

脑启发人工智能的计算理论、方法与应用



助理教授, 博士生导师
类脑智能方向、机器学习课题组
南京大学 智能科学与技术学院

联络邮箱: zhangsq@lamda.nju.edu.cn
zhangsq@nju.edu.cn

个人主页: <https://www.lamda.nju.edu.cn/zhangsq/>

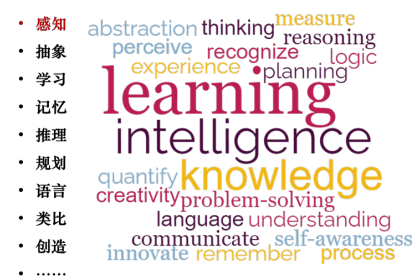
研究方向：机器学习与数据挖掘

- 高效低耗计算 for Edge AI
 - 大模型的轻量化方法与开源工具
 - 脉冲神经网络的表示与泛化理论
- 时空建模表征 for TSFM
 - TSFM 关键技术攻关
 - 工业自动化场景（能源、医疗等）
- 理论保障：机器学习理论，尤其是深度学习和大模型理论
 - 表示和泛化理论 (Expressivity and Generalization)
 - 知识与数据双驱动的反问题求解 (Inverse Problem)
 - 不确定性分析 for Trustworthy AI (Uncertainty Analysis)



个人主页

智能科学与技术学院
School of Intelligence Science and Technology



- ① 神经网络模型是系统还是智能？
- ② 存算一体、高效低功耗是系统还是智能？
- ③ 数学题求解是系统还是智能？

如何区别系统和智能?

- ① 系统强调结构和实现方式
- ② 智能强调行为和使用的智能表现



Q1. 大模型轻量化研究

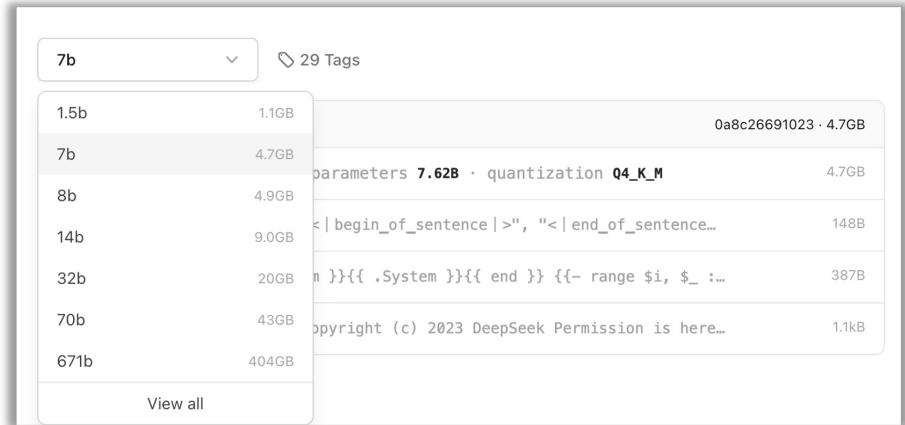


南京大學
NANJING UNIVERSITY



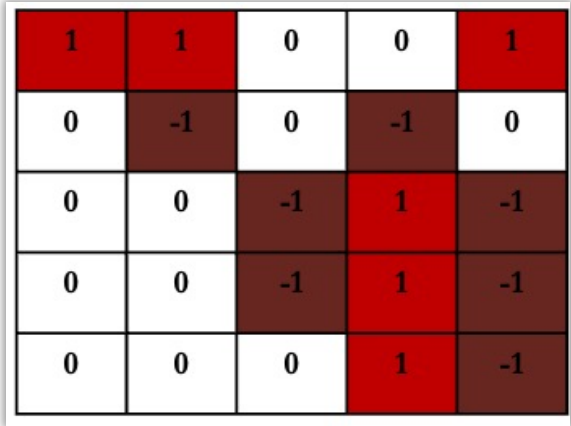
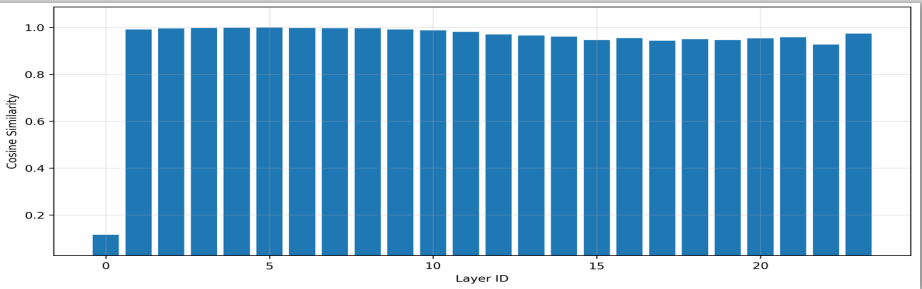
智能科学与技术学院
School of Intelligence Science and Technology

[高效低耗计算] 大模型在训练和部署的时候将导致较大的计算量、存储量、能耗等问题，如何在工业、端侧等资源受限场景实现高效低耗部署？

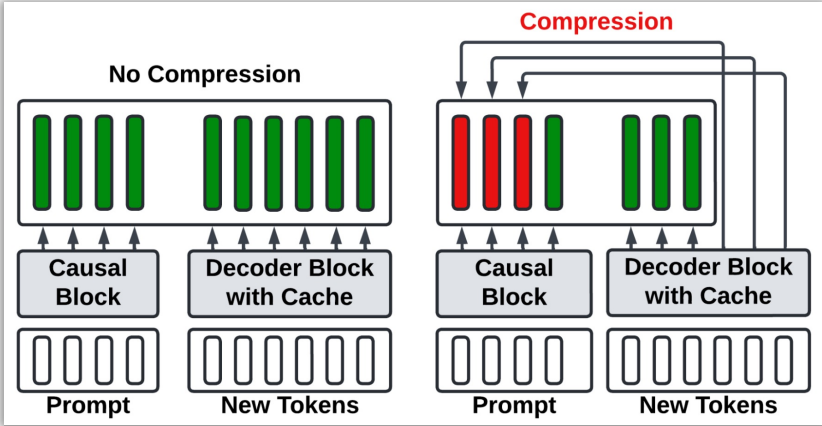


大模型“阉割”参数量 **NO!**

高相似性、冗余表征

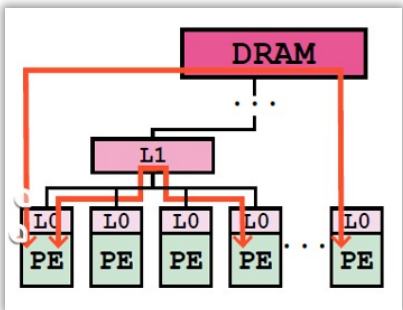
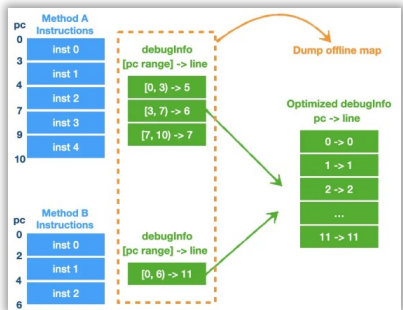


量化表示



压缩表征

拆解算法计算单元，优化指令集映射



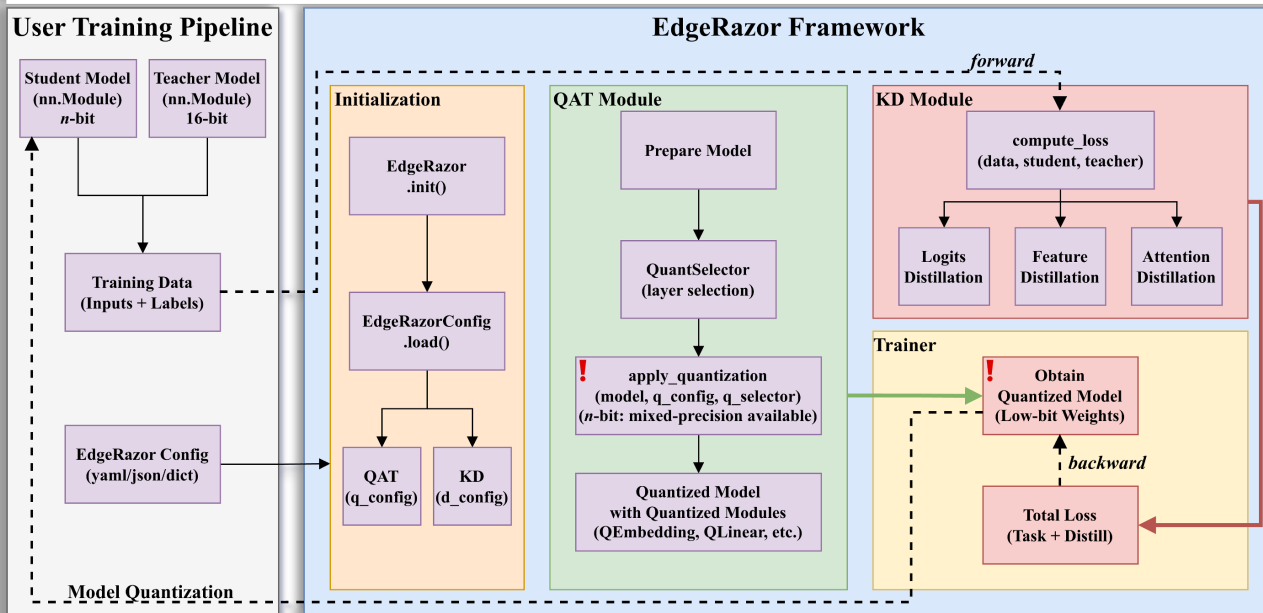
1.1. LLM 轻量化开源工具



Lightweight Framework for Edge AI

 HuggingFace  Collection  README  ZH  License  Apache 2.0

✨ If you like our project, please give us a star ⭐ for the latest update.



- **全方位适配多尺度大模型。** 覆盖350M-7B全参数量级，包括基础大模型、指令微调大模型、多模态大模型。
- **极致低比特量化能力。** 灵活支持1.58-bit至4-bit混合低比特量化，压缩与性能双向兼顾。
- **极简集成，零门槛使用。** 仅需少量代码修改，就能无缝集成到现有全精度大模型训练流程中，大幅降低边缘端大模型部署与优化成本。
- **适配 llama.cpp 等“硬件通吃”的软件平台，** 支持家用电脑（MAC）、手机运行大模型



Github



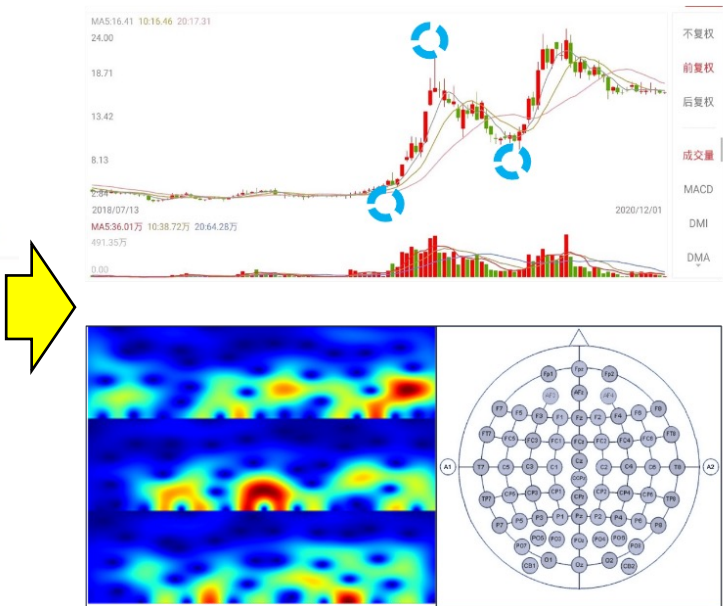
Huggingface

Q2. 时空数据表征及基础模型建模

[时空表征及建模] 如何实现工业场景数据的时空表征？

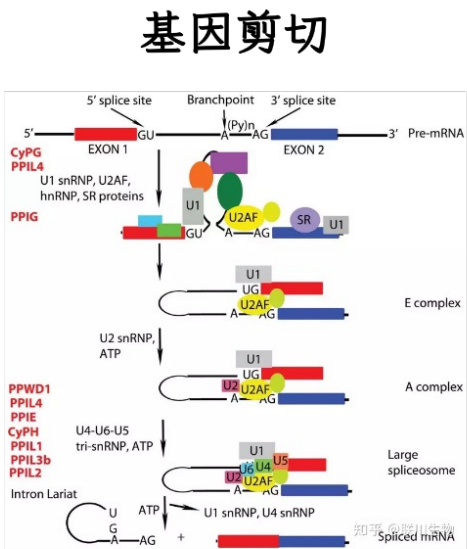


Amazon 2025 年
(Chronos-2)



量化
交易

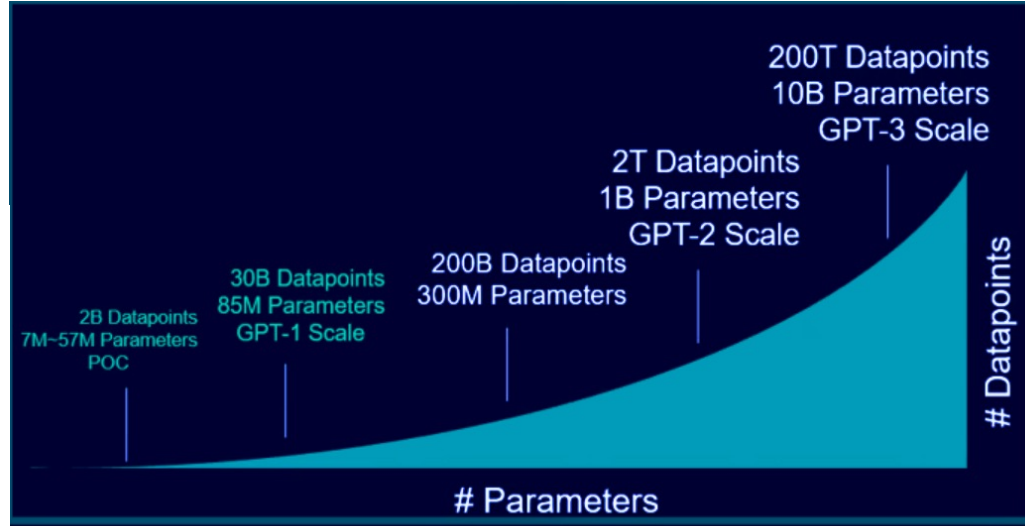
神经信
号处理



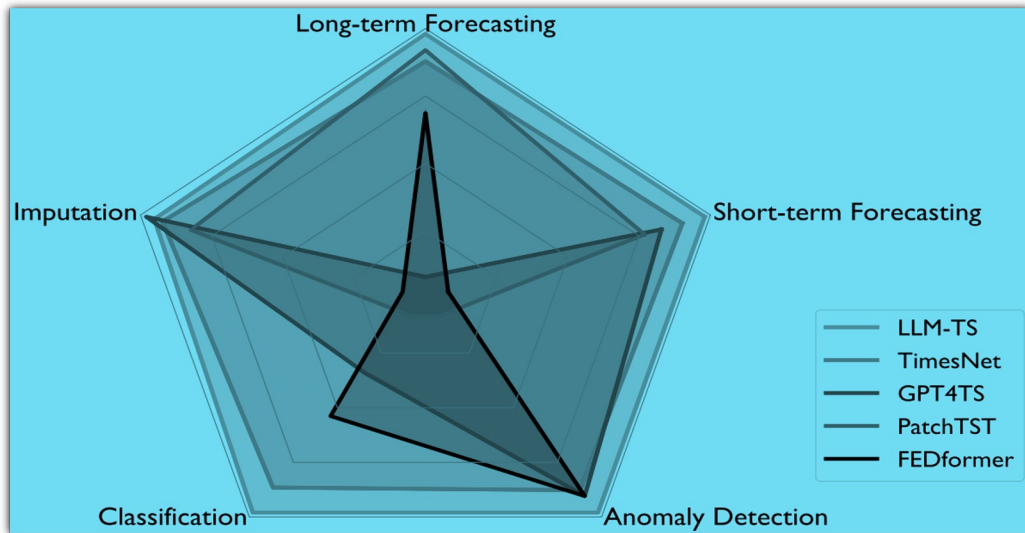
当前时间序列基础模型 TSFM 仍缺乏多变量 (Multi-Variable)、多源 (Multi-Source)、变周期 (Aperiodic) 建模

2. 时空表征及基础模型关键技术攻关

Scaling Law

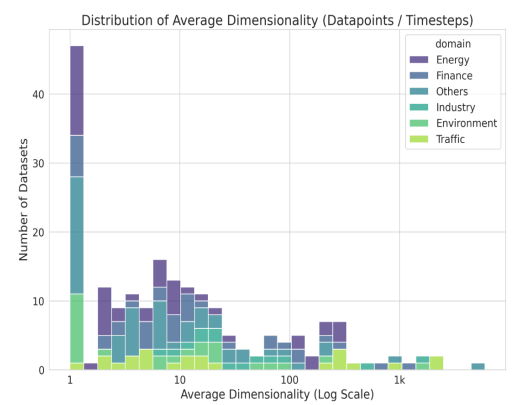
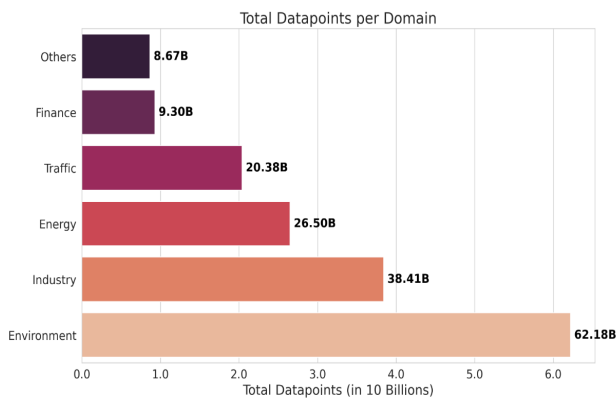
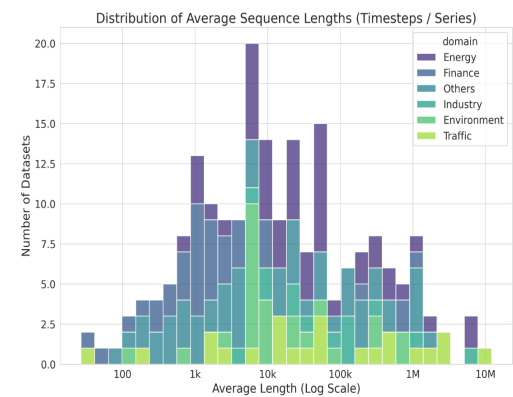
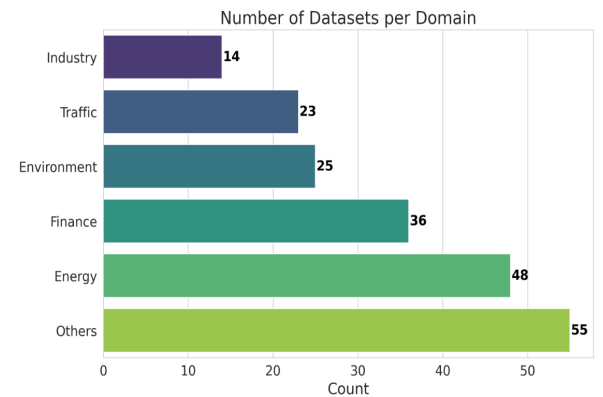


Comprehensiveness



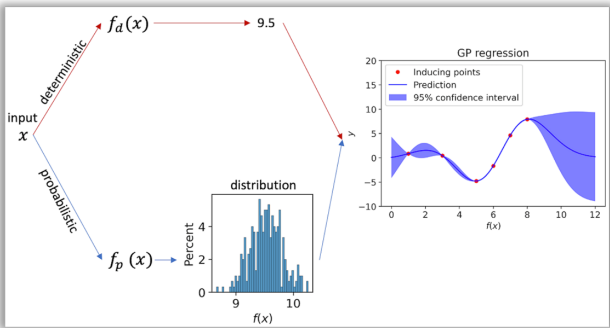
维护多变量工业时间序列数据集 数据规模 $\approx 200M/165 B$

工业
金融
交通
能源
天气
医疗
其他



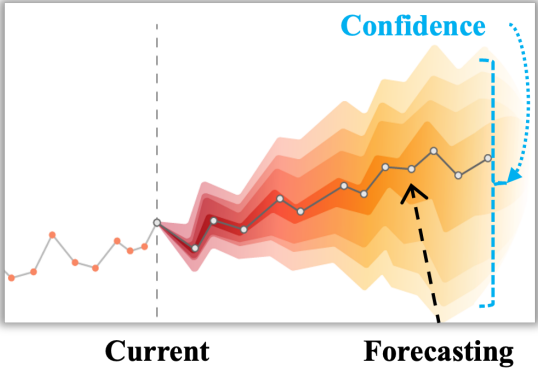
Uncertainty Analysis
不确定分析

(towards 幻觉和一致性等问题)

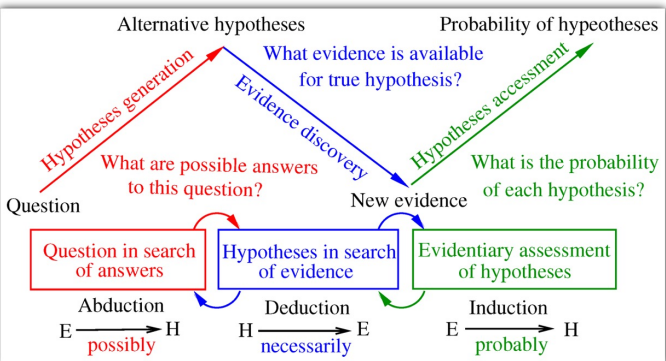


Quantification
& Optimization

Make Decision
with Confidence



Predictable PAC Learning Theory
可预测学习理论



Generalization bound with sequential Rademacher complexity

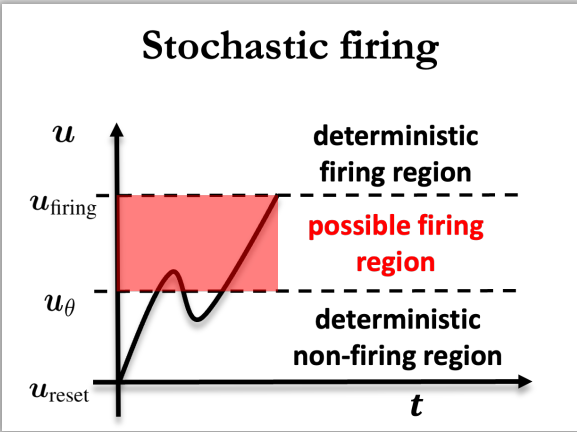
$$\mathbb{L}(h) \leq \widehat{\mathbb{L}}_p(h) + \boxed{\mathfrak{R}_p} + C_\ell \|\gamma\|_2 \sqrt{2 \log \left(\frac{\mathbb{E}_\sigma [\mathcal{M}_e(\chi, \mathcal{H}, \sigma)]}{\delta} \right)}$$

Discrepancy, estimated from Data Sequential complexity, related to non-stationarity

where

$$\mathfrak{R}_p = \sup_{h \in \mathcal{H}} \left[\mathbb{E}_{e_{T+1} \in \tilde{\mathbf{E}}} [\ell(h(e_{-(T+1)}), e_{T+1})] - \frac{1}{T} \left(\sum_{t=2}^T \gamma_t \mathbb{E}_{e_t \in \mathbf{E}} [\ell(h(e_{-t}), e_t)] + C \right) \right]$$

Bio-inspired Computing Theory
类脑计算理论



证明了首个关于脉冲神经网络的
万有逼近定理、结构稳定性、泛化性

Theorem 12 Let $\mathcal{F}_W^{one}$ denote the function space of L-layer stochastic neurons. If $u_{reset} = 0$, $\|W^l\|_2 \leq C_l$ for $l \in [L]$, and $\|X\|_2 \leq C_X$ for $X \in \mathcal{X}$, we have

$$\mathfrak{R}_n(\mathcal{L} \circ \mathcal{F}_W) \leq C_n \mathfrak{R}_n(\mathcal{F}_W) \leq \frac{(C_n)^L C_X}{\sqrt{n}} \left(\prod_{l \in [L]} C_l \right) (p_{max})^{(L+1)/2}, \quad (42)$$

where $p_{max} = \max_{i \in [n], l \in [L]} \{1 - \max\{p^{(l,i)}, p_\theta\}\} \in (0, 1)$ and C_n is a universal constant.

3.1. LLM 不确定性归因-评估体系

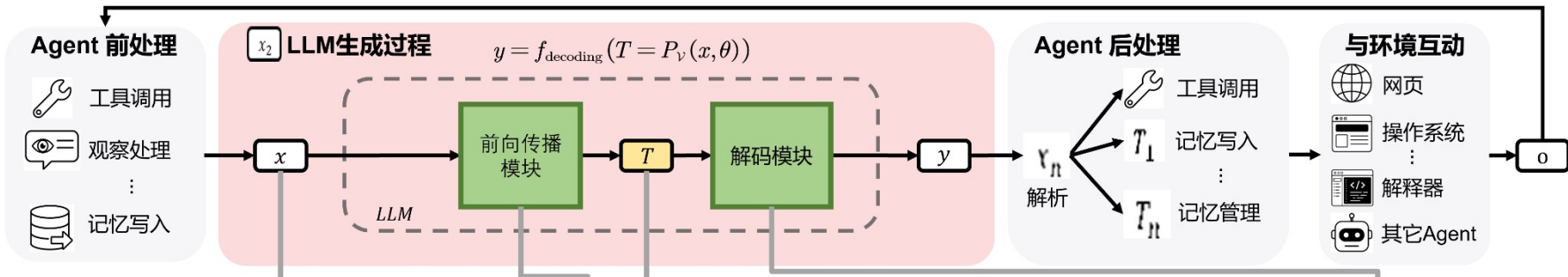
表象层

大模型驱动的Agent幻觉现象类型



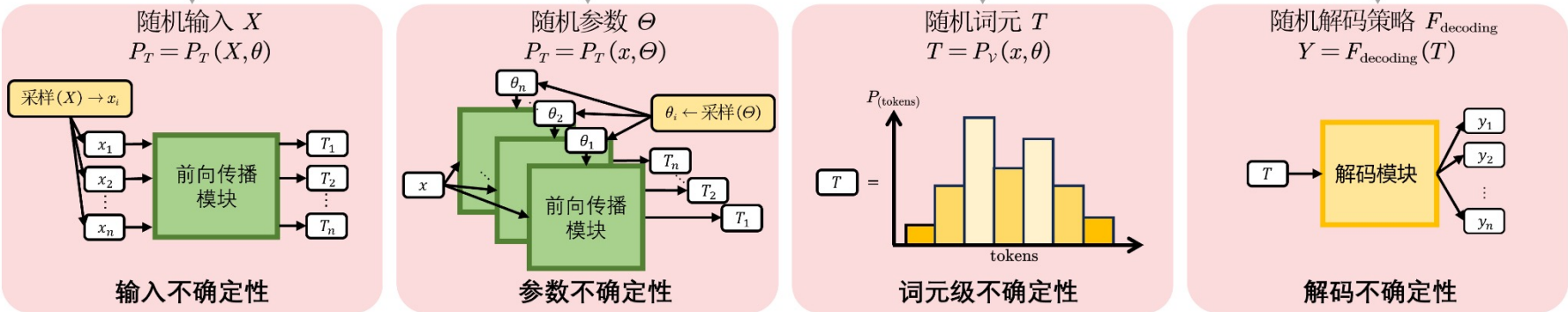
机制层

大模型驱动的Agent系统的交互与执行流程



根源层

大模型的内在随机性



3.2. 脑启发人工智能系列论坛



南京大学
NANJING UNIVERSITY



智能科学与技术学院
School of Intelligence Science and Technology

发起并组织深度技术论坛（执行主席，collaboration with 戴望州）

2024.11

2025.11

FUTURE

通往下一代人工智能 —
类脑智能的路径和未来

定义问题

- 探讨类脑智能的**释义**、**发展前景**、**实现路径**，输出整体演进路线
- 类脑不是科幻，而是**发展一代人工智能及突破算力瓶颈的切实路线**



智脑同行 — 探索神经启发与
智能融合的技术路径

求解方案

- 探讨人工智能和脑科学协同融合的**技术路径**
- 从“是什么”推进到“**怎么做**”



系列论坛
敬请期待

建立较为完备的脉冲计算理论体系

The following have been proved:

- ✓ ScSNN is a **universal approximator** to dynamical systems. **First**
- ✓ The parameter complexity of ScSNNs can be **exponentially smaller** than conventional artificial neural networks when approximating radial functions. **First**
- ✓ ScSNN has **polynomial approximation efficiency** for handling more difficult tasks. **Few**
- ✓ ScSNN enables **structural stability** of the SNN system. **First**
- ✓ StocSNN derives the **generalization** of SNNs. **First**
- ✓ The gradient estimation led by StocSNNs is **unbiased**. **First**

3.3.1. 脉冲神经网络的表示理论



Theorem 1 Let $K \subset \mathbb{R}^m$ be a compact set. If the spike excitation function f_e is l -finite and $w_i \in \mathbb{R}$ where $i \in [n]$, then for all $r \in [l]$, there exists some time t such that the set of IFR functions $f(\cdot, t) : K \rightarrow \mathbb{R}$ of the form $f(\mathbf{x}, t) = \sum_{i \in [n]} w_i f_i(\mathbf{x}, t)$ is dense in $\mathcal{C}^r(K, \mathbb{R})$.

通用近似性

ScSNNs can
universally approximate discrete
dynamical systems.

Studies	Universal Approximation		
	weight	activation	complexity
G. Cybenko (1989)	Real-valued	sigmoidal	Finite depth, Exponential width
Zhang & Zhou (2022)	Real-valued	spiking	Finite depth, Exponential width
F. Voigtlaender (2023)	Complex-valued	--	Finite depth, Exponential width

参数复杂度

Theorem 2 Given a compact set $K^m \subset \mathbb{R}^m$, a probability measure μ , and a radial function $g : K^m \rightarrow \mathbb{R}$. For some apposite spike excitation function f_e and any $\epsilon > 0$, there exists some time t such that the radial function g can be well approximated by a one-hidden-layer scSNN of $\mathcal{O}(C_m^{15/4})$ spiking neurons, that is,

$$\|f(\mathbf{x}, t) - g(\mathbf{x})\|_{L^2(\mu)} < \epsilon.$$

Theorem 2 [Zhang, Gao, & Zhou. Neural Netw'2022]

there exists a constant $\delta > 0$ such that

$$\mathbb{E}_{\mathbf{x} \sim \mu} (f_R(\mathbf{x}) - f(\mathbf{x}))^2 \geq \delta,$$

for any one-hidden-layer real-valued network $f_R : \mathbb{R}^{2d} \rightarrow \mathbb{R}$ with exponential parameter number $\mathcal{O}(C_1(2d+1)e^{C_1(2d)})$. Here, C_1 is a constant independent to d .

ScSNN: $\mathcal{O}(C_m^{15/4})$ polynomial

ANN: $\mathcal{O}(C_1(2d+1)e^{C_1(2d)})$ exponential

The parameter complexity of ScSNNs can be exponentially smaller than ANNs when approximating radial functions.

3.3.2. 脉冲神经网络的泛化理论



提出两个基于 Rademacher Complexity 的脉冲神经网络泛化界

Theorem 12 Let $\mathcal{F}_{\mathcal{W}}^{\text{one}}$ denote the function space of L -layer stochastic neurons. If $u_{\text{reset}} = 0$, $\|\mathbf{W}^l\|_2 \leq C_l$ for $l \in [L]$, and $\|\mathbf{X}\|_2 \leq C_X$ for $\mathbf{X} \in \mathcal{X}$, we have

$$\mathfrak{R}_n(\mathcal{L} \circ \mathcal{F}_{\mathcal{W}}) \leq C_n \mathfrak{R}_n(\mathcal{F}_{\mathcal{W}}) \leq \frac{(C_n)^L C_X}{\sqrt{n}} \left(\prod_{l \in [L]} C_l \right) (p_{\max})^{(L+1)/2}, \quad (42)$$

where $p_{\max} = \max_{i \in [n], l \in [L]} \{1 - \max\{p^{(l,i)}, p_\theta\}\} \in (0, 1)$ and C_n is a universal constant.

随机发射 SNN 的泛化界 (JMLR 2024)

Rademacher complexity of stochastic neurons can be upper bounded by an **exponential** function that consists of the **network depth** and **excitation probability**.

Theorem 1 (Generalization Bound for SNNs) Let $\mathcal{H}$ denote the function collection of L -layer SNNs with the width of N_w on the time interval $[0, T]$, the hypothesis space $\mathcal{H}$ is universally bounded according to $\|f\|_\infty \leq N_f$ for $f \in \mathcal{H}$, $\mathcal{D}$ is the distribution of sample variables $(\mathbf{X}, y)$, S_n indicates the collection of n pairs of training samples $(\mathbf{X}_i, y)$ where $i \in [n]$, and $L_2(S_n)$ denotes the data-dependent L^2 metric space. Assume that the norm value of connection weights is finite, that is, $\|w\| \leq M_w$. Let $\tilde{h} : [-N_f, N_f] \times [-N_f, N_f] \rightarrow \mathbb{R}$ denote the non-negative loss function, which satisfies that

- i) $\tilde{h}(\cdot, \cdot)$ is upper bounded by M_h , i.e., $\tilde{h}(f, f') \leq M_h$ for all $f(\cdot), f'(\cdot) \in [-N_f, N_f]$,
- ii) for any fixed $f \in [-N_f, N_f]$, the mapping $y \mapsto \tilde{h}(f, y)$ is L_h -Lipschitz for some $L_h > 0$.

Then with probability at least $1 - \delta$ where $\delta \in (0, 1)$, we have the generalization bound as follows

$$E(f) \leq \hat{E}(f) + 2L_h \hat{\mathfrak{R}}_n(\mathcal{H}) + 3M_h \sqrt{\frac{\log(2/\delta)}{2n}},$$

where $E(f) = \mathbb{E}_{(x,y) \sim \mathcal{D}}[\tilde{h}(f(w, \mathbf{X}), y)]$ denotes the expected error, $\hat{E}(f) = n^{-1} \sum_{i=1}^n \tilde{h}(f(w, \mathbf{X}_i), y_i)$ denotes the empirical error, and the empirical Rademacher complexity $\hat{\mathfrak{R}}_n(\mathcal{H})$ is bounded by

$$\hat{\mathfrak{R}}_n(\mathcal{H}) \leq \frac{128 T N_f N_w^{\frac{3}{2}} \log 2}{3\pi n} - 32 \sqrt{\frac{2 \log 2}{3\pi}} \sqrt{\frac{T N_f^2 N_w^{\frac{3}{2}}}{n}},$$

where $N_f \in \mathcal{O}[(TM_w)^L \exp(-TL)]$

通用 SNN 泛化界 (arXiv 2026)

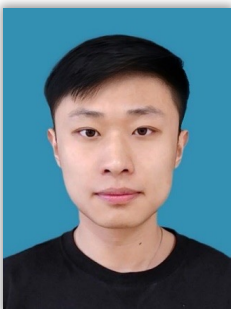
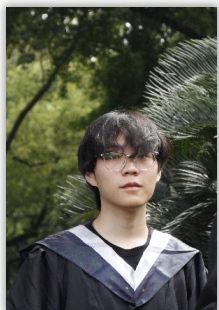
Empirical Rademacher complexity is **exponential** to the **network depth** and the **maximum time duration** of the received spike sequences, **superlinear and subquadratic** to the **network width**, polynomial to the parameter norm, and inverse linear to the number of training samples.

Table 1. Progresses on generalization bounds of SNNs.

Studies	Configurations	Approaches	Generalization Bounds
Maass & Schmitt (1997)	Single neuron with Temporal Coding	VC Dimension	$\text{VC} \in \Omega(n \log n)$ with regard to n samples
Schmitt (1999)	Binary and Analog Coding	VC Dimension	$\text{VC} \in \Omega(L N_w \log(L N_w))$ where L is the network depth.
Neuman et al. (2025)	Affine Network	Covering Numbers	$N_{\text{nc}} \in \mathcal{O}\left(\left(32 N_w^{5/2} + 48 L N_w M_w^2\right) n \exp\left(3 N_w^2\right)\right)$
Zhang et al. (2024)	Stochastic firing	Rademacher Complexity Dropout	$\hat{\mathfrak{R}}_n(\mathcal{H}) \in \mathcal{O}\left(C_w^L p_{\max}^{(L+1)/2}\right)$ where $p_{\max} \in [0, 1]$ and C_w universally relates to parameter w .
Zhang (2026)	Common-used Expressions in Eq. (1)	Rademacher Complexity Covering Numbers	$\hat{\mathfrak{R}}_n(\mathcal{H}) \in \mathcal{O}\left(n^{-1} M_w^L N_w^{3/2} T^{L+1} \exp(-TL)\right)$



Teams & Cooperation



Join us!



Academic & Cooperation



JS NHC PRC



Culture

