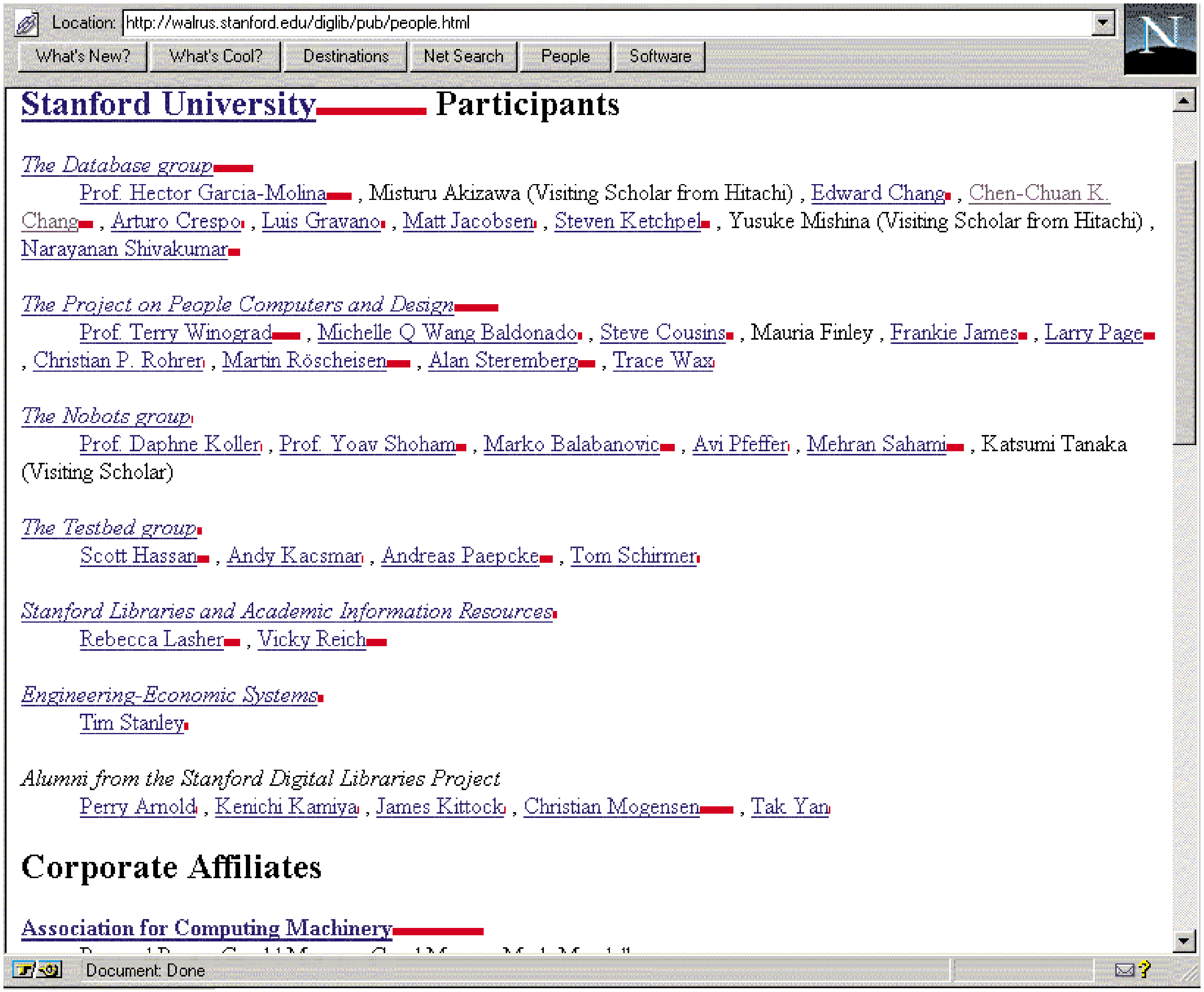
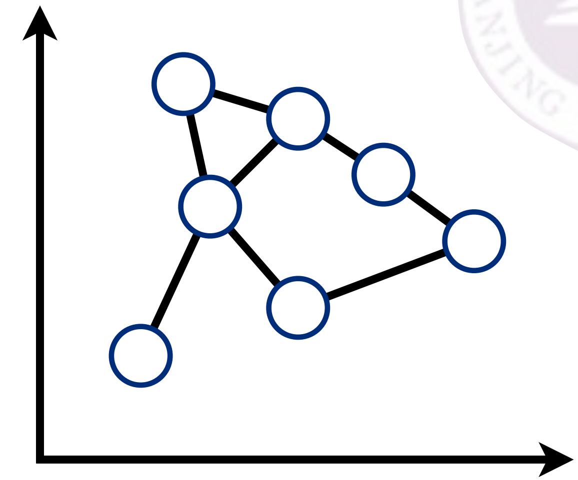


Figure 7: PageRank Proxy

[Page, et al., 1998]

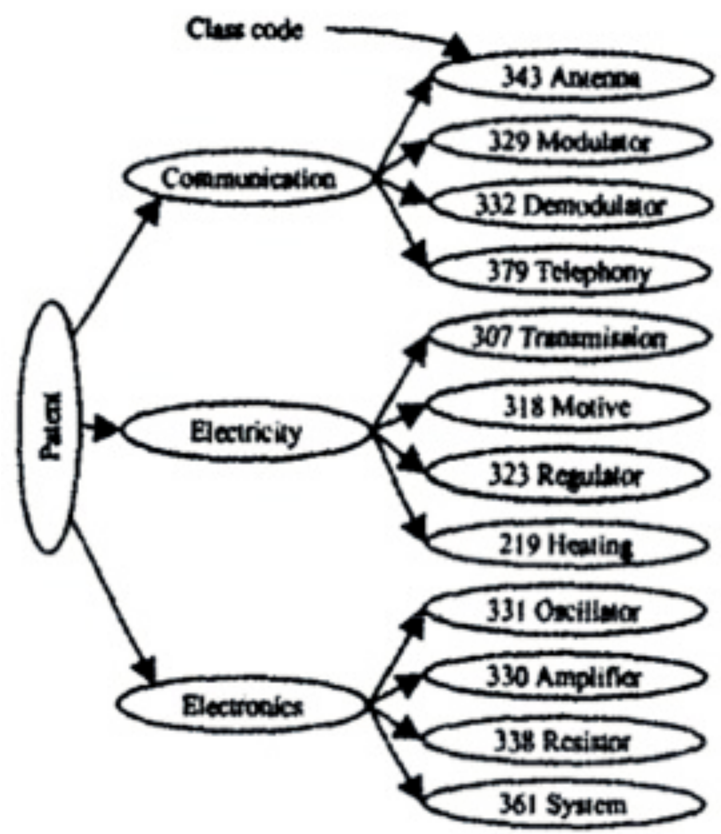
Object classification

Incorporate link information could improve the classification accuracy



Classification of web pages

[Chakrabarti, et al., SIGMOD98]



Object classification

Classification of web pages

[Chakrabarti, et al., SIGMOD98]

use pure text for classification: 36% error

Object classification

Classification of web pages

[Chakrabarti, et al., SIGMOD98]

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Object classification

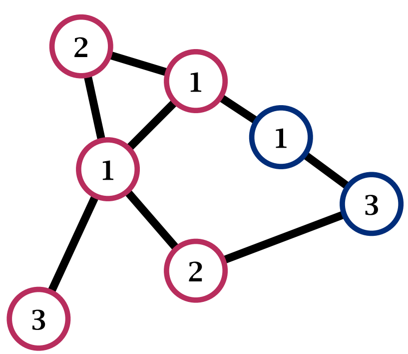
Classification of web pages

[Chakrabarti, et al., SIGMOD98]

use pure text for classification: 36% error

use neighbor predicted classes:
34% error, 22.1% error

hyperlink forms a neighborhood relationship



Given test node δ_0
Construct a radius-r subgraph $G_r(\delta_0)$ around δ_0
Assign initial classes to all $\delta \in G_r(\delta_0)$ using local text
Iterate until consistent:
  Recompute the class for each δ based on
    local text and class of neighbors

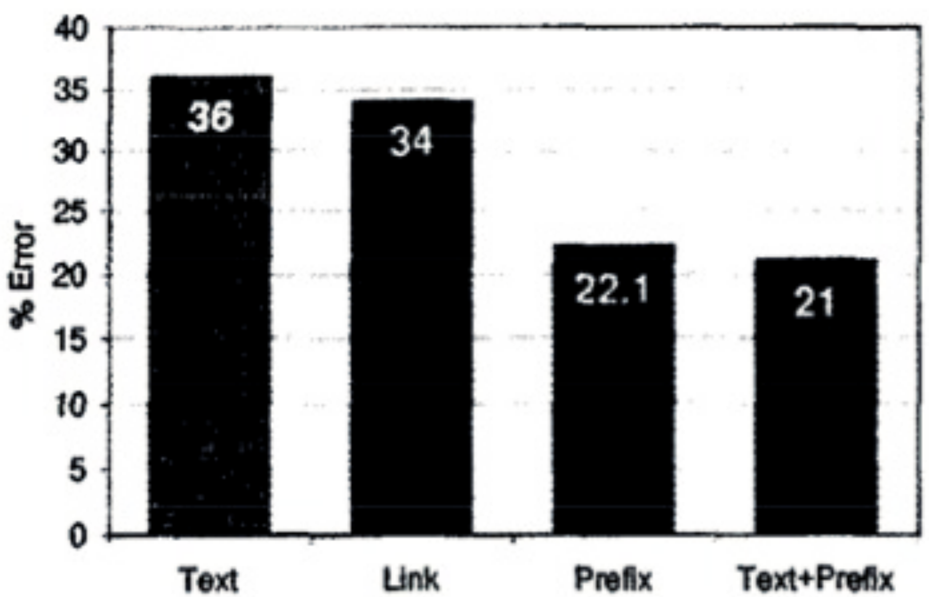
Object classification

Classification of web pages

[Chakrabarti, et al., SIGMOD98]

use pure text for classification: 36% error

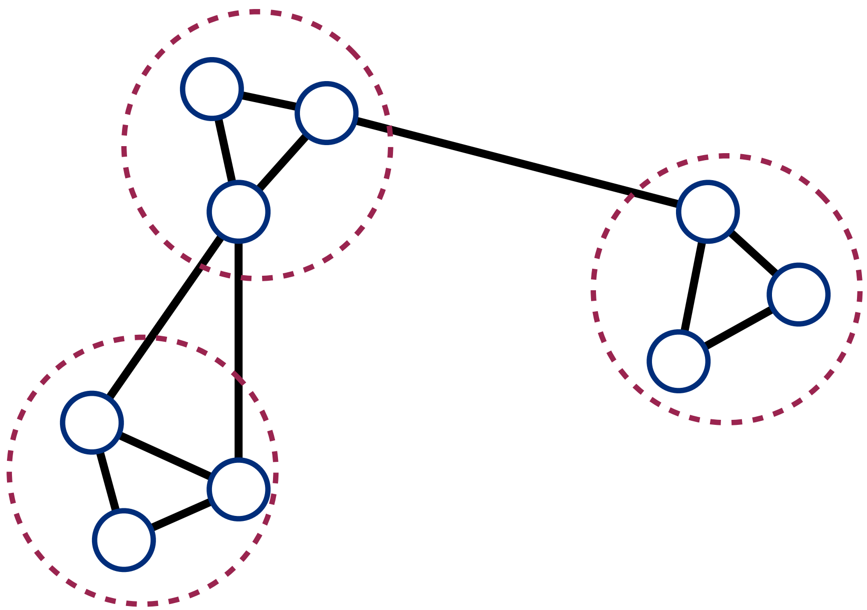
use neighbor predicted classes:
34% error, 22.1% error



Object clustering

Clustering nodes using link information

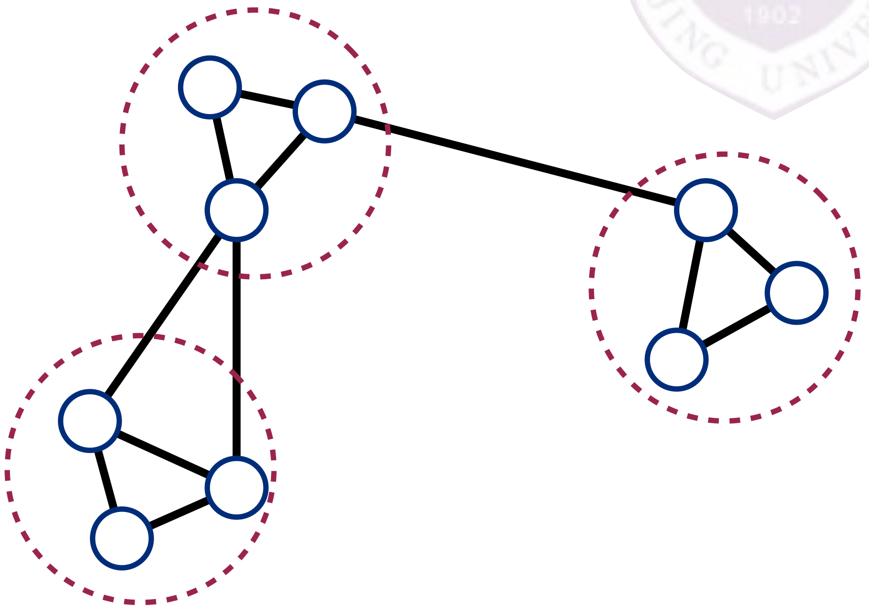
community discovery in social networks



Object clustering

Presenting the graph into an adjoint matrix

1	0	1
1	1	0
0	1	1



many clustering algorithms utilize only the adjoint matrix

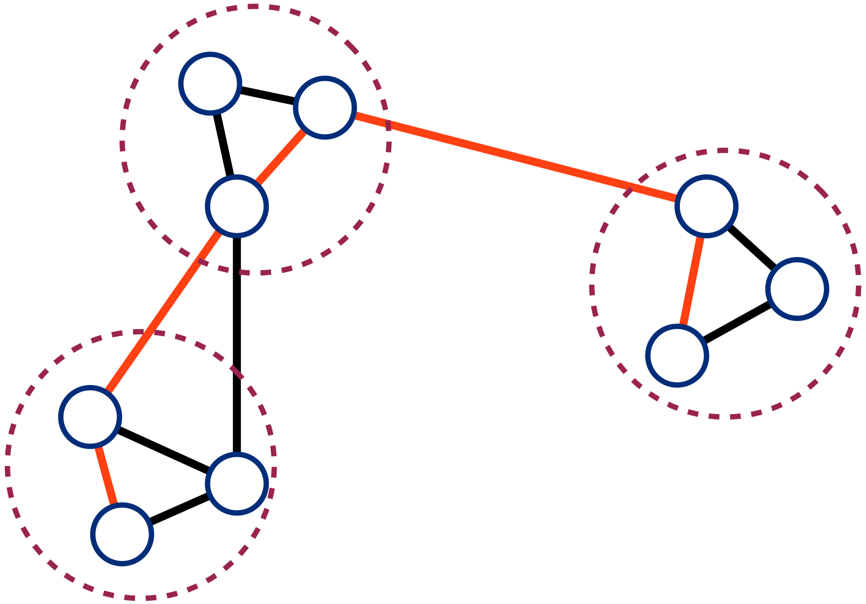
hierarchical clustering

graph-cut

k-medoids

Object clustering

Defining the distance between any two nodes as the shortest path length

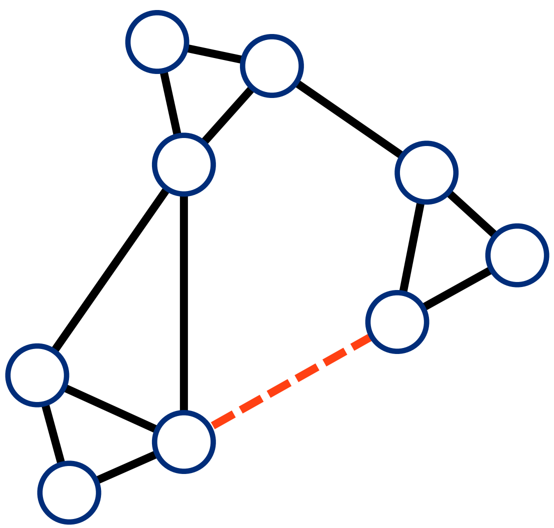


all clustering algorithms can be used

Link prediction

Predict the existence of a link between two nodes

recommendations in social network



Link prediction

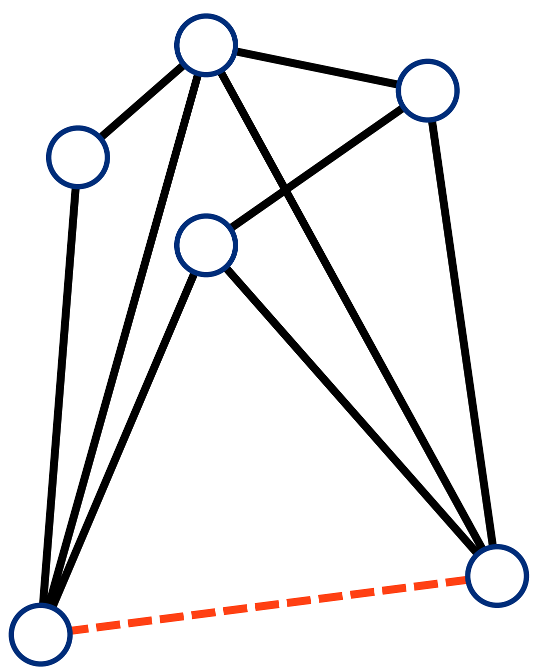
node feature based link prediction

(node1, node2) -> yes/no

binary classification

link structure based link prediction

two persons shares a lot of
friends are likely to be friends



习题

PageRank算法的思想是什么?